

Sublimation Ring of HD45677

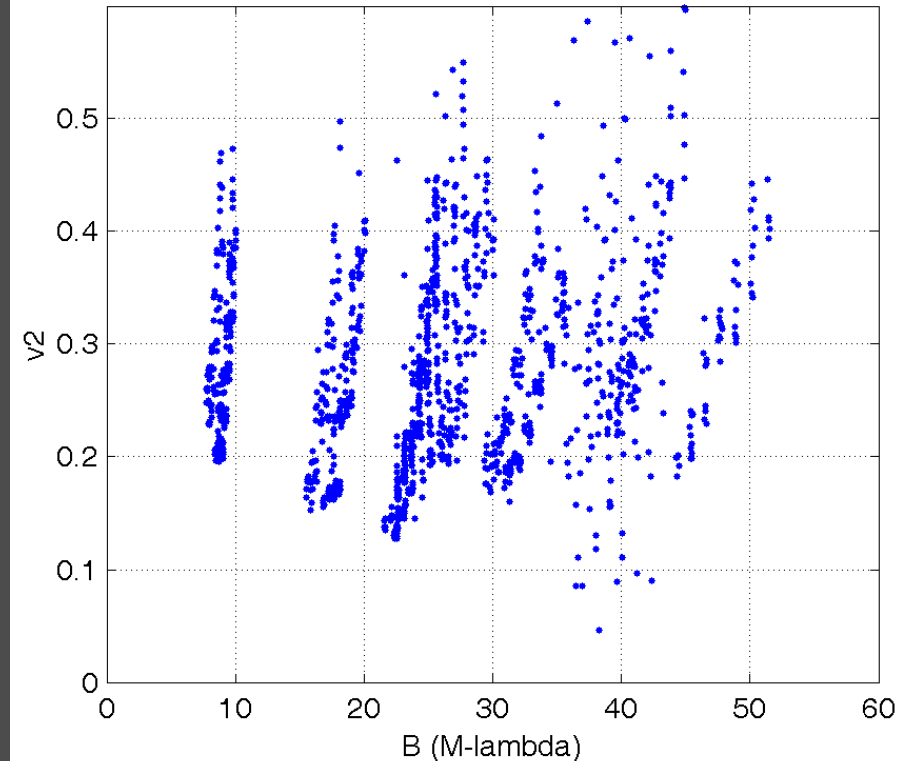
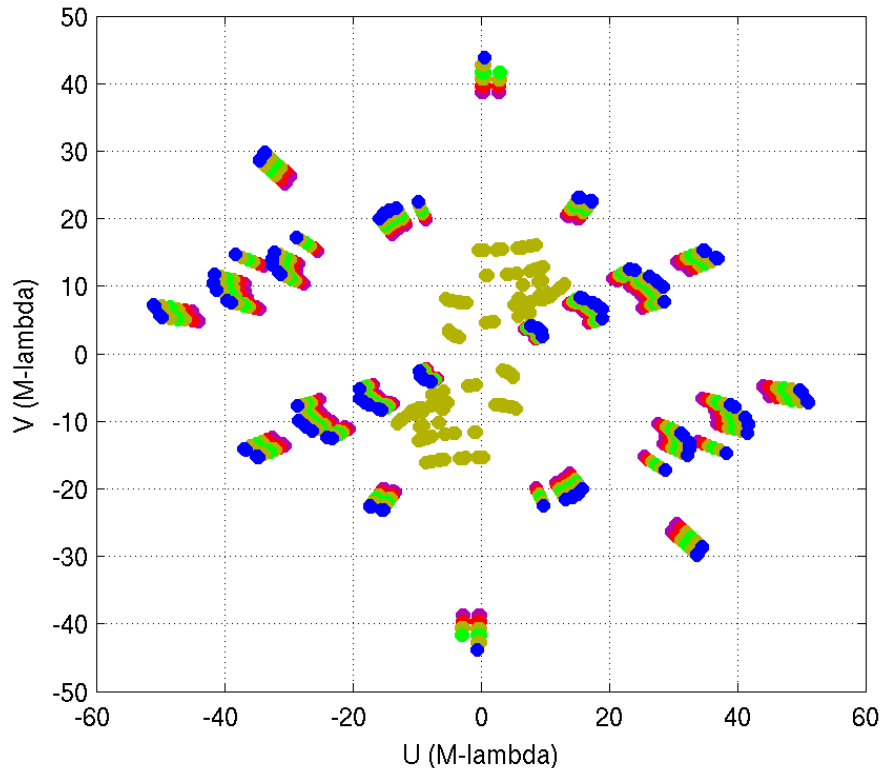
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Multi-Wavelength Interferometry – Pionier 1.55-1.8 μm

- Benefits and challenges...
- Extended UV coverage
- But... $B(x,y,\nu) = b(x,y) \times f(\nu)$?? NO

■ Dominant pattern is unrelated to spatial structure

UV baselines Pionier v1.8 + Iota



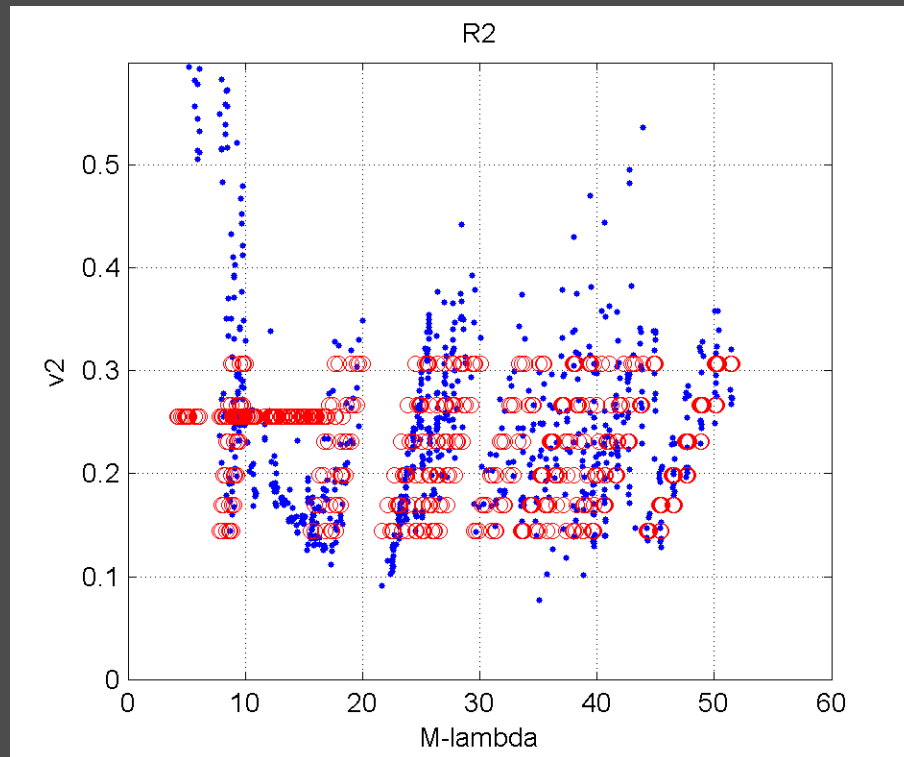
Adopted approach

- Parametric model fitting (no existing imaging package can cope with **non-grey** case)
- Complexify model **step by step**
- Model fitting is done **directly in UV plane**
- Fully **analytic** model for visibilities

1: Dilution with different spectral indices

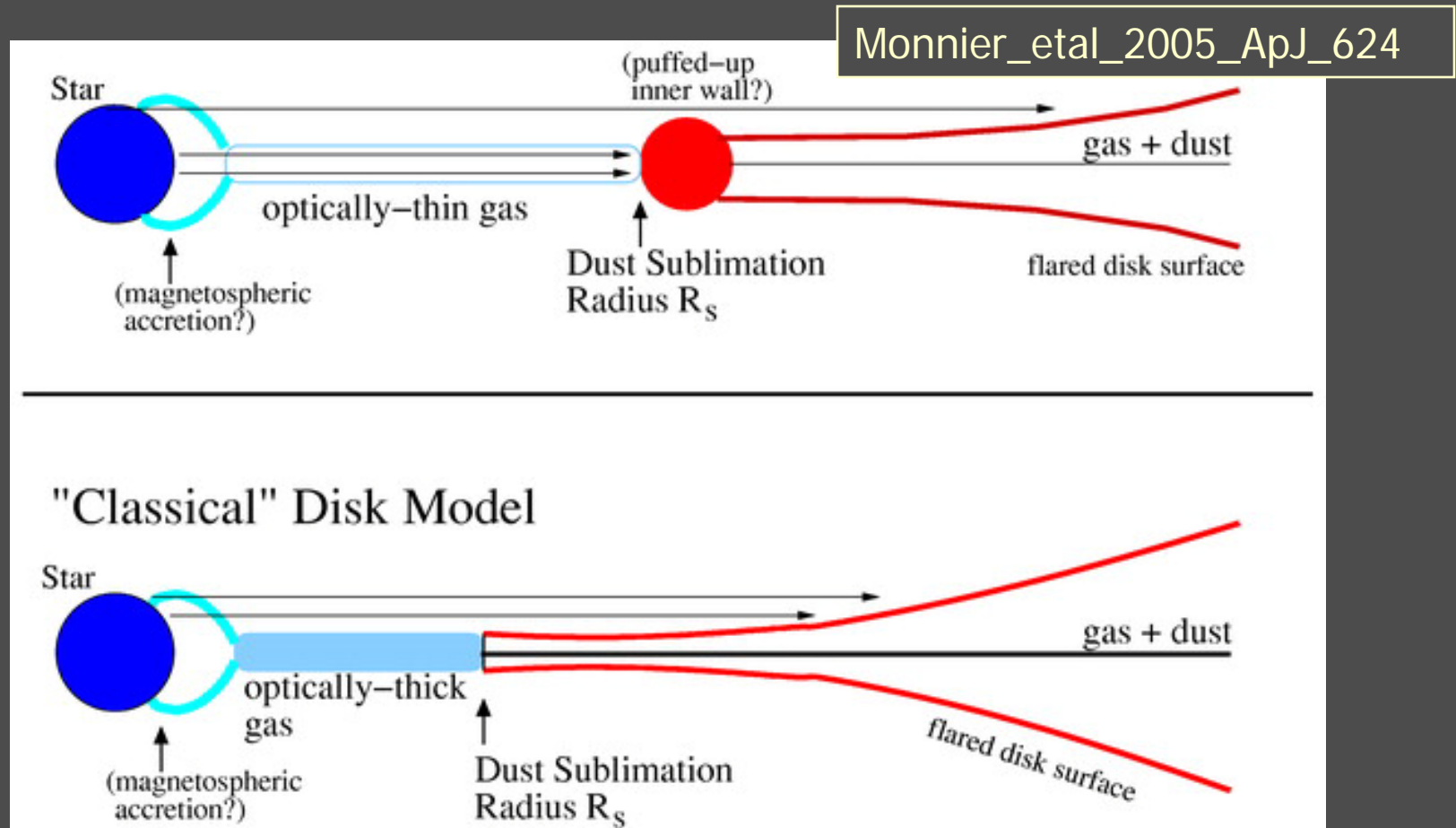
$$V = 1 \times (v/v_0)^2 / (1 \times (v/v_0)^2 + r_{flux} \times (v/v_0)^\kappa)$$

- Two components with different spectral indices κ
- Star $\kappa_S = +2$ (RJ régime)
- Nebula κ_N (free parameter)
- Reproduces "commas" with NO spatial structure in model



Spatial structure: why a ring?

- Circumstellar matter settles into disk
- Stellar radiation zaps grains out to sublimation radius
- → bright inner ring



2: Analytic model for bright rim

$$V_{neb}(u, v) = J_0(2\pi a \sqrt{u_c^2 + v_c^2})$$

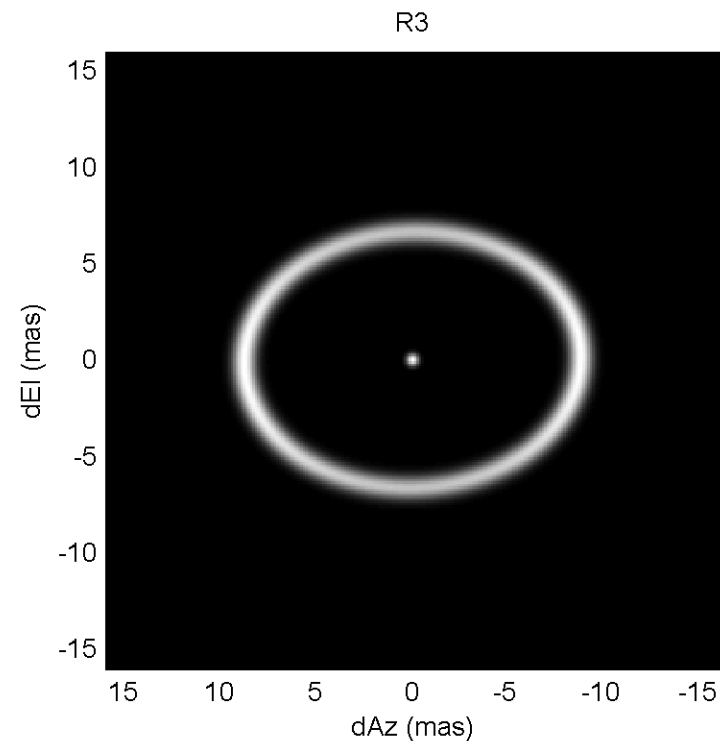
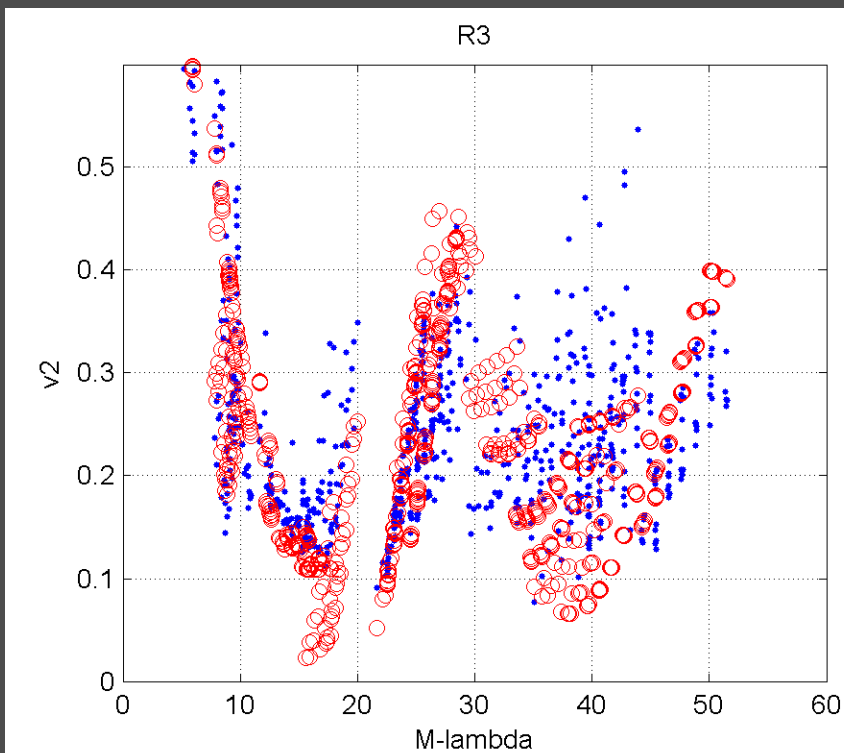
$$u_c = u_r \quad v_c = v_r \times (b/a)$$

$$\begin{pmatrix} u_r \\ v_r \end{pmatrix} = \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix} \cdot \begin{pmatrix} u \\ v \end{pmatrix}$$

■ Circular ring

■ Squeeze

■ Rotate



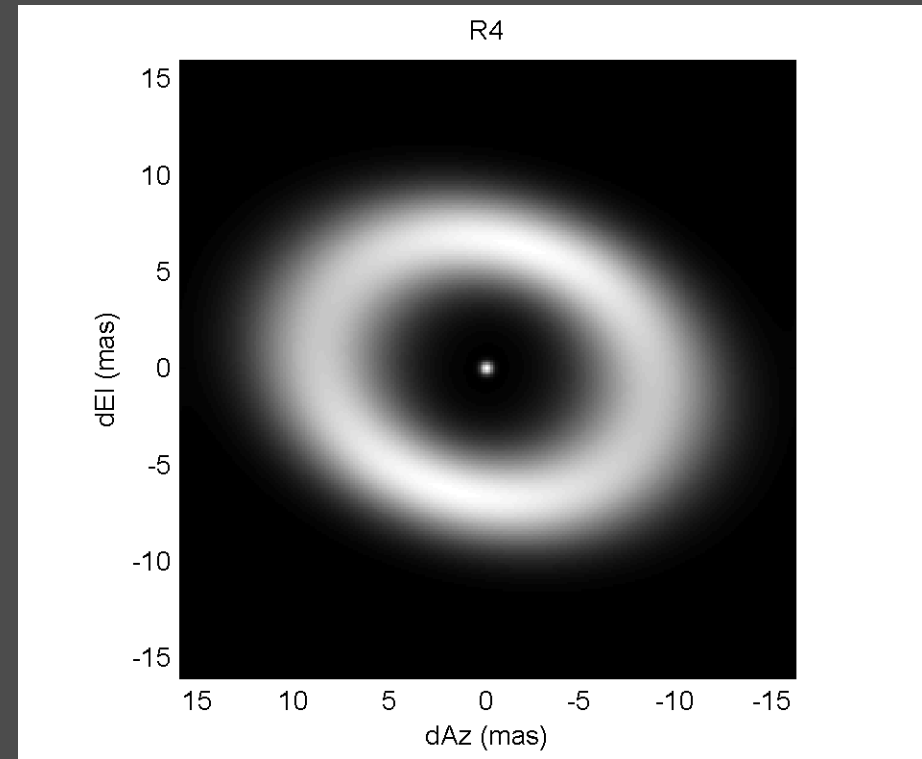
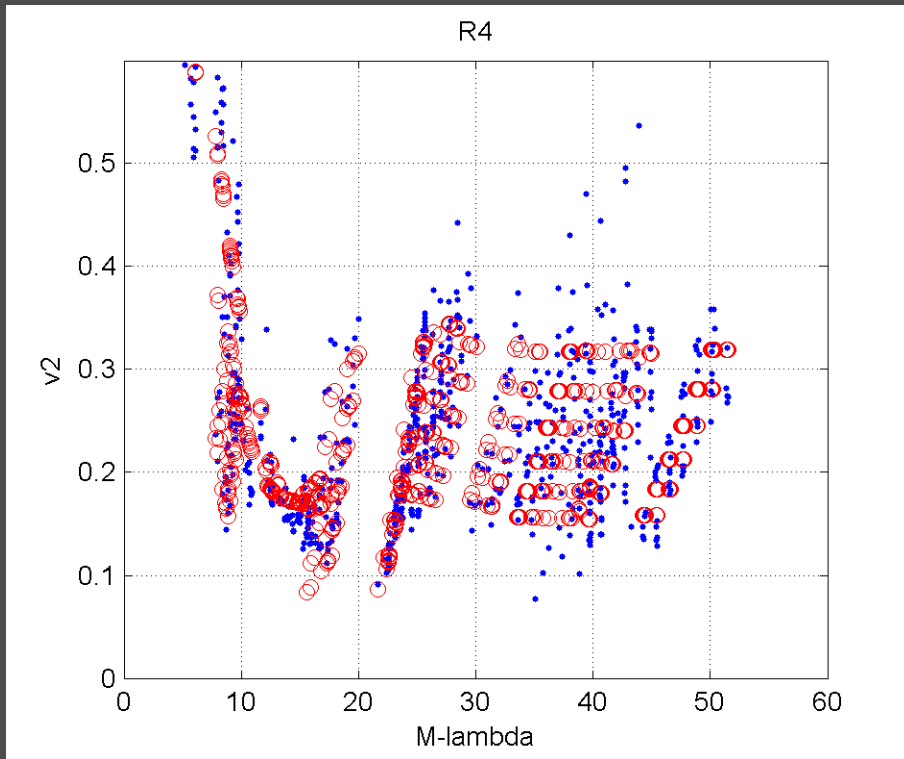
3: Put some flesh on the skeleton

- Convolve by gaussian

$$V_{neb}(u, v) = V_{neb}(u, v) \times \exp\left[-\frac{\pi^2}{4Ln(2)} \left((a_g u_r)^2 + (b_g v_r)^2 \right)\right]$$

- Multiplication is applied in ur vr coordinates
- ag bg : full width @half maximum
- Gaussian axes aligned with elliptical ring

3: Put some flesh on the skeleton



4: Azimuthal modulation

$$B(\vec{r}) = \delta(r - a) \cdot \begin{bmatrix} c_1 \cos \alpha + s_1 \sin \alpha + \\ c_2 \cos 2\alpha + s_2 \sin 2\alpha \end{bmatrix}$$

$$s = \sqrt{u_c^2 + v_c^2}$$

$$V_{neb}(u, v) = J_0(2\pi as)$$

$$-i(c_1 \cos \alpha + s_1 \sin \alpha) J_1(2\pi as)$$

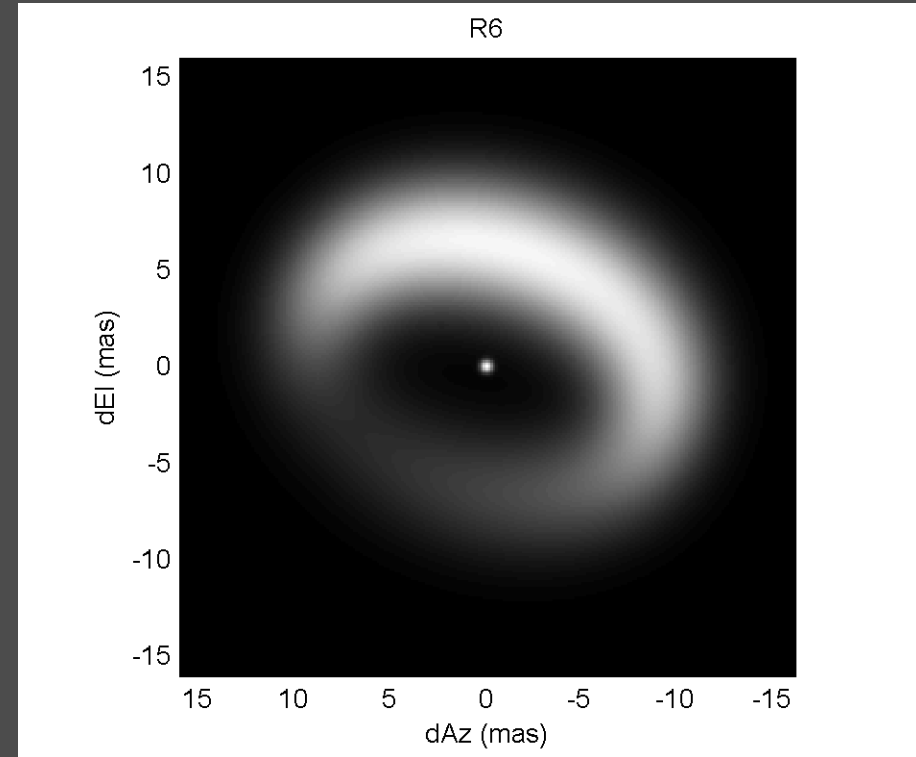
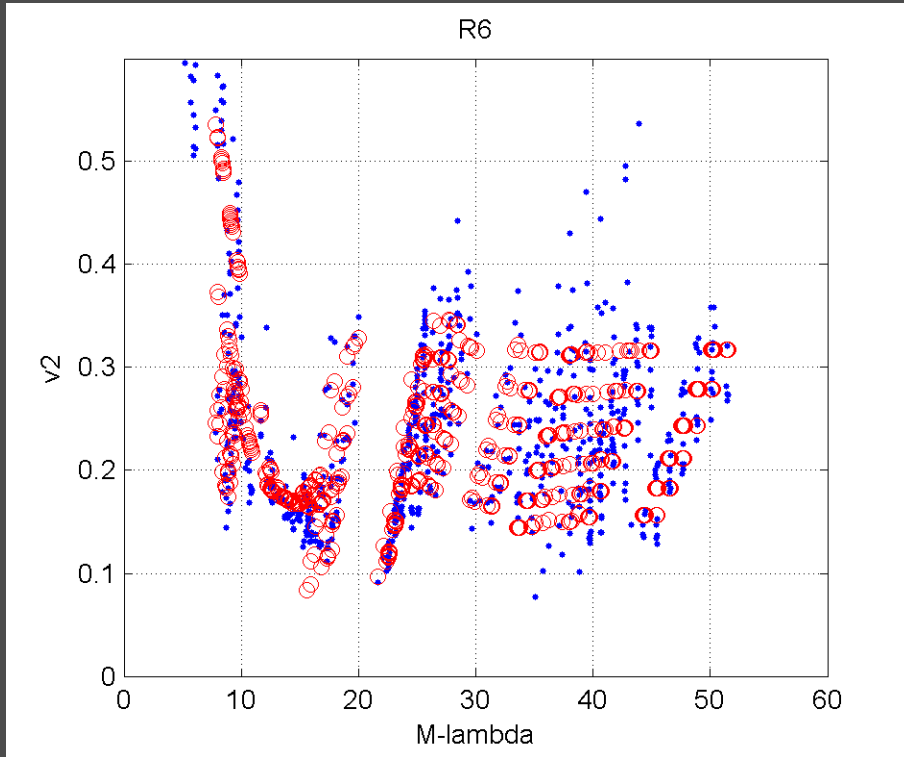
$$-(c_2 \cos 2\alpha + s_2 \sin 2\alpha) J_2(2\pi as)$$

- **Modulated circular ring (m=1, m2)**

- **Complex visibility**

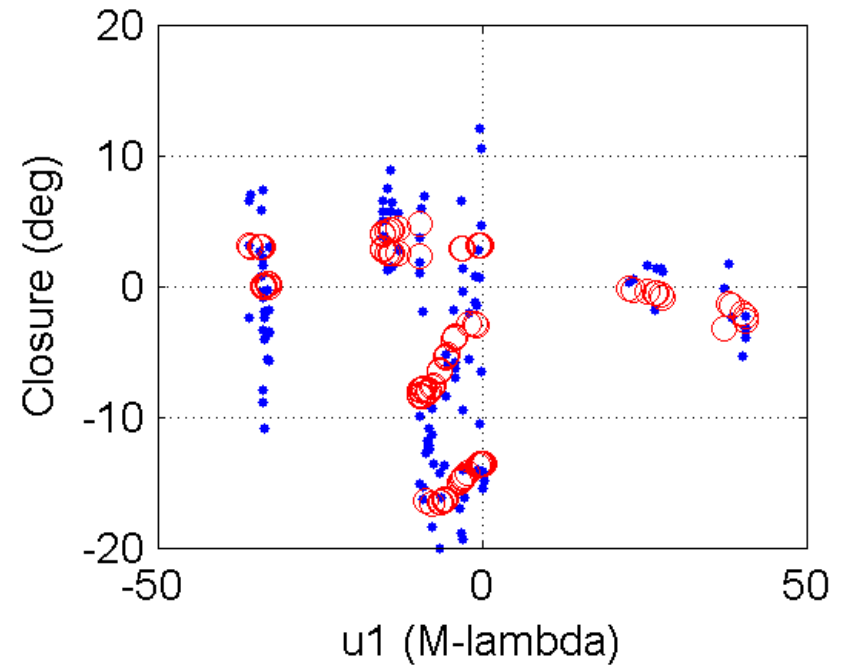
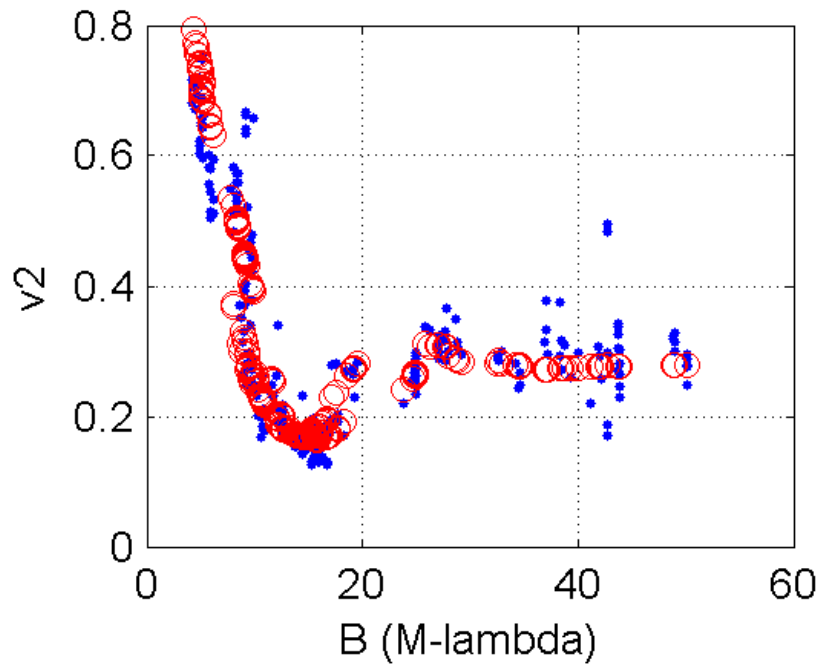
- **Then: squeeze and rotate as before**

4: Azimuthal modulation (m=1 + m=2)



Good agreement with Monnier et al 2006

4: Azimuthal modulation ($m=1 + m=2$)

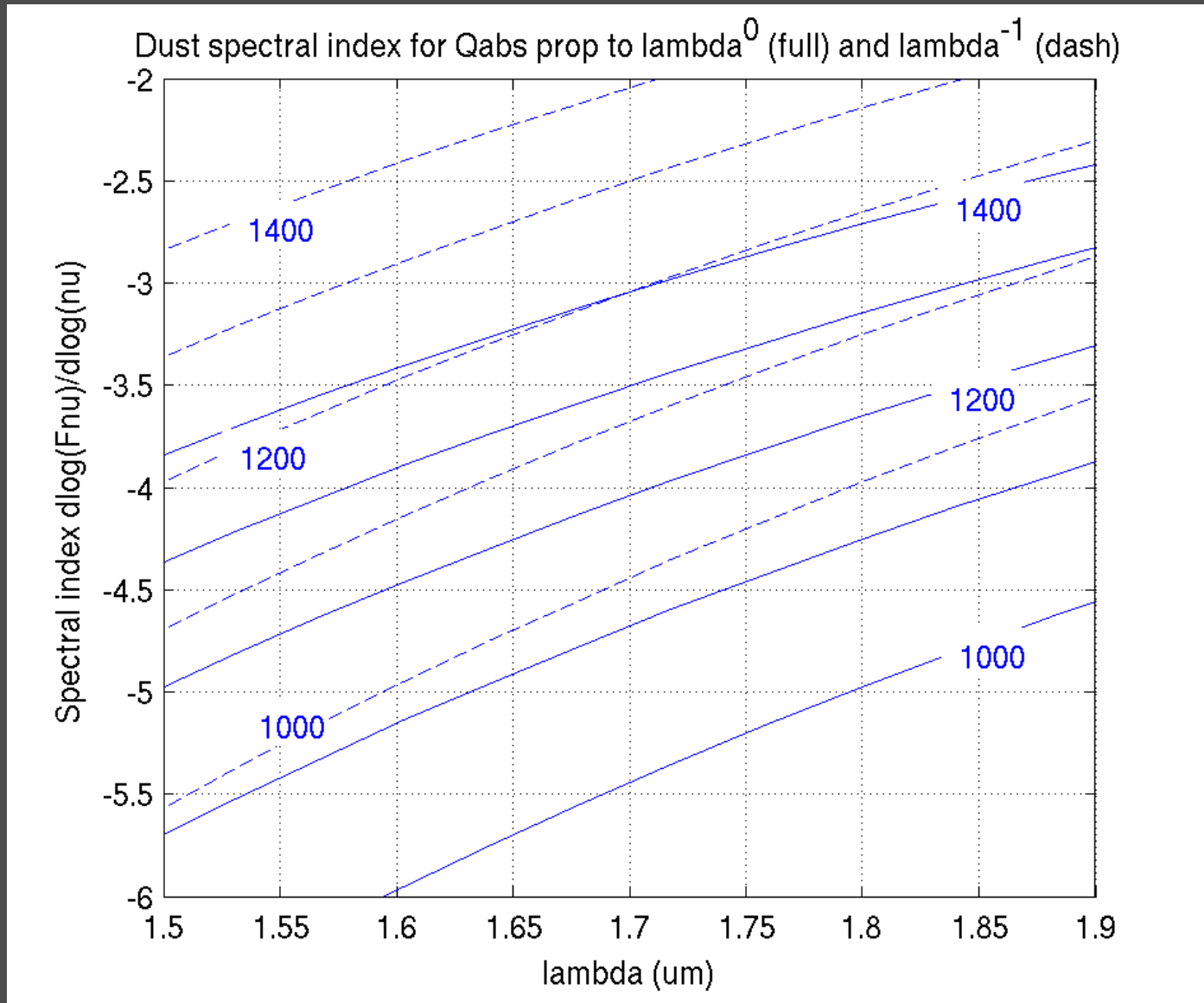


Final fit parameters

$F_{\text{NEB}}/F_{\text{STAR}}$	0.80
Nebular spectral index	-3.51
Semi major axis (mas)	9.59
Semi minor axis	6.37
P.A.	73°
Broadening	4.54 / 5.49
M=1 cos	-0.12
M=1 sin	0.78
M=2 cos	-0.29
M=2 sin	0.10

$$\chi^2 \approx 3$$

Dust temperature



Dust sublimation radius

- From dust properties (Laor & Draine 1993)

$$\theta_{sub} = \frac{r_{sub}}{d} = 34 \times 10^{-0.2[V_0 + BC]}$$

- Independent of distance
- Plug in values for HD45677

$$\theta_{sub} = 7.7 \text{ mas}$$