

**CONSTRAINING THE DARK MATTER PROPERTIES IN  
INTERMEDIATE REDSHIFT CLUSTERS OF GALAXIES**

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Université Paul Sabatier

in collaboration with

SOUCAIL G., LIMOUSIN M., RICHARD J. (Lensing team)  
POINTECOUTEAU E., ARNAUD M. & PRATT G.W. (Xray team)

# SCIENTIFIC GOALS

Clusters of galaxies are useful for :

- + cosmology tool : number counts, mass function
- + formation/evolution of structures : signature of non grav. process in scaling relations (*e.g.*  $M$ - $T_x$ ), redshift evolution, self-similarity

 Need reliable **mass estimators**

difficult @ high  $z$   $\longrightarrow$  combine different data sets : **Xrays** and **lensing**

in **this work** : preliminary results from a **lensing analysis**  
of a sample of galaxy clusters

# Xrays DATA

## XMM-Newton Large Programme

(P.I. M. Arnaud)

unbiased, flux limited sample

20 clusters

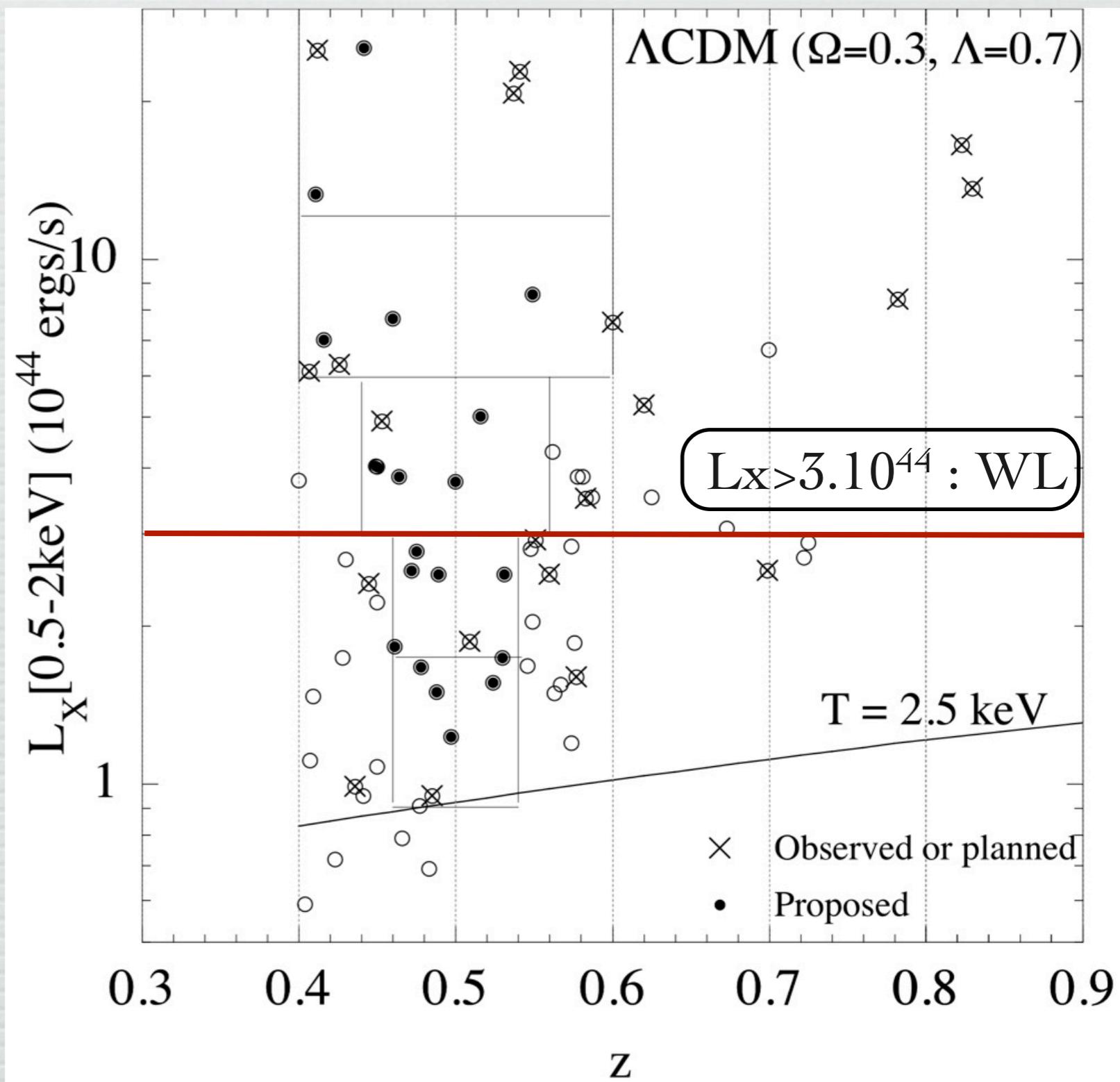
$2.5 \text{ keV} < kT < 12 \text{ keV}$

$0.4 < z < 0.6$

good sampling of  $L_x$

total exposure time  $\sim 1.1 \text{ Msec}$

defined as the REXCESS  
sample to compare at low  $z$



## Megacam @ CFHT

(P.I. G. Soucail)

11 brightest clusters  
( $L_x > 3 \cdot 10^{44}$  erg/s)

$g'$  (1.6ksec),  $r'$  (7.2ksec)

$i'$  (1.2ksec),  $z'$  (1.8ksec)

- homogeneous obs.
- good seeing ( $< 0.8''$  for  $r'$ )
- low  $m_c$  ( $\sim 26$  for  $r'$ )

weak lensing

+ strong lensing (4 clusters)

# LENSING DATA

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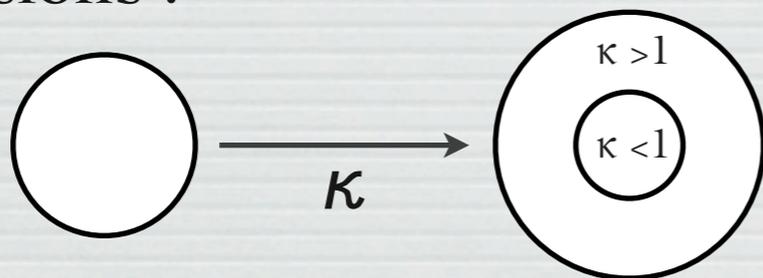


# GRAVITATIONAL LENSING BASICS

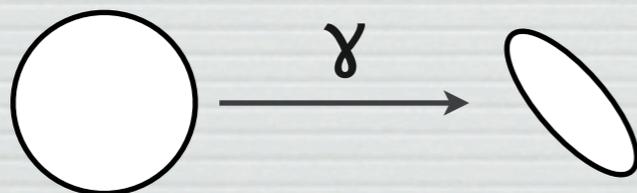
Deflection of the light by a mass  
 $=f(\text{grav. potential})$

2 grav. distortions :

convergence



shear



high mass density (center) : strong lensing --> arcs, multiple images

low density (outskirt) : **weak lensing** --> small distortions, stat. approach

background galaxy ~ ellipse  $\mathbf{e} = e_1 + ie_2$   $\longrightarrow$  source/image relation :  $e = \frac{e^{(s)} + g}{1 + g^* e^{(s)}}$

- select galaxies behind a cluster
- measure  $\langle e \rangle$ , assume  $\langle e^s \rangle = 0$
- $\rightarrow g = f(\text{grav. pot., universe geometry})$
- $\rightarrow$  mass

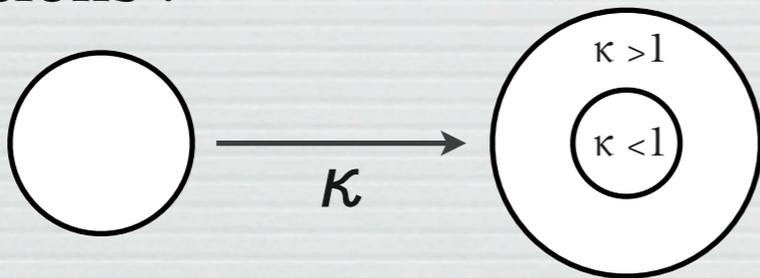
with reduced shear  $g = \frac{\gamma}{1 - \kappa}$

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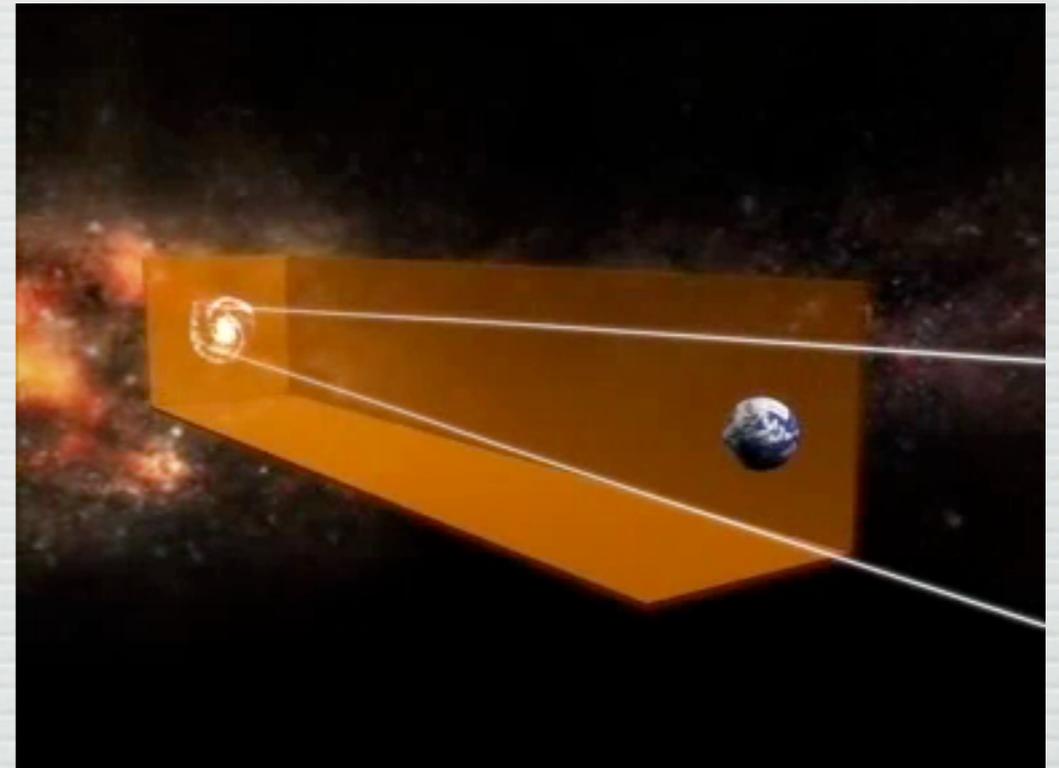
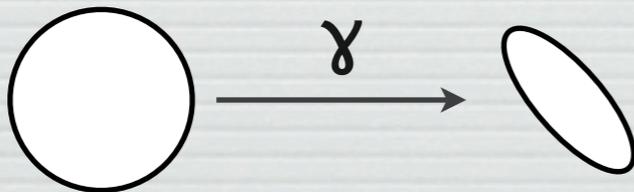
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with reduced shear  $g = \frac{\gamma}{1 - \kappa}$

# WEAK LENSING

- star/galaxy separation
- background members
- shape parameters
- geometry of the system

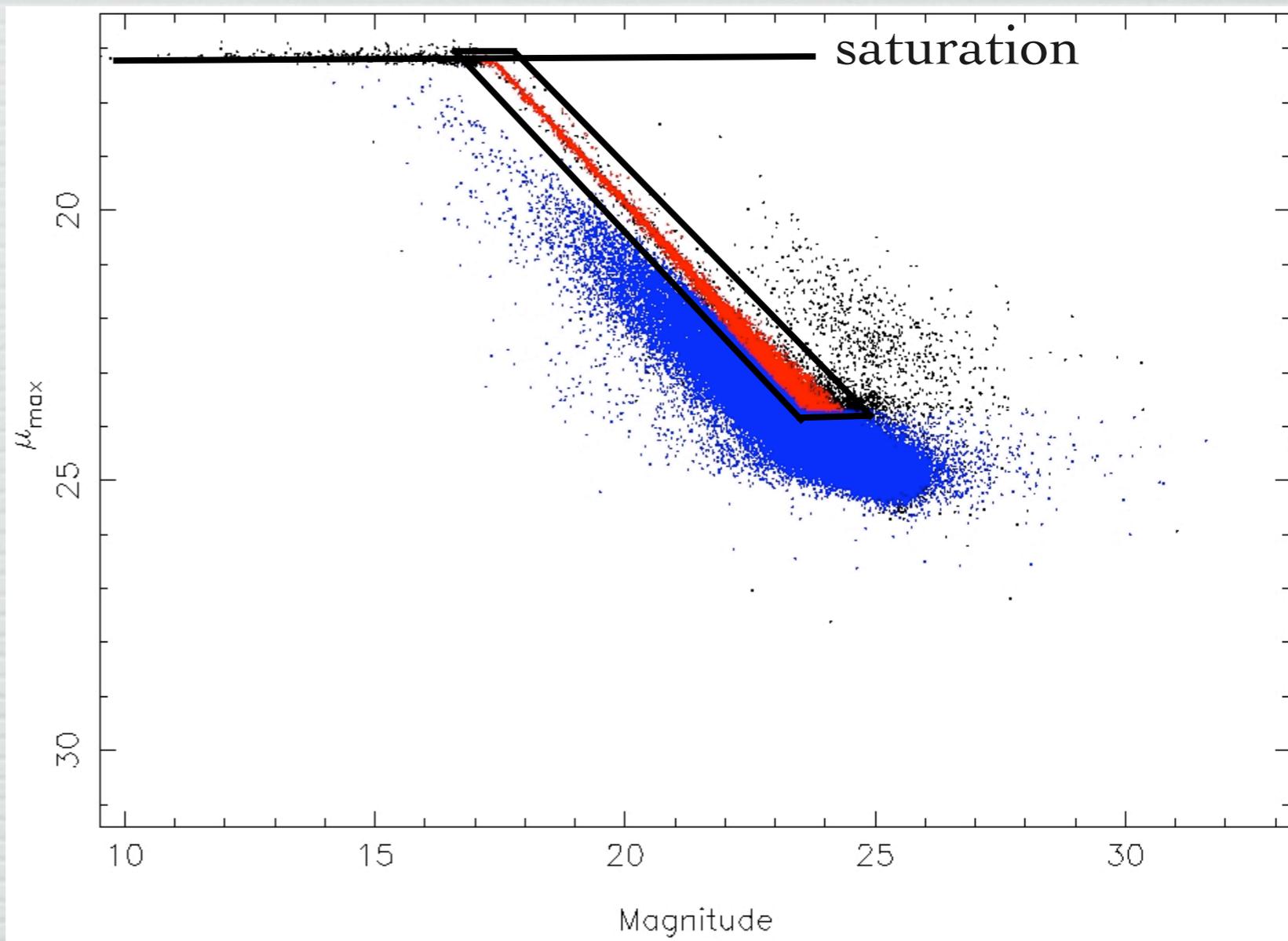
**SExtractor**

(dual mode on chi2 image)

→ **stars** (PSF estimation)

→ **galaxies** (lensing sources)

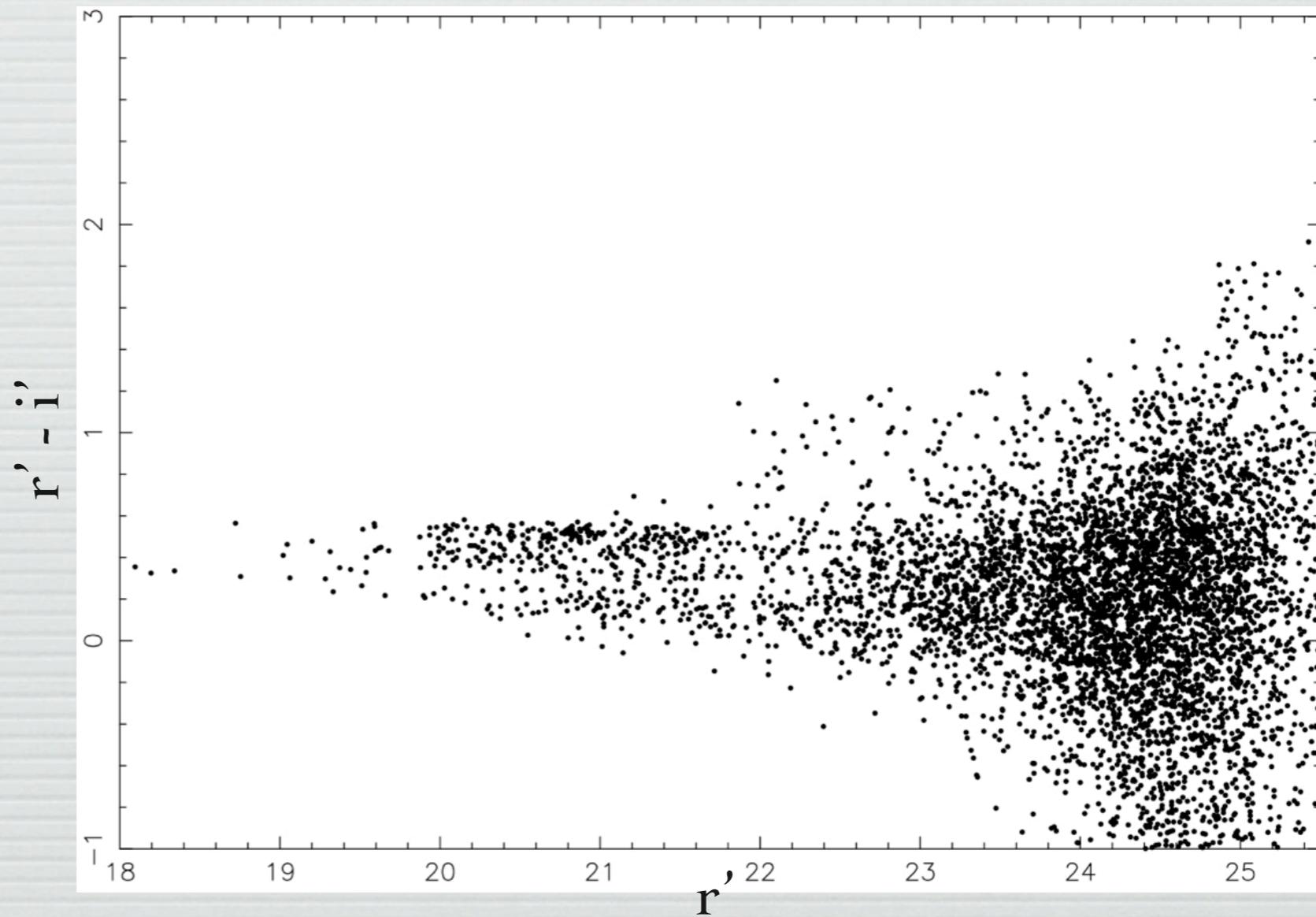
mag/flux + size/stellarity criteria



RXJ1120.0+3254

# WEAK LENSING

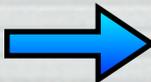
- star/galaxy separation
  - background members
  - shape parameters
  - geometry of the system
- 

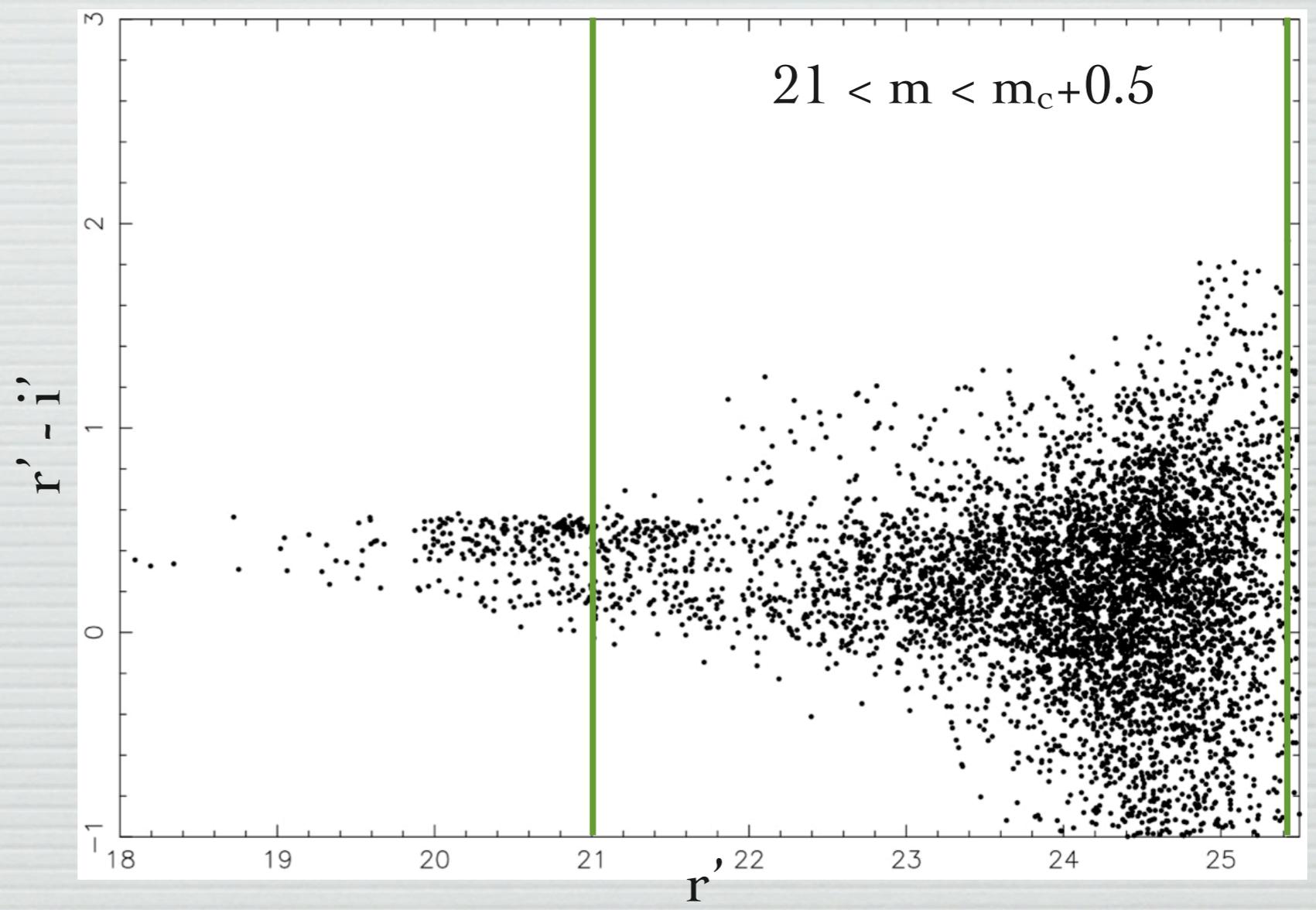


RXJ2228.5+2036

# WEAK LENSING

- star/galaxy separation
- background members
- shape parameters
- geometry of the system

 magnitude cuts

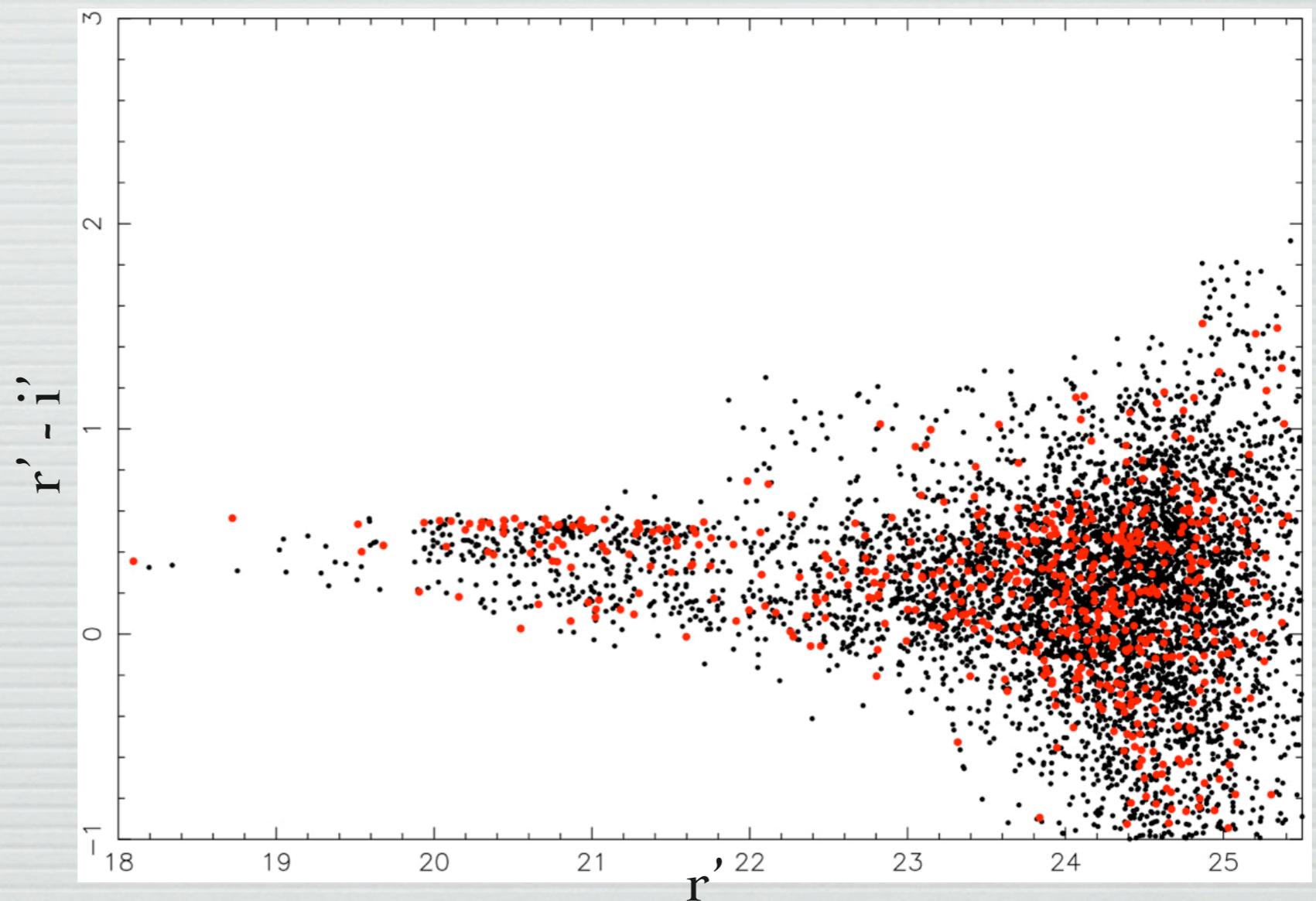


RXJ2228.5+2036

# WEAK LENSING

- star/galaxy separation
- background members
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- geometry of the system

- 
- ➔ magnitude cuts
  - ➔ red sequence

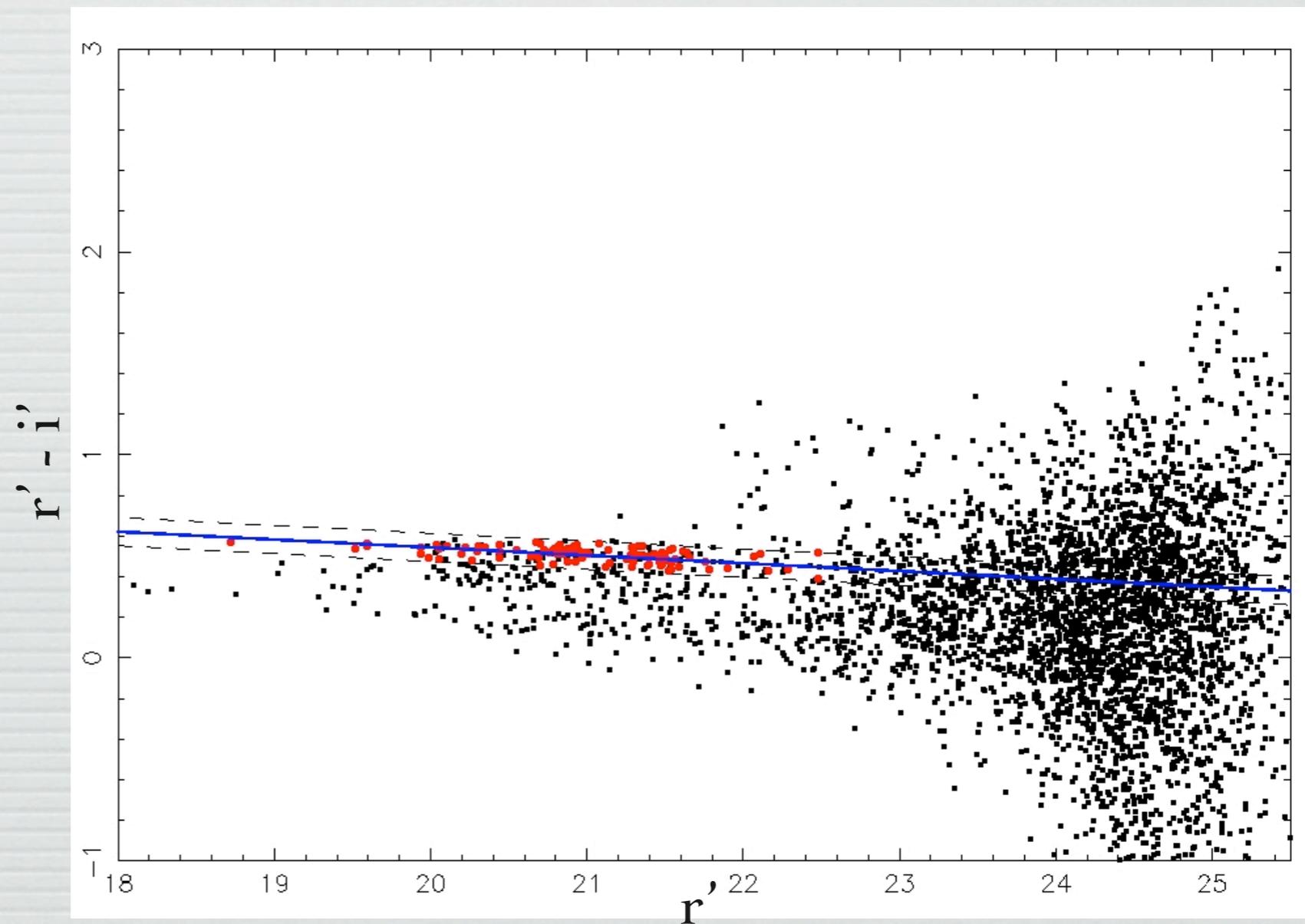


RXJ2228.5+2036

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RXJ2228.5+2036

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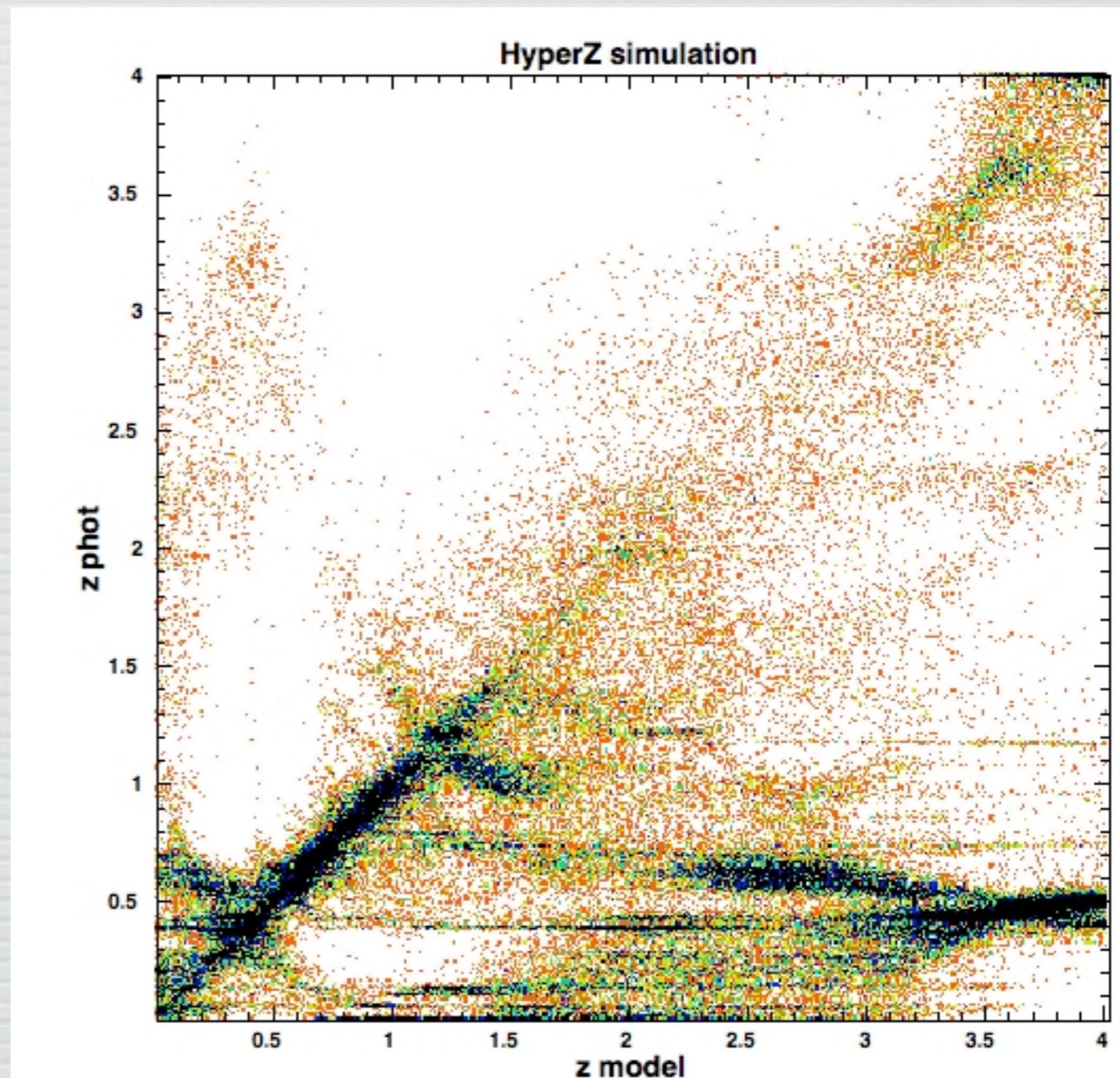
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→ magnitude cuts

→ red sequence

high  $z$  = high foreground contamination = need more than mag cuts

→ photo\_z **HyperZ** (R. Pello)



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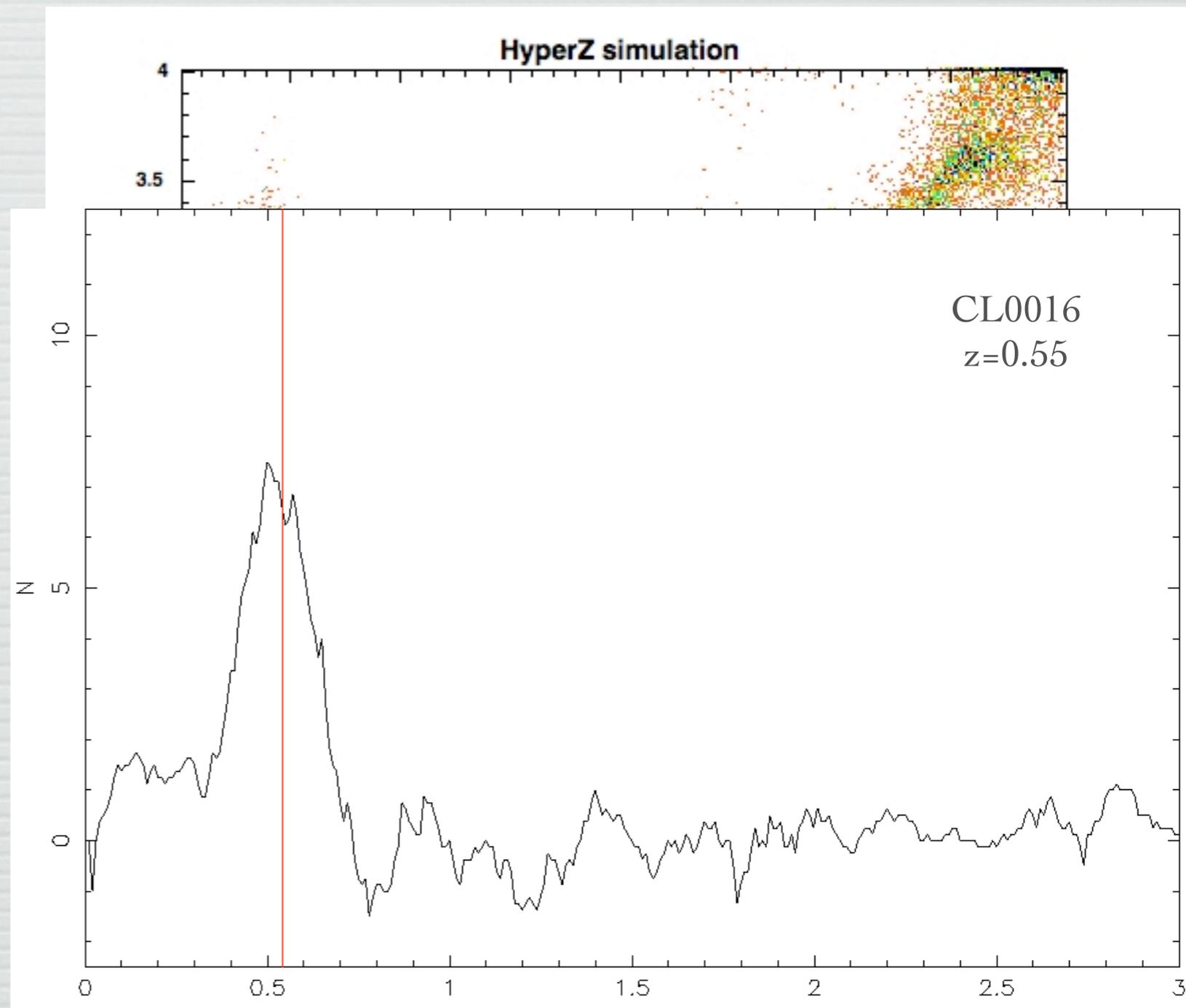
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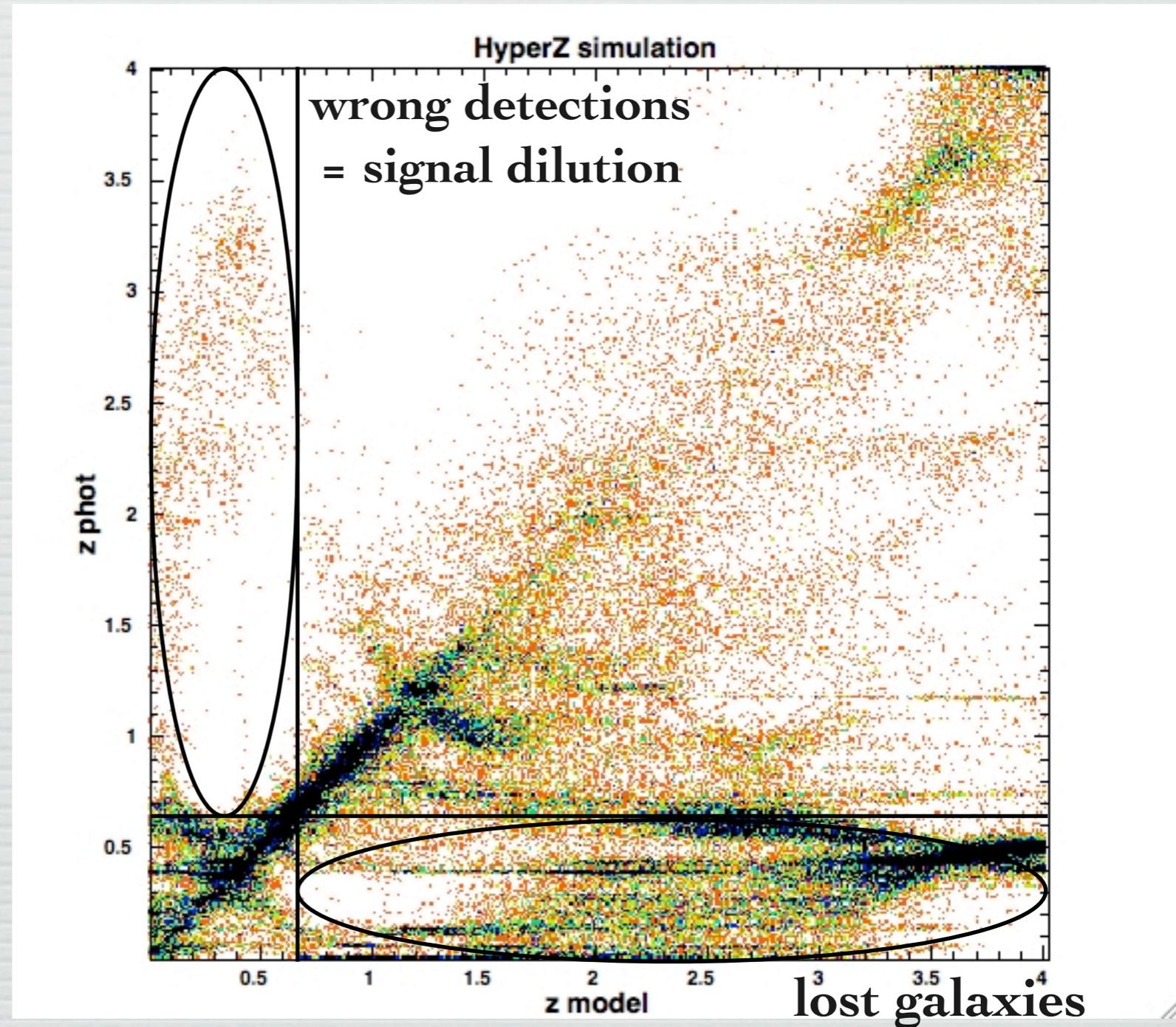
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- ➔ red sequence

high  $z$  = high foreground contamination = need more than mag cuts

➔ photo\_z **HyperZ** (R. Pello)



$z_{\text{phot}}$  challenging with 4 bands --> PDZ only as a proba. criterion for  $z < z_c$  or  $z > z_c$

# WEAK LENSING

- star/galaxy separation
- background members
- shape parameters (r' image)
- geometry of the system

---

**Im2shape** (S. Bridle)

# WEAK LENSING

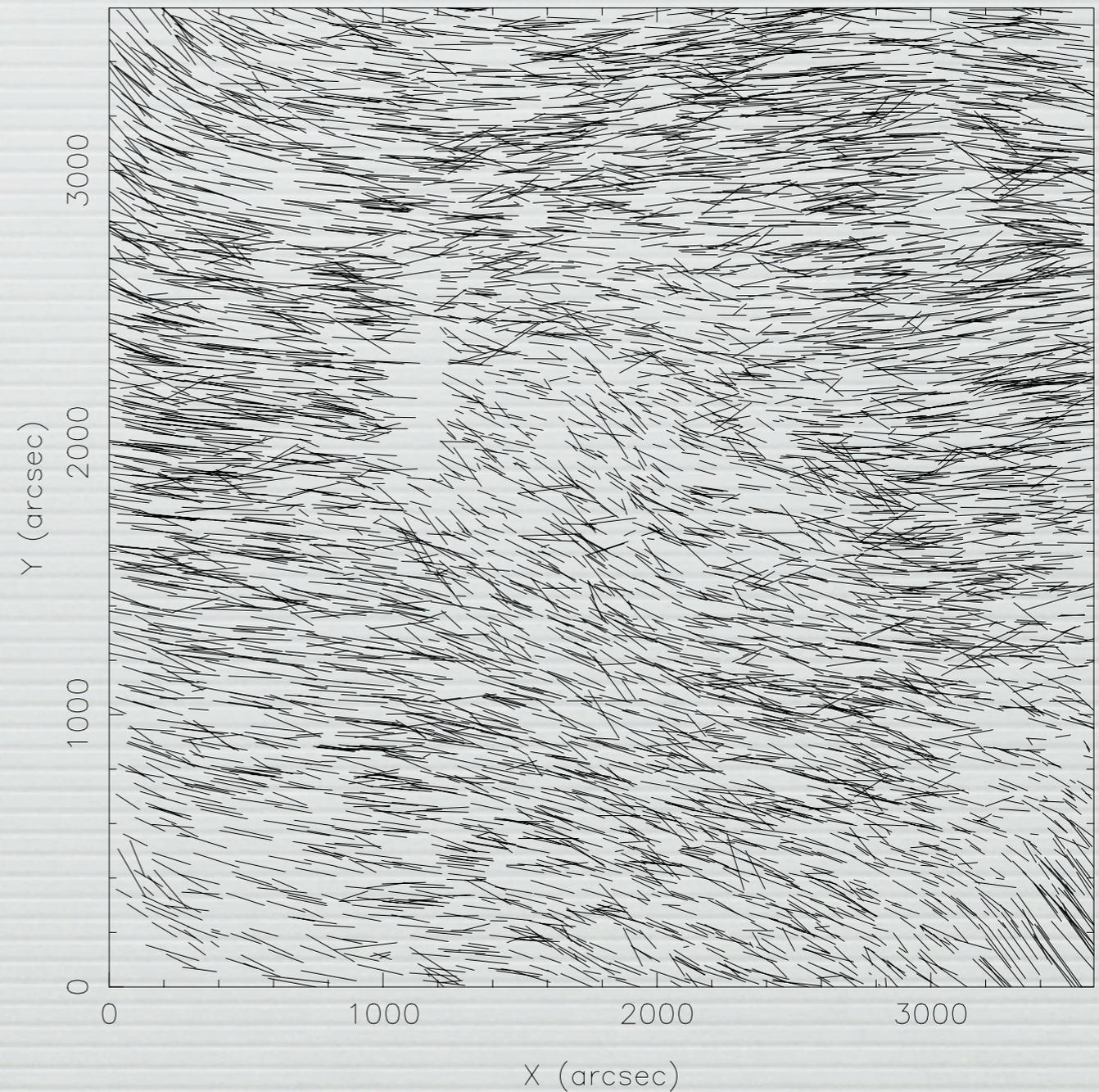
- star/galaxy separation
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- geometry of the system

---

**Im2shape** (S. Briddle)

**→** 1st run on stars = **PSF**

RXJ0856r : 5302 best selected stars



RXJ0856.1+3756

# WEAK LENSING

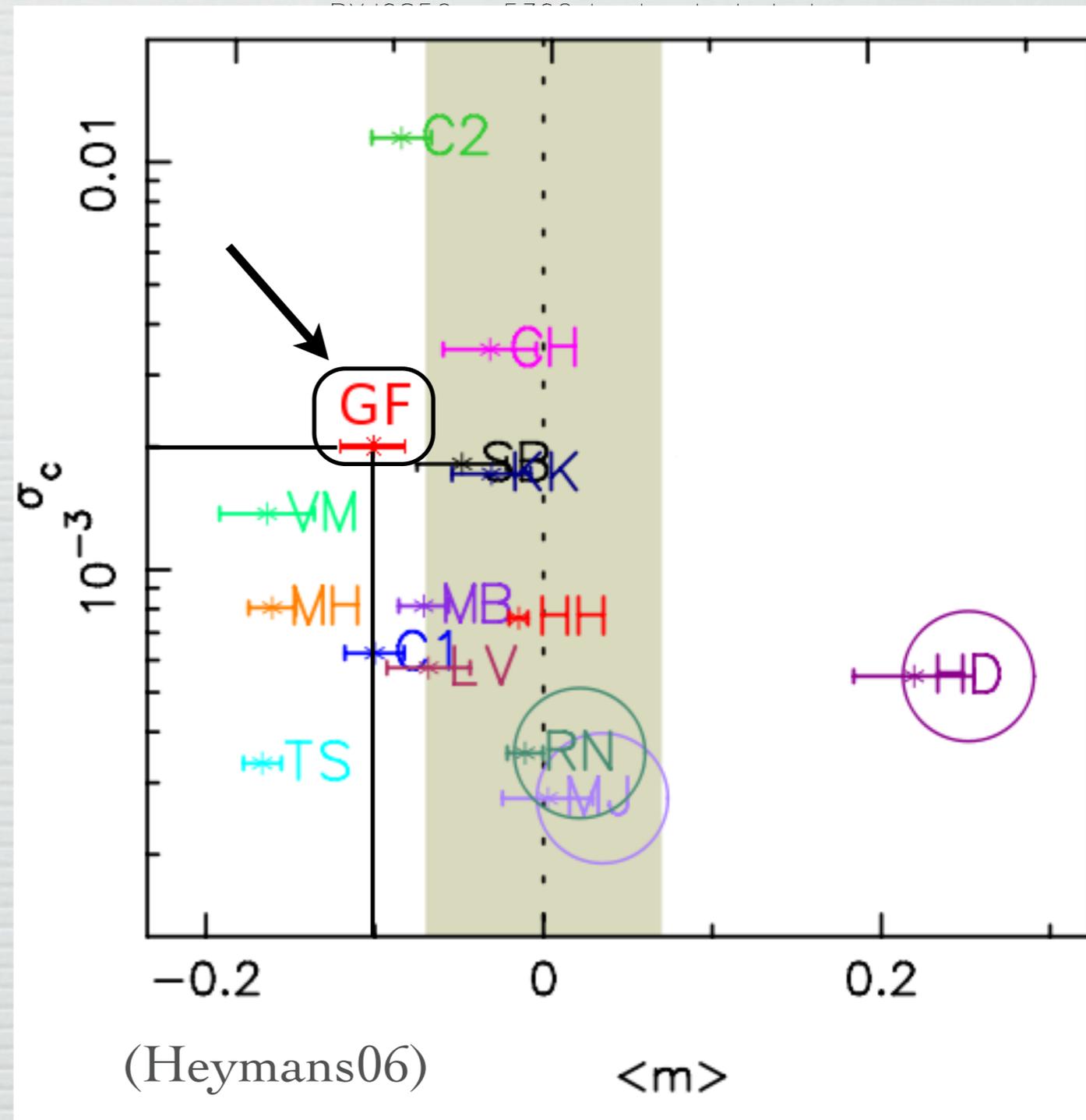
- star/galaxy separation
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- shape parameters (r' image)
- geometry of the system

**Im2shape** (S. Bridle)

- ➔ 1st run on stars = **PSF**
- ➔ 2nd run on galaxies  
(fit gauss\*PSF)
- ➔ tested on **STEP** simu.  
(Shear **T**esting **P**rogramme)

$$\gamma_1 - \gamma_1^{true} = q(\gamma_1^{true})^2 + m\gamma_1^{true} + c_1$$

$q = 0$   $\langle m \rangle \sim -0.1$   $\sigma_c \sim 2 \cdot 10^{-3}$  ➔ underestimation  $\sim 10\%$  of the shear



# WEAK LENSING

- ☑ star/galaxy separation
- ☑ background members
- ☑ shape parameters
- ☑ geometry of the system

➔ geometrical factor  $\beta(z_s) = D_{ls}/D_s$

$$g = \frac{\gamma}{1 - \kappa} = \frac{\beta_s \gamma^\infty}{1 - \beta_s \kappa^\infty}$$

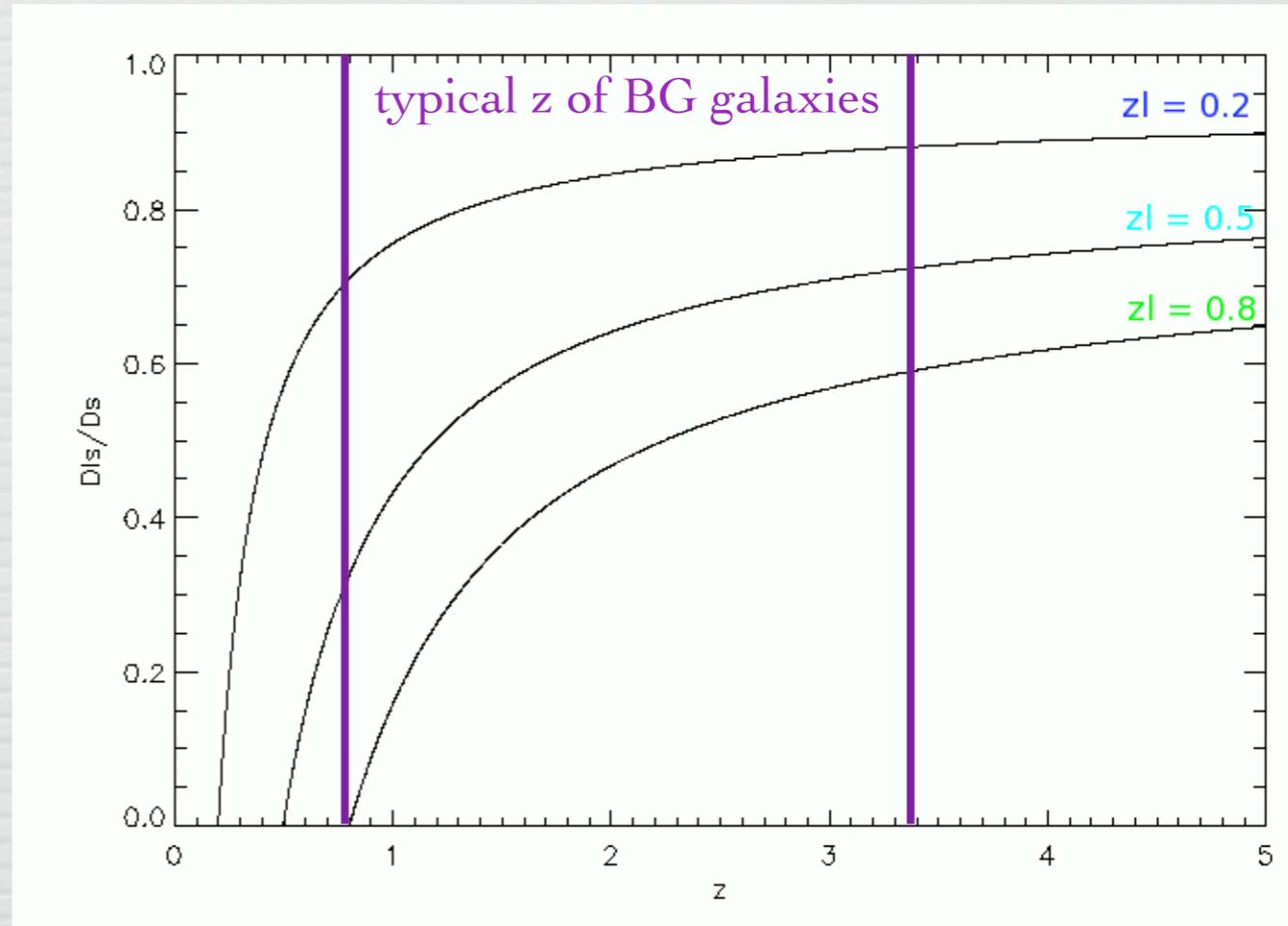
weak lensing

average of BG galaxies :  $\langle g(z) \rangle \sim \langle \gamma(z) \rangle = \langle \beta(z) \rangle \cdot \gamma^\infty$

low  $z_l$  :  $\langle \beta(z) \rangle \sim \beta(\langle z \rangle) \sim \beta(1)$

high  $z_l$  :  $\langle \beta(z) \rangle = \frac{\int_{z_l}^{z_{max}} p(z) \beta(z) dz}{\int_{z_l}^{z_{max}} p(z) dz}$

➔  $p(z) ?$



- + deep obs. with same instrument
- + more filters (ugriz)
- + catalogue of calibrated zphot (private comm.)

# WEAK LENSING

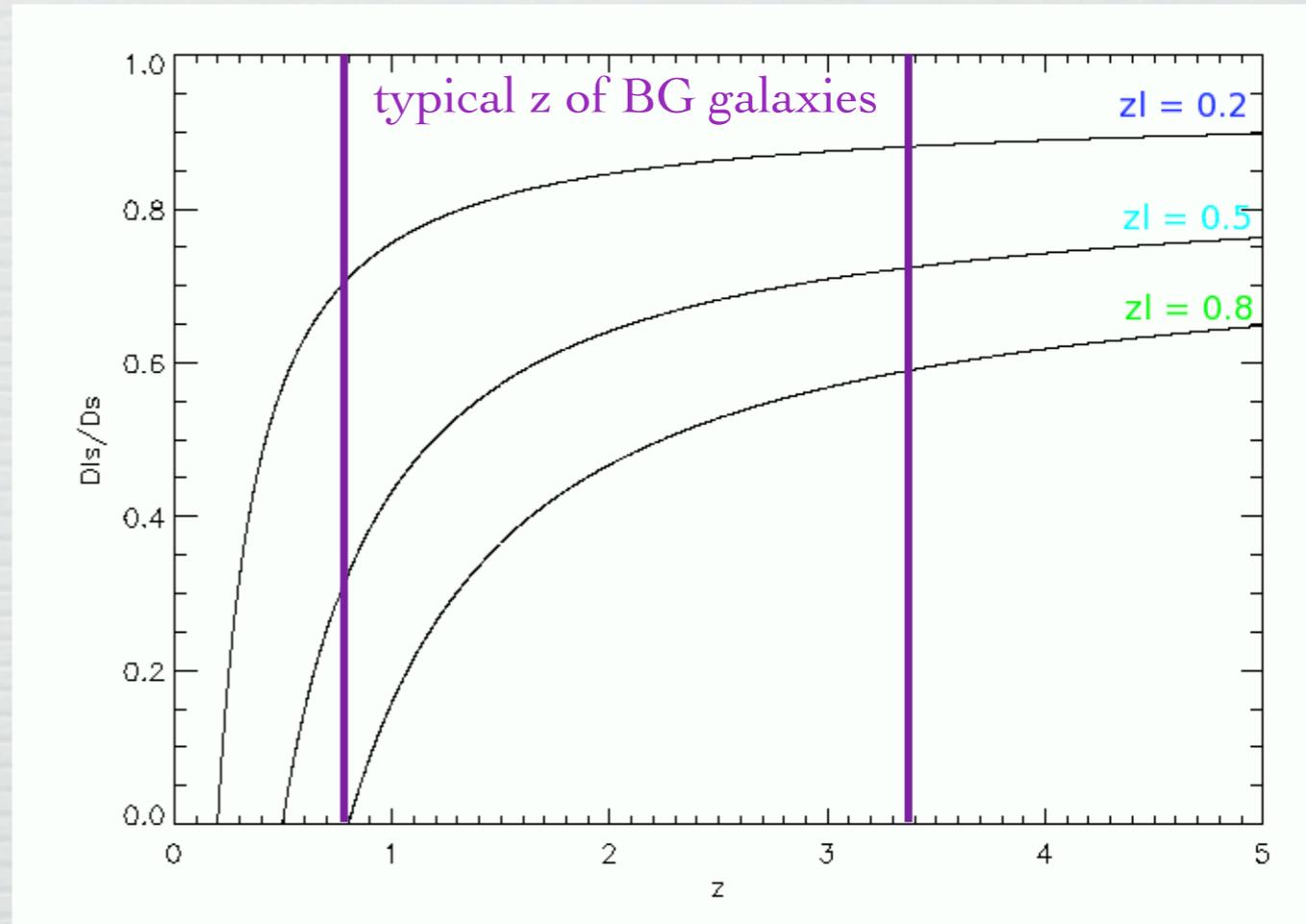
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$\rightarrow p(z) ?$

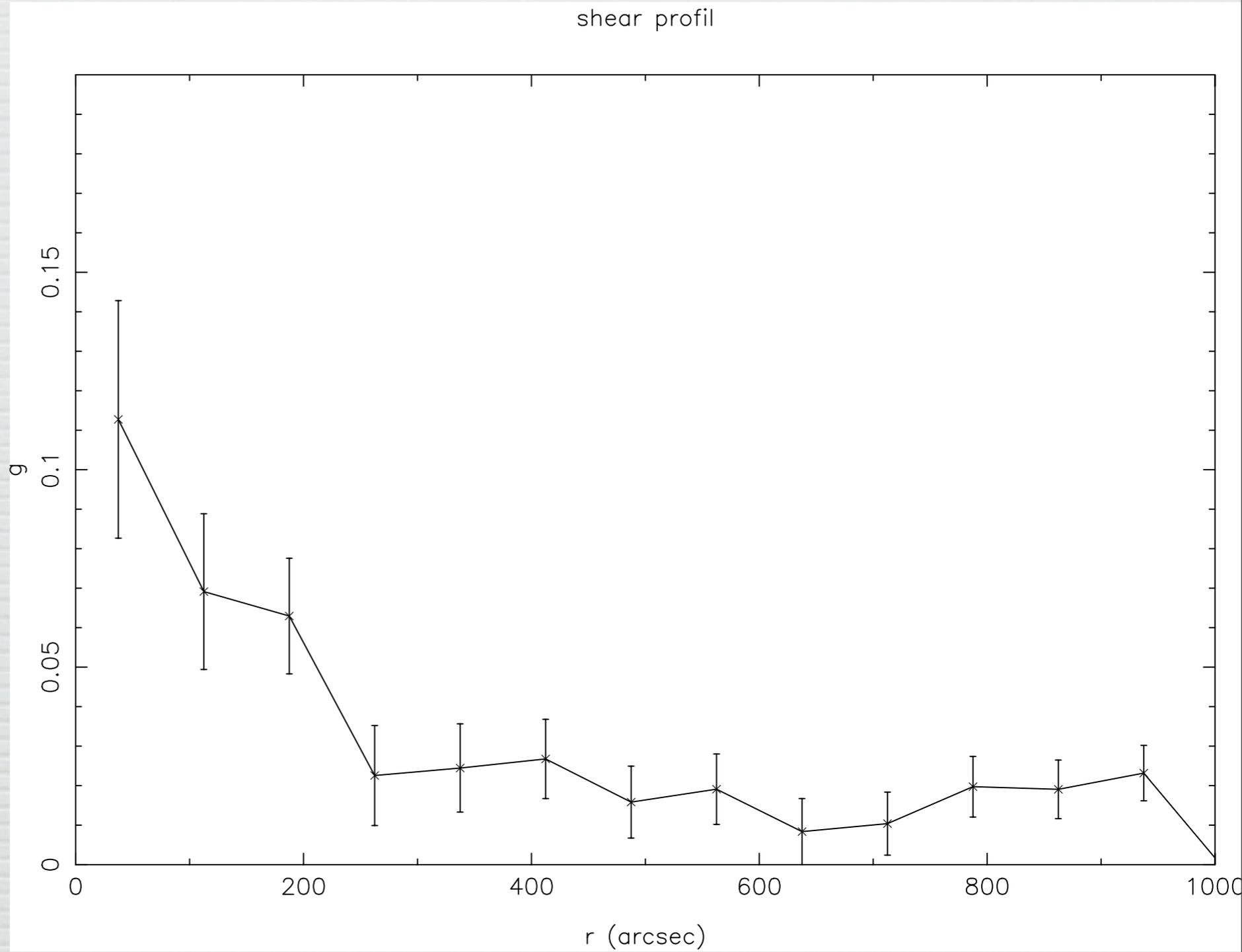
**CFHTLS-Deep** (T0004 release)

- + deep obs. with same instrument
- + more filters (ugriz)
- + catalogue of calibrated zphot (private comm.)

# MASS ESTIMATION

1D analysis : shear profile

model fitting



MACSJ1206.2-0848

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1D analysis : shear profile

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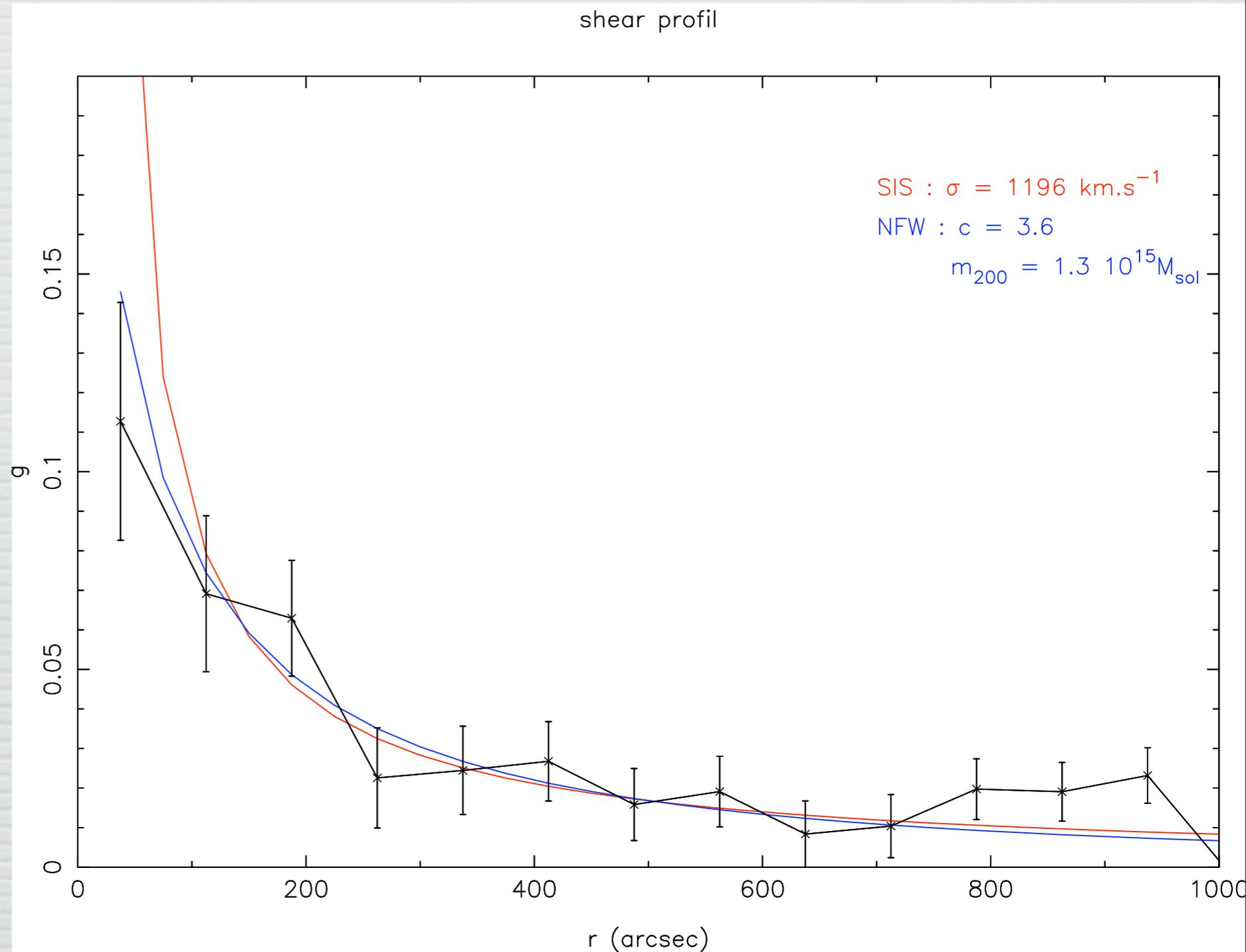
- SIS (velocity dispersion)
- NFW (c, virial mass)

analytical g

$\chi^2$  with  $\langle e_{\tan} \rangle \sim g^{\text{obs}}$

best fit parameters

analytical mass profil



MACSJ1206.2-0848

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1D analysis : shear profile

model fitting

- SIS (velocity dispersion)
- NFW (c, virial mass)



analytical g



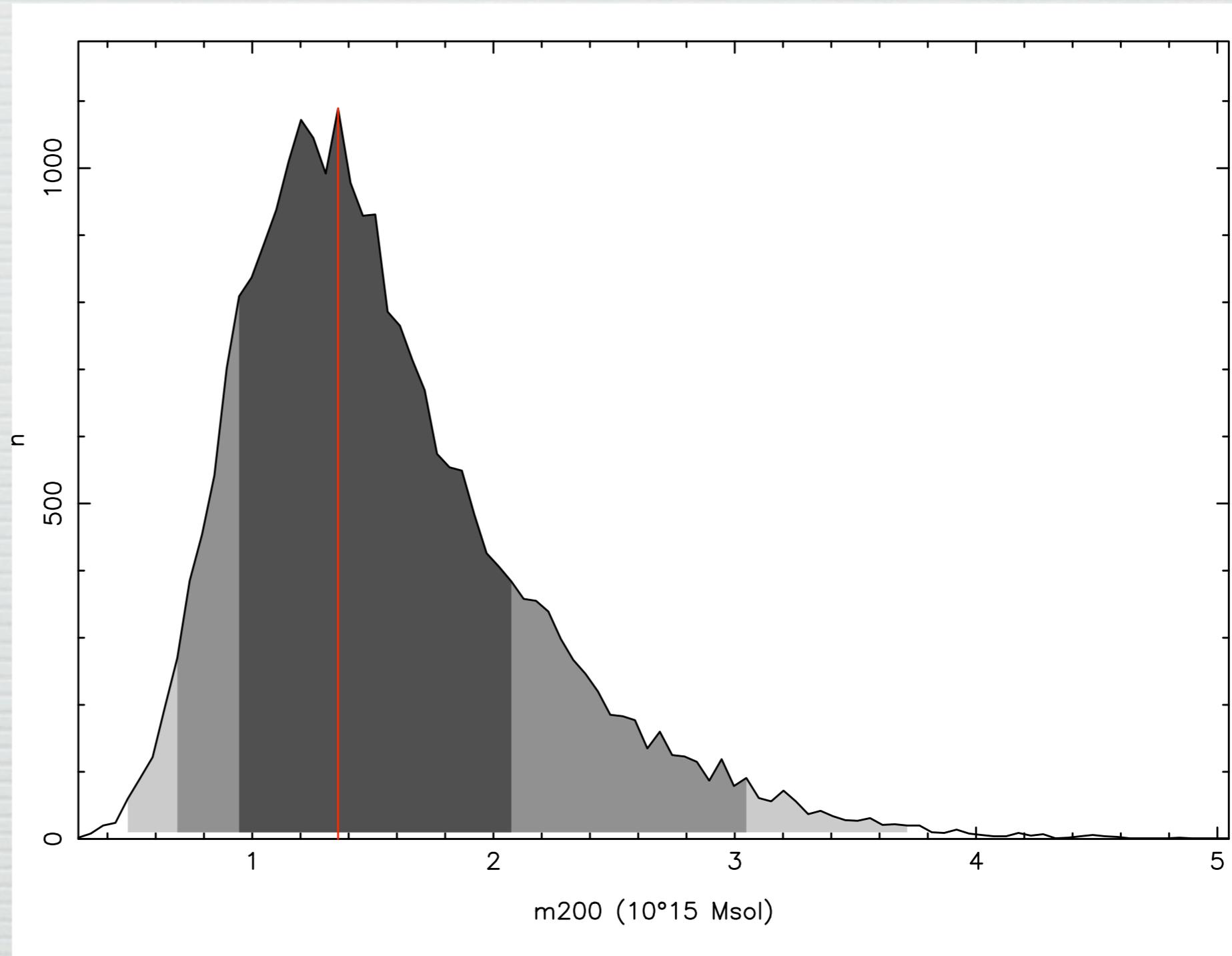
$\chi^2$  with  $\langle e_{\text{tan}} \rangle \sim g^{\text{obs}}$



best fit parameters



analytical mass profil



MACSJ1206.2-0848

+  $g_{\text{obs}}$  gauss.  $\longrightarrow$  best fit for severals MC g-profiles  $\longrightarrow$  best fit param. distrib.

# MASS ESTIMATION

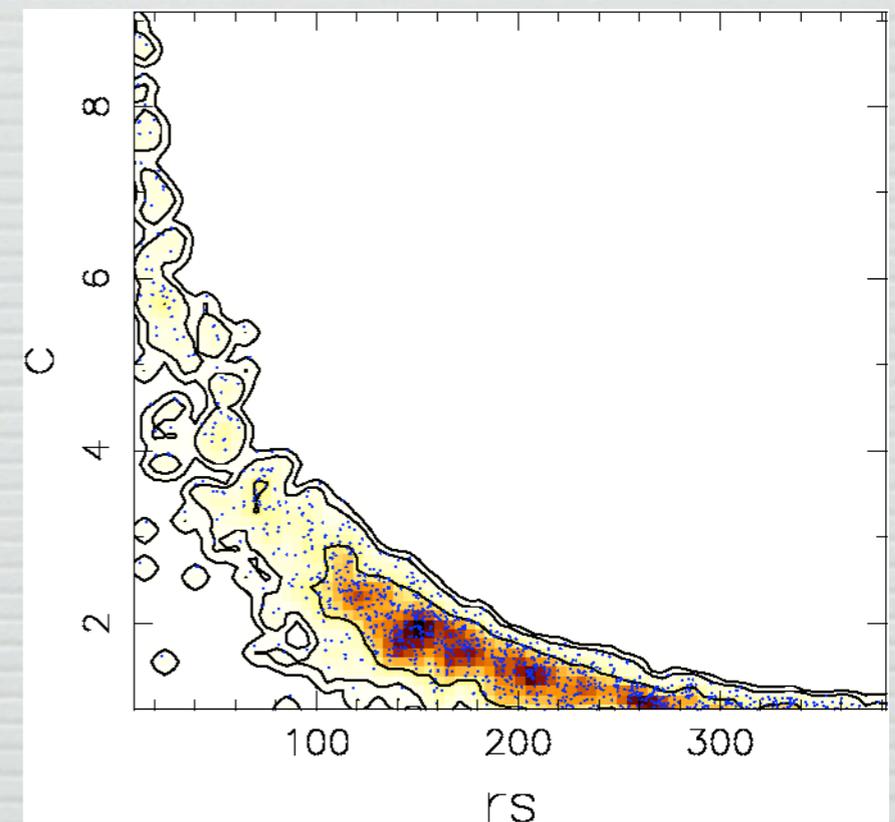
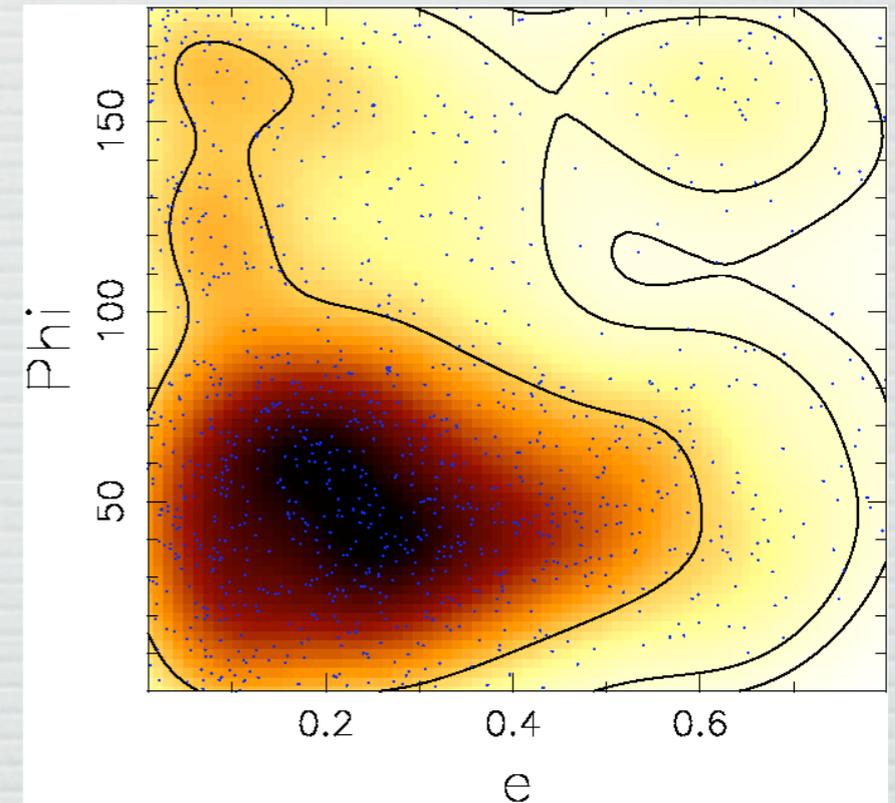
2D analysis

model fitting with **Lenstool**

(J.P. Kneib/E. Jullo)

- 'unlens' each galaxy :  $e^s = f(e^i, g^{\text{theo}})$
- use  $z_{\text{eff}}$  for each galaxy ( $\beta(z_{\text{eff}}) = \langle \beta(z) \rangle$ )
- fit the likelihood  $L = \prod (P_i(e^s))$  to  $N(0, \sigma \sim 0.3)$
- bayesian MCMC optimization

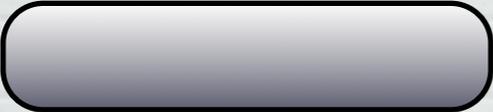
- + more complex models  $(x, y, e, \varphi)$
- + WL+SL (work in progress)



MACSJ1206.2-0848

# MASS ESTIMATION

2D analysis

 with   
(P. Marshall)

input model = grid of mass pixels  $\Sigma$

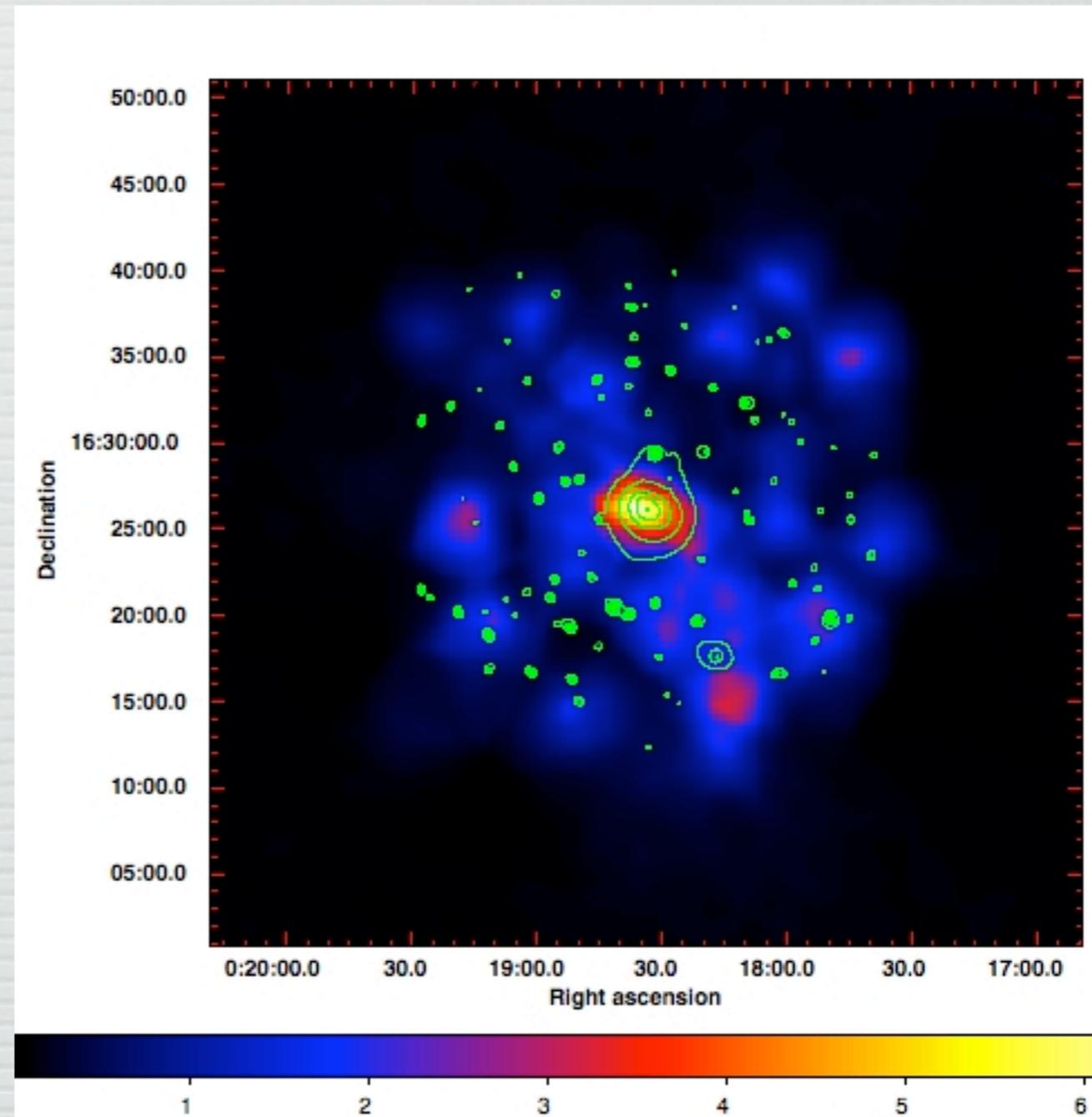
uses each galaxy shape component  $e_i$  as a reduced shear estimator



Likelihood :  $\Pr(\text{Data}|\Sigma) = \frac{1}{Z_L} \exp\left(-\frac{\chi^2}{2}\right)$

$$\text{with } \chi^2 = \sum_{i=1}^N \sum_{j=1}^2 \frac{(\epsilon_{j,i} - g_{j,i})^2}{\sigma^2}$$

ML with bayesian MCMC optimization  $\longrightarrow$  mass & SNR maps



CL0016

# MASS ESTIMATION

2D analysis

non parametric with **LensEnt2**  
(P. Marshall)

input model = grid of mass pixels  $\Sigma$

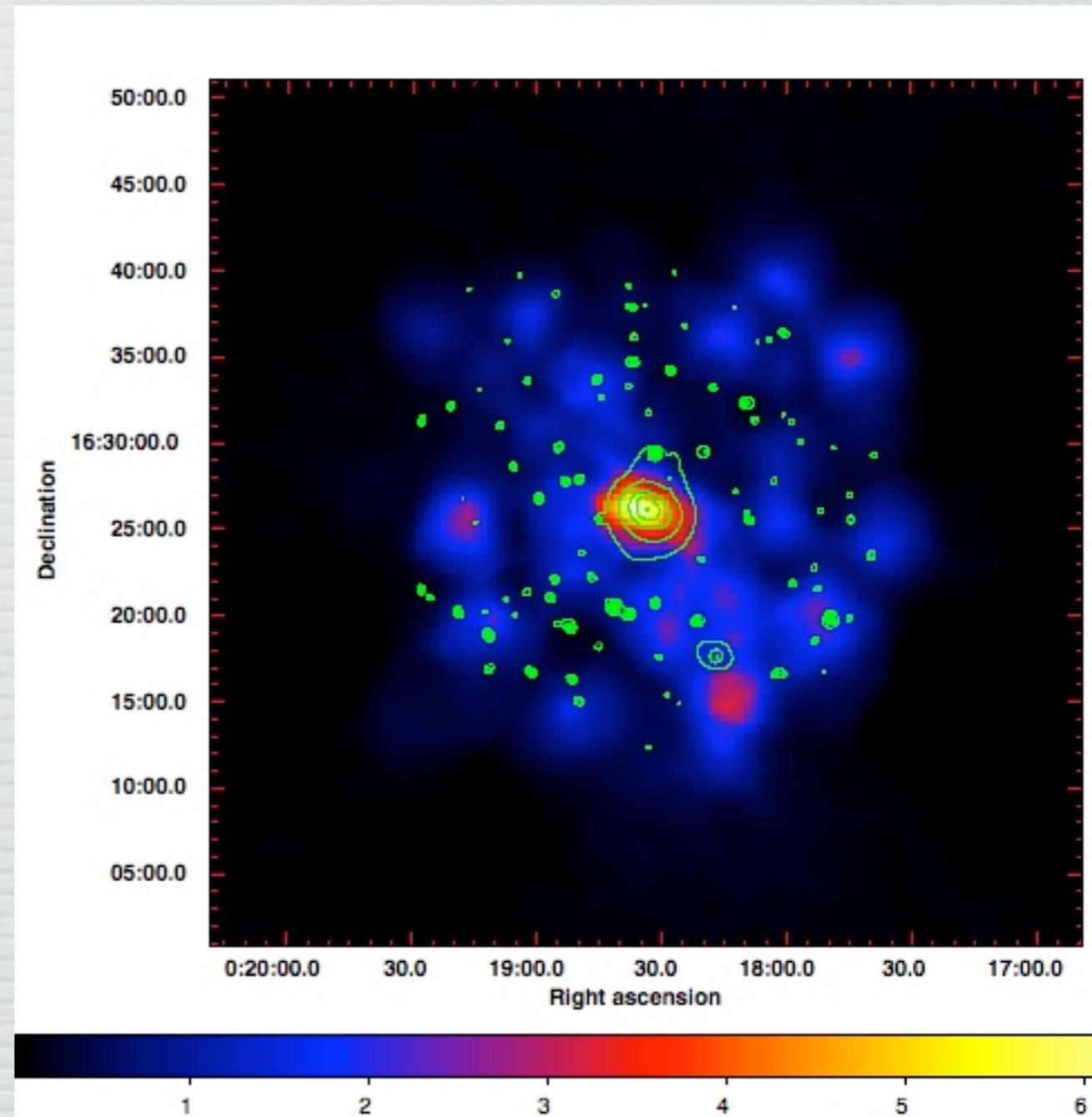
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ML with bayesian MCMC optimization  $\longrightarrow$  mass & SNR maps



CL0016

# ERROR ESTIMATION

List of uncertainties :

 shape measurements :

STEP simu : -10% bias

 contamination

 geometry



correction of  $g_{\text{obs}}$

!! based on simu. !!

- averaged over several different shear/PSF
- could change over the field/from a cluster to another

# ERROR ESTIMATION

List of uncertainties :

➔ shape measurements

➔ contamination

➔ geometry

cluster members removed  
(rs+zphot)

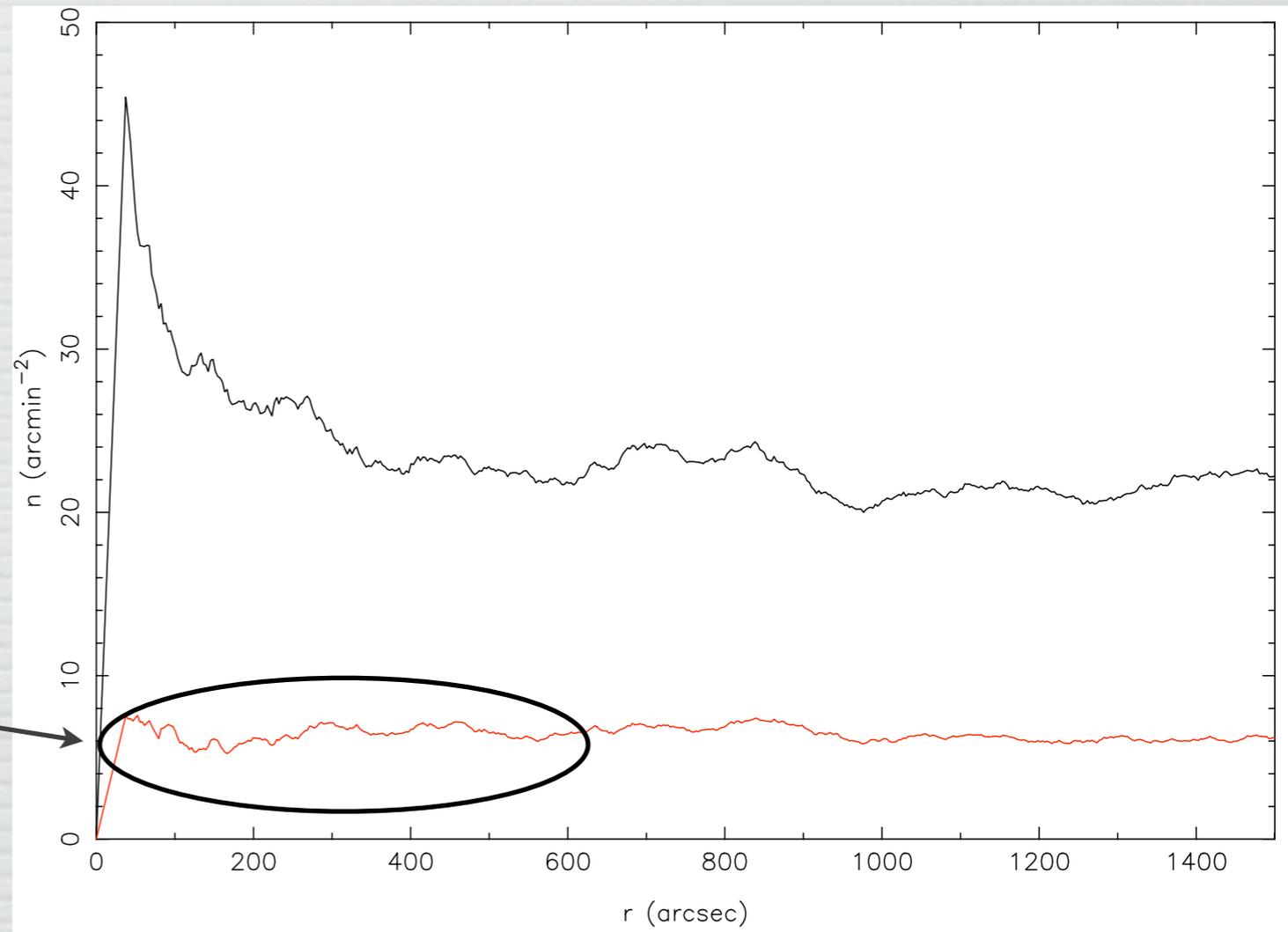
strong selection cuts

--> low bg density

% of fg gal. remaining ?

$$g \sim \frac{\sum_i^{N_{back}} e_{||}^i + \sum_j^{N_{fore}} e_{||}^j}{N_{back} + N_{fore}} \simeq \frac{N_{back}}{N_{back} + N_{fore}} g^{true}$$

underestimation of the shear  
= underestimation of the mass



RXJ2228.5+2036

requires a good sources catalogue !  
compromise between contamination and SNR

# ERROR ESTIMATION

List of uncertainties :

$$\beta(z_s) = D_{ls}/D_s$$

➔ shape measurements

➔ contamination

➔ geometry

-  $\langle \beta \rangle$  from CFHTLS good ??

- errors on z

- cosmic variance

- structures (e.g. clusters) in the field

WL :  $g \sim \beta \cdot \gamma^\infty$

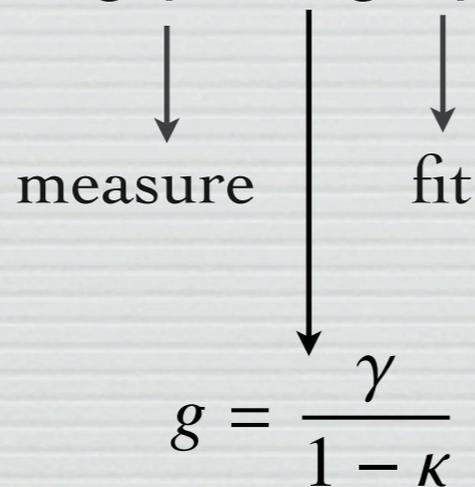
if :  $\beta = x \cdot \beta_{true}$

then :  $\gamma^\infty = \frac{\gamma_{true}^\infty}{x}$



x % overestimation on  $\beta$   
 ~ x% underestimation on the mass

-  $\langle g(\beta) \rangle \neq g(\langle \beta \rangle)$



negligible for  $r > 100''$  @  $z \sim 0.5$



don't use the galaxies in the central part

# ERROR ESTIMATION

List of uncertainties :

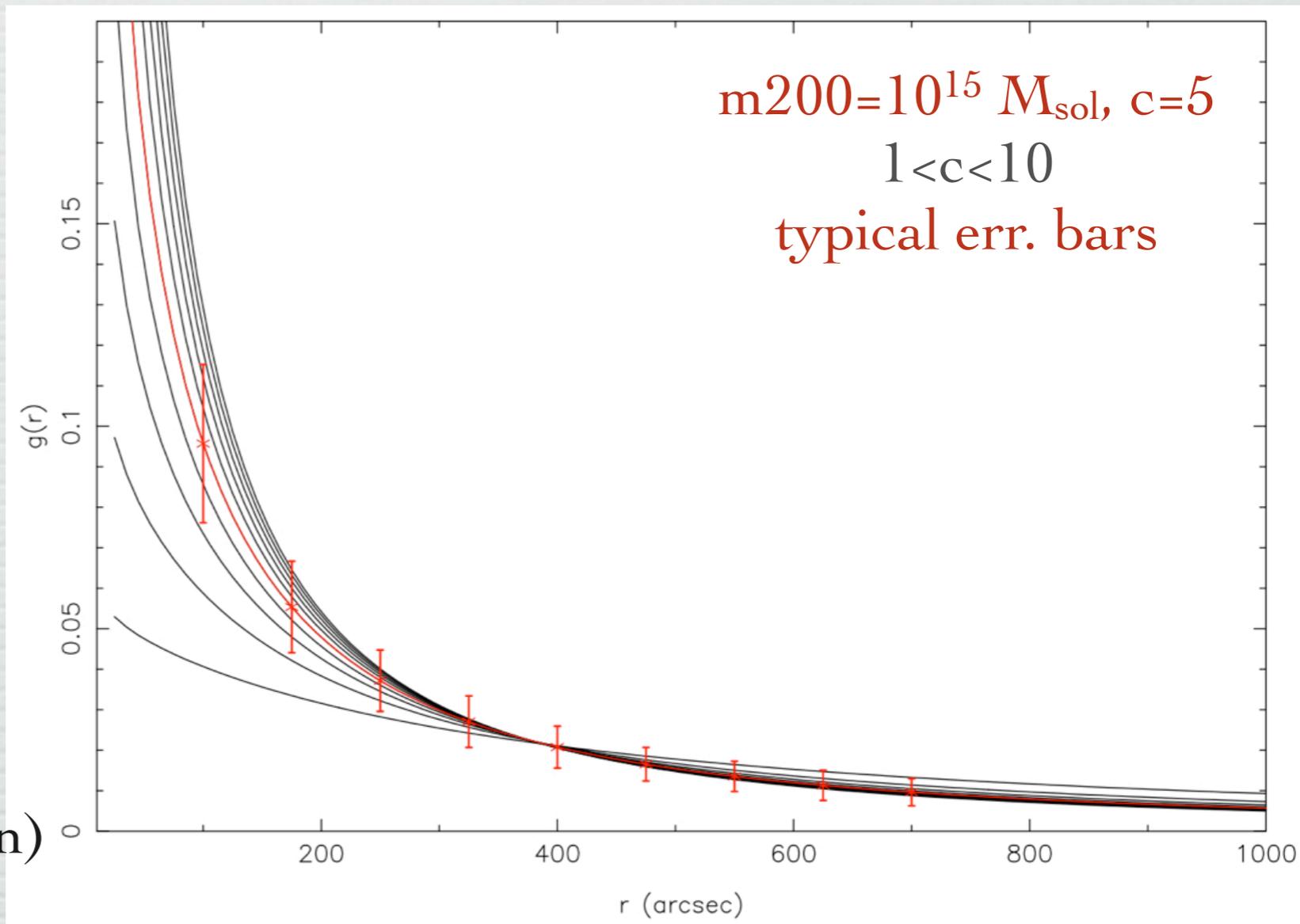
➔ shape measurements

➔ contamination

➔ geometry

hard to derive reliable error bars

increasing err. towards the center  
(SL effects, low number of gal./bin)



➔ no reliable info. on  $c$

Need other data (SL, X) to constrain the center and decrease error bars

# ERROR ESTIMATION

List of uncertainties :

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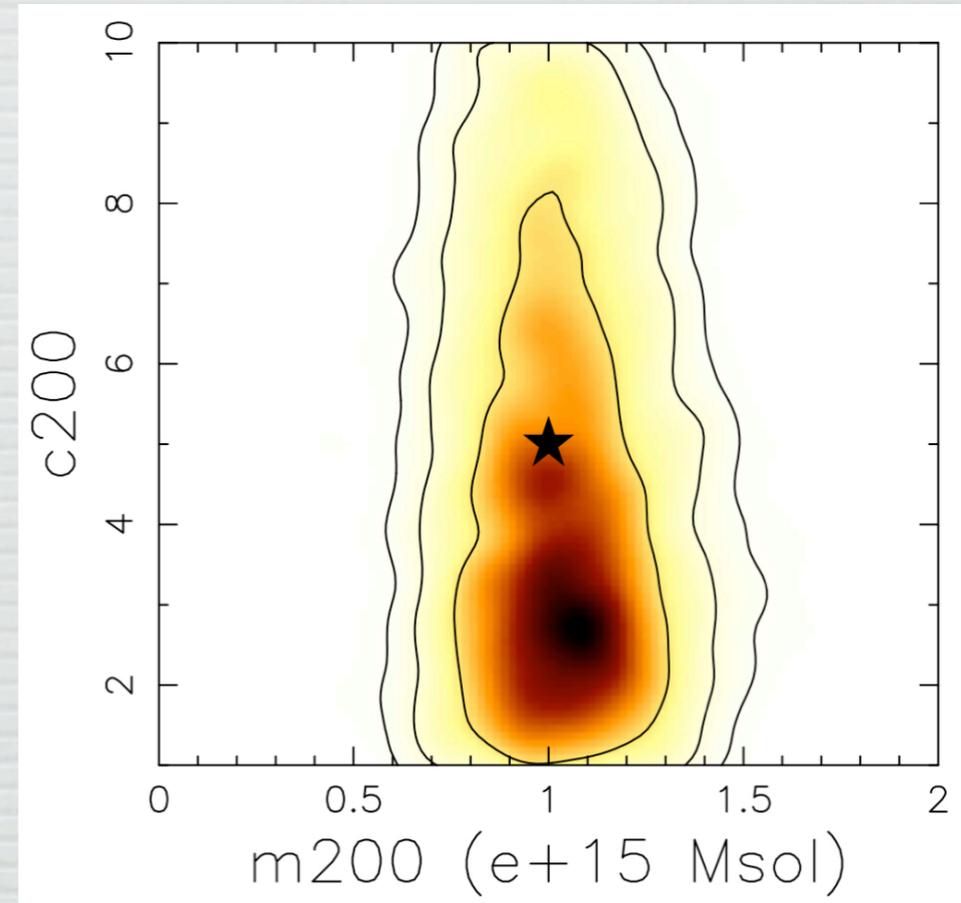
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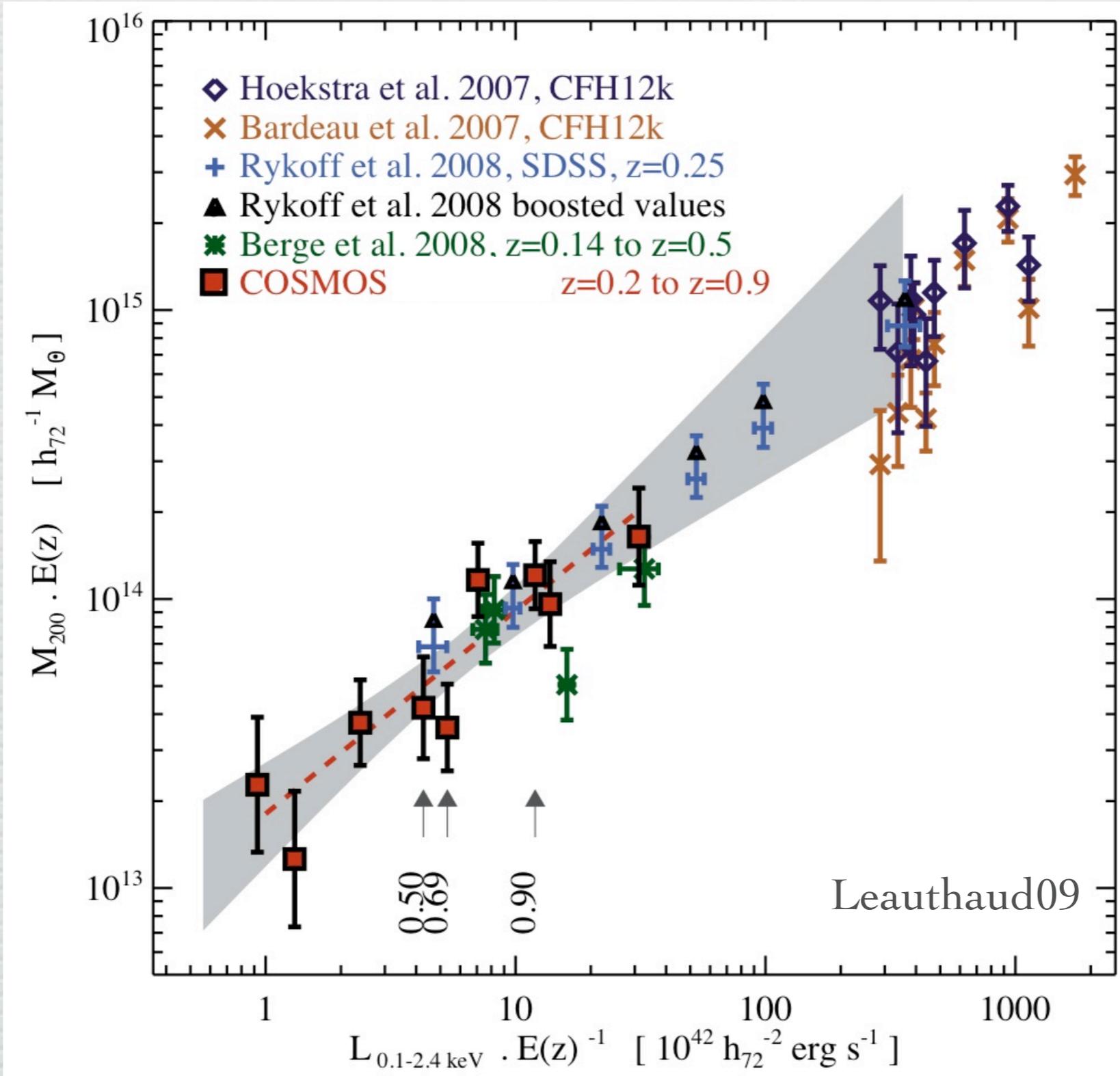
simulation  
( $z=0.5$ ,  $\rho_b=10 \text{ arcmin}^{-2}$ ,  $\rho_f=0$ ,  $n_{\text{clust}}=0$ )



➔ no reliable info. on c

Need other data (SL, X) to constrain the center and decrease error bars

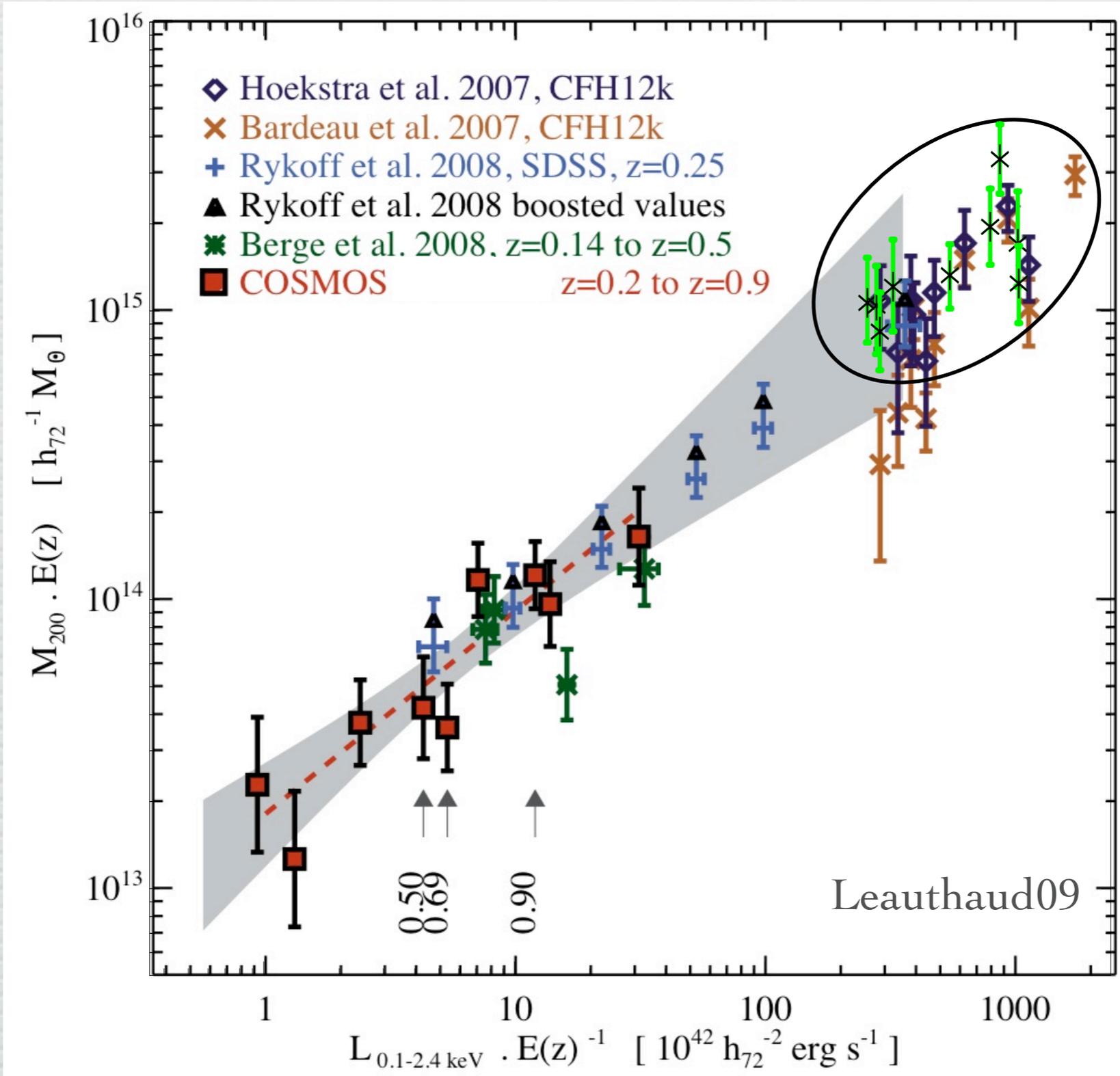
# SCALING RELATIONS



- M200 from shear profil  
- Lx Rosat

preliminary....

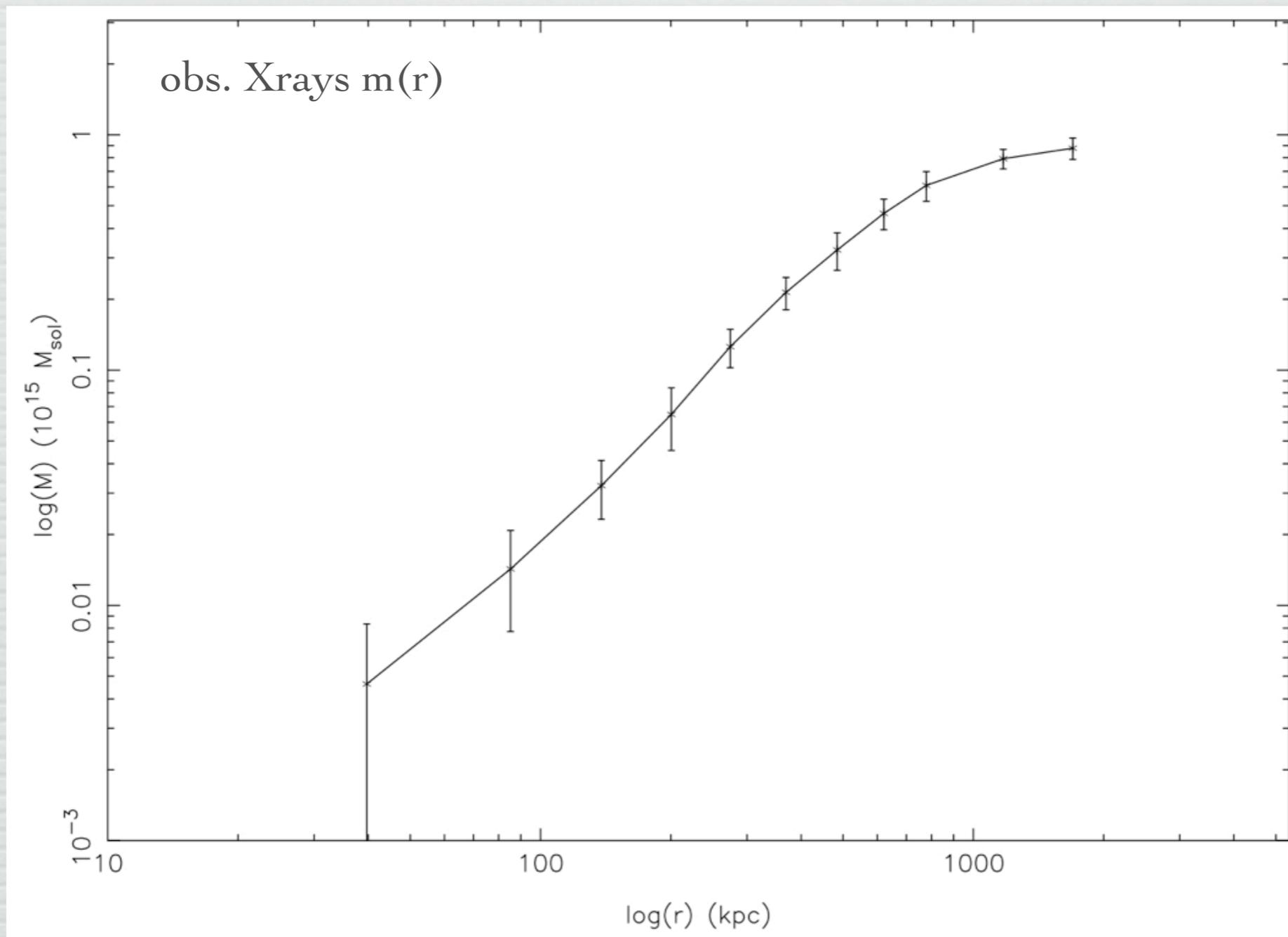
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preliminary....

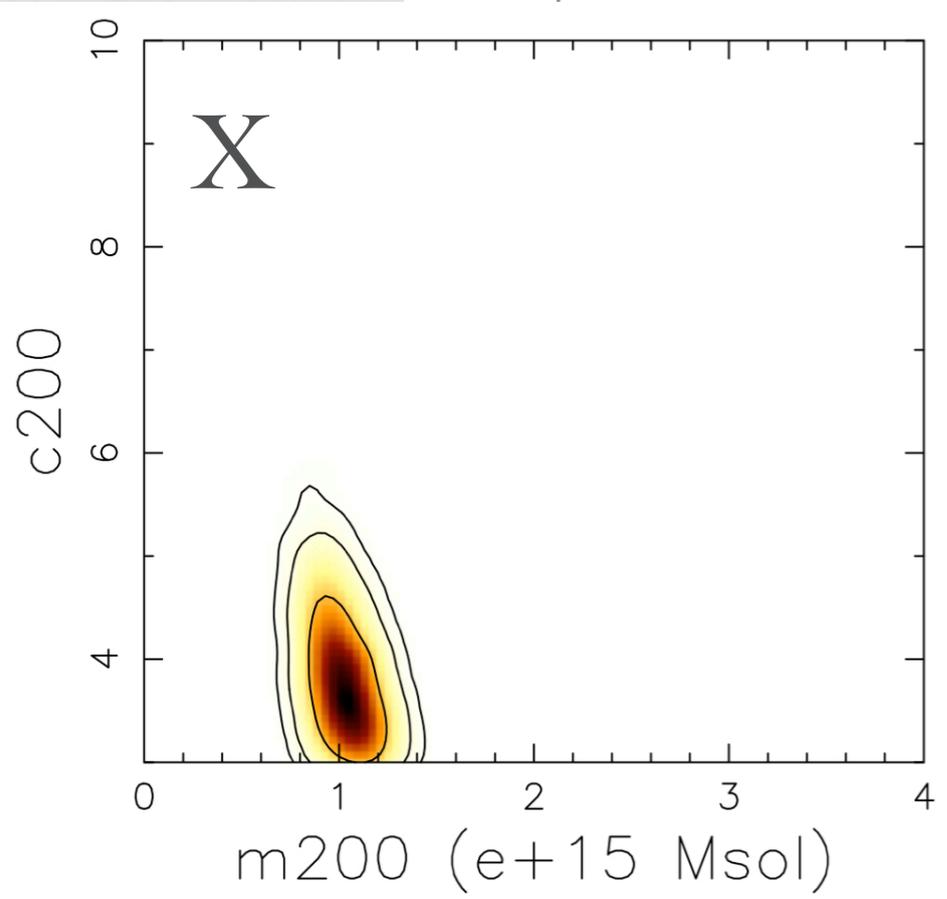
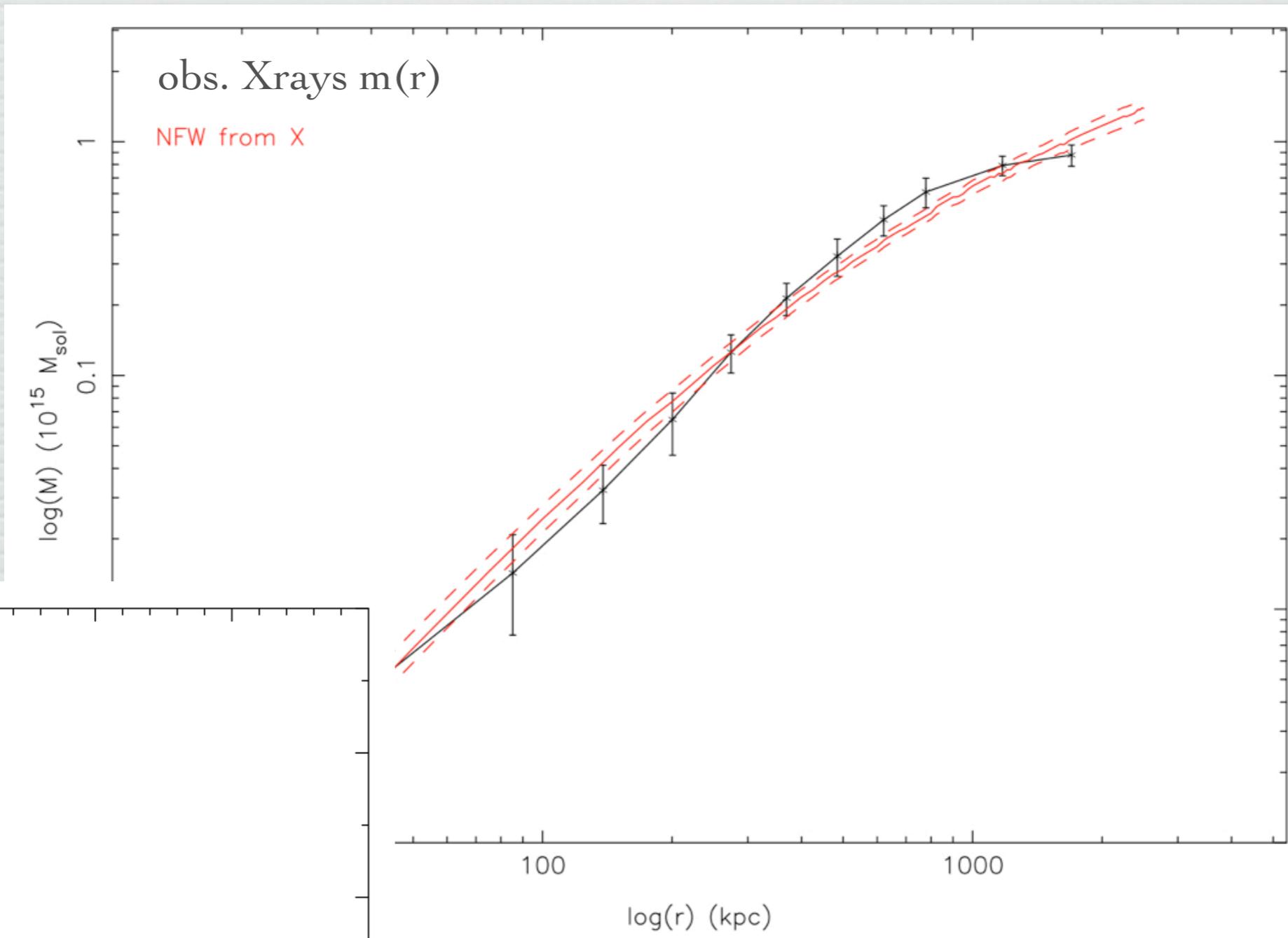
# COMPARE/COMBINE



CL0016

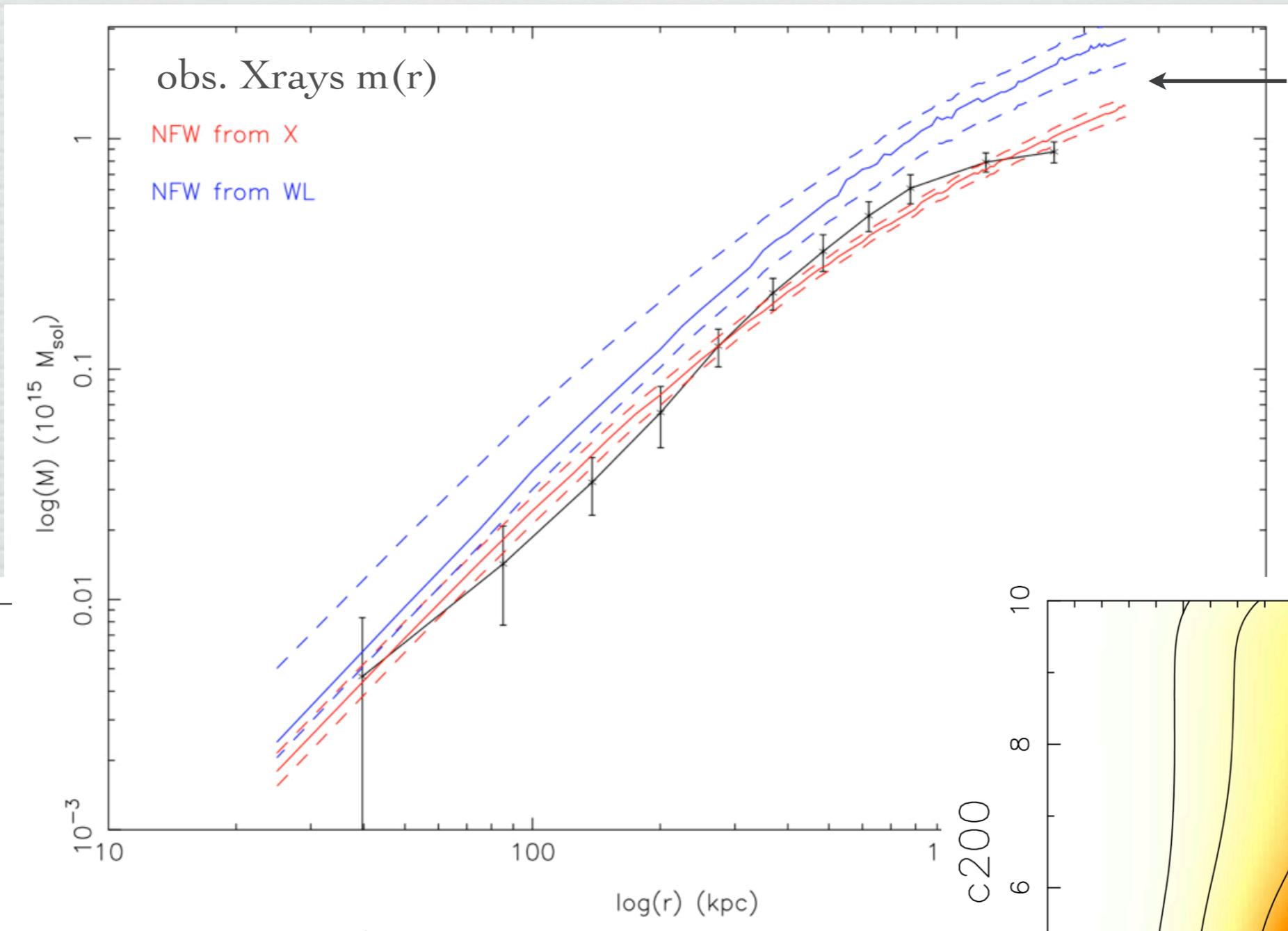
preliminary....

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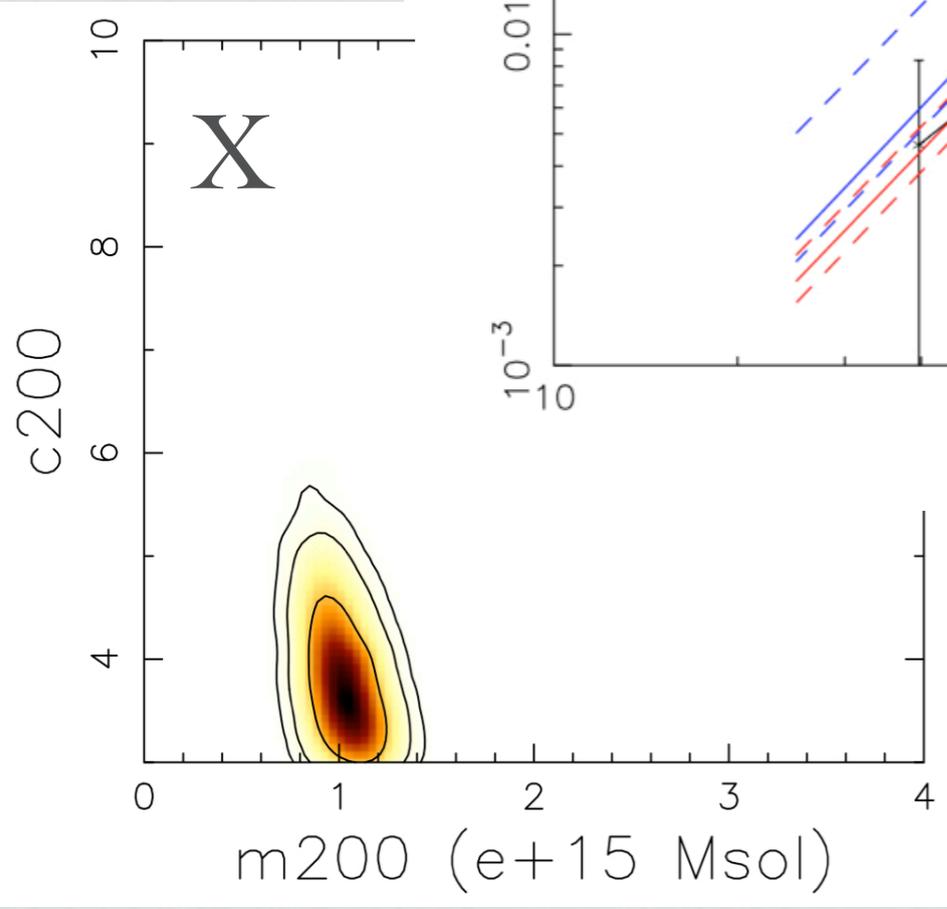


CL0016  
preliminary....

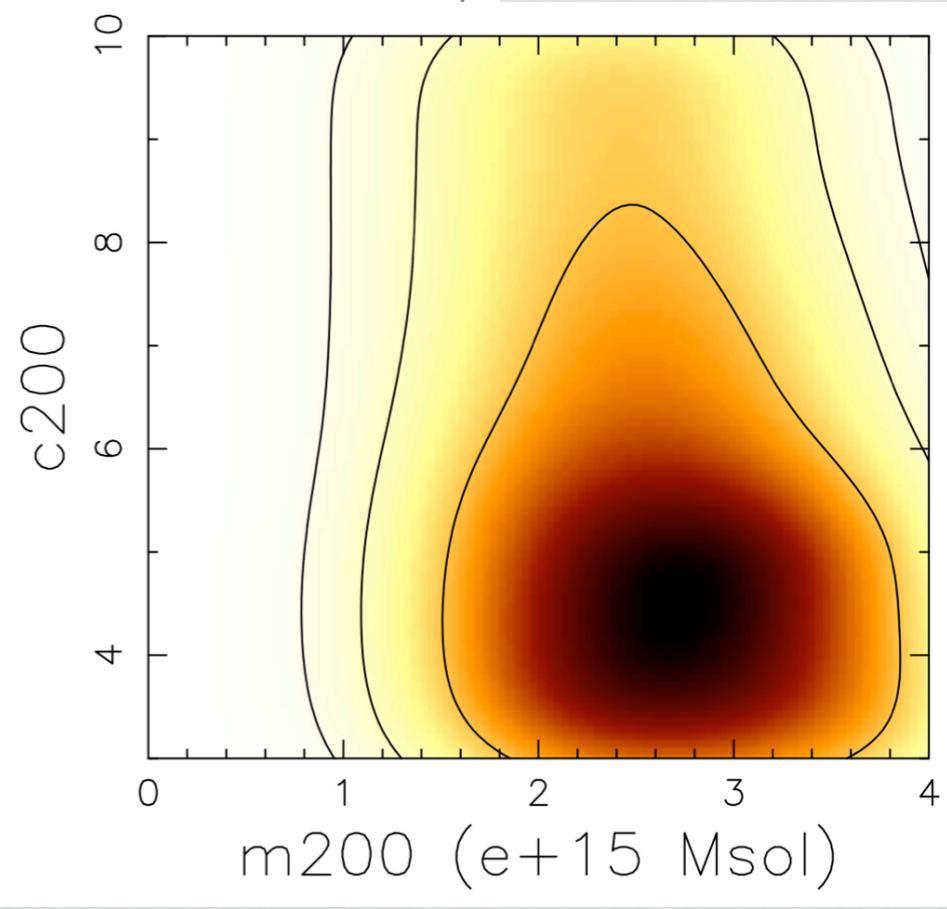
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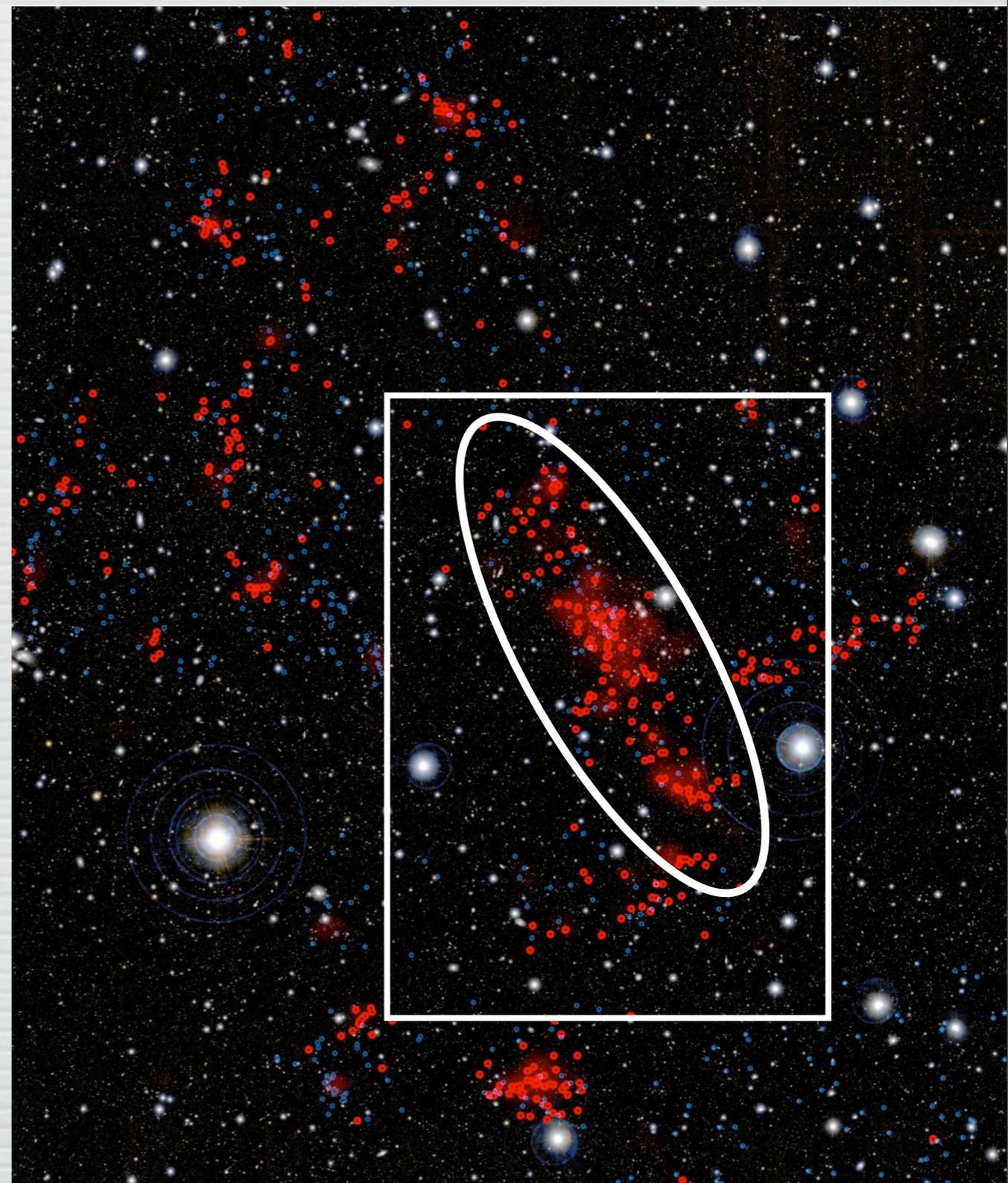
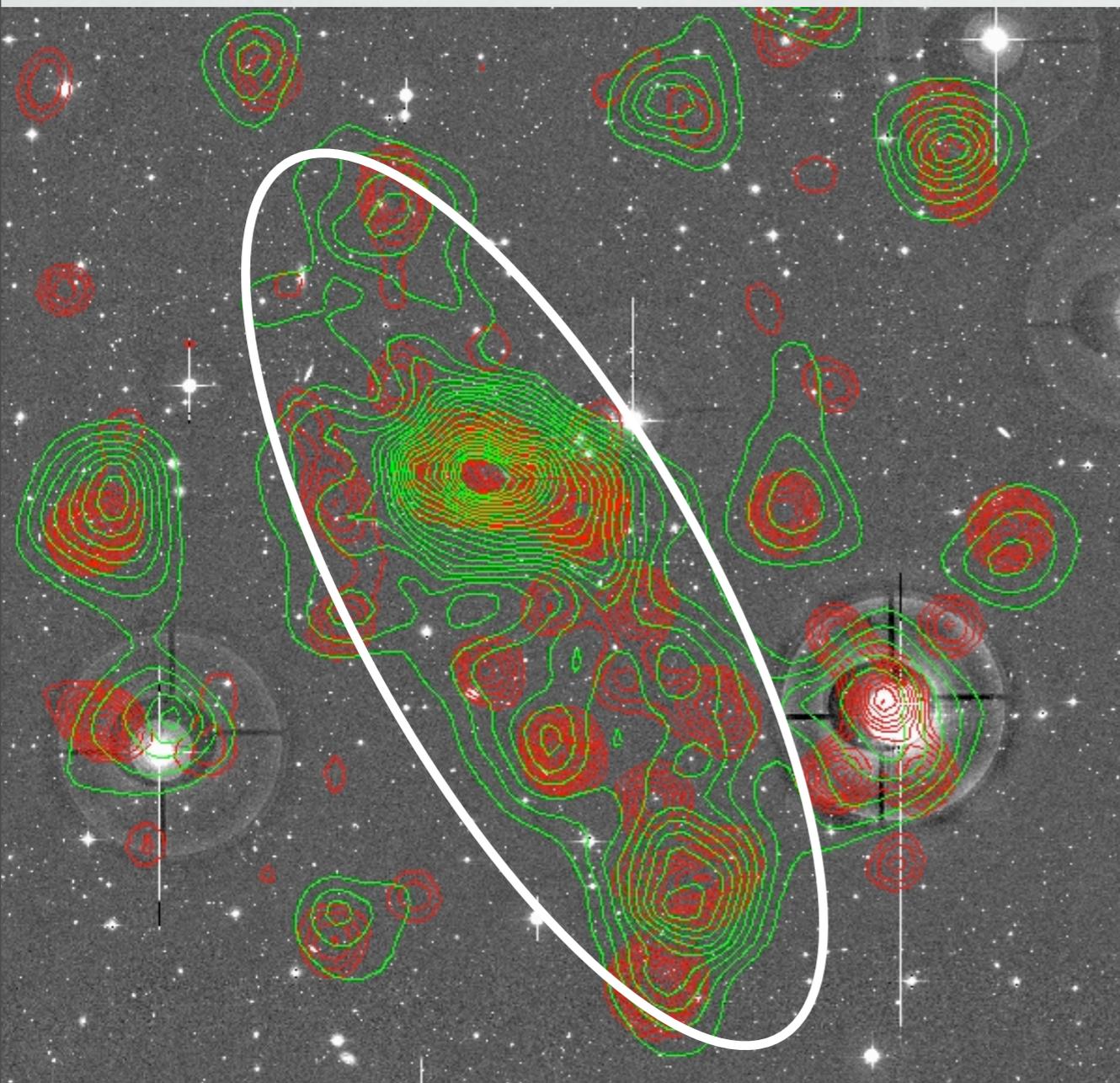
HE wrong ?  
large structure ?



CL0016  
preliminary....



# CL0016 ( $z=0.54$ )



preliminary....

Tanaka09

# CONCLUSION/PERSPECTIVES

- + weak lensing analysis of 11 clusters
- + efficient to constrain the mass at large scales

high  $z$  :

- contamination by foreground galaxies (= large fraction at these  $z$ )
- low density of background galaxies
- need other data (X, SL) to explore the clusters center
- hard to estimate truthfull error bars

→ weak lensing @ high  $z$  is challenging and requires very good data (space based)

Next steps :

combine the data sets and optimize the mass/concentration estimation

explore mass properties, scaling laws

put constraints on evolution (comparison with REXCESS sample)