

A Kinematical Detection of Two Unseen Jupiter Mass Embedded Protoplanets

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1 **Planets form deep within the midplane of protoplanetary disks consisting of circumstellar**
2 **material that orbits a young star. Substructure in the disk, such as spirals and rings, ap-**
3 **pears ubiquitous in the thermal emission arising from mm-sized solid particles. This has**
4 **been argued to indicate the presence of hidden planets¹⁻⁴. Relating substructure in thermal**
5 **emission to potential planet masses and locations is highly uncertain due to ill-constrained**
6 **gas-to-dust ratios and optical properties for the dust. Interpretation is further hampered by**
7 **grain evolution and gas dynamical effects which result in similar substructure without the**
8 **need for the presence of a planet⁵⁻⁹. Here we report the first kinematical evidence of two**
9 **embedded Jupiter-mass planets in the disk around the young star HD 163296 at 100 au and**

10 **165 au. By detecting small changes in rotation velocity of the gas arising from local gas pres-**
11 **sure gradient changes, we are able to constrain the embedded planet mass and location to an**
12 **exceptional precision of $\sim 50\%$ and $\sim 10\%$, respectively. This method opens up a new avenue**
13 **for the exploration of planetary systems into the formative stages.**

14 To date over 3700 planets have been detected¹⁰ with the first detections obtained by utilizing
15 the gravitational influence of the planet on the star inducing velocity shifts via the Doppler effect.
16 Planet detection during the formative stages is more challenging. There are a handful of claimed
17 detections via direct imaging¹¹⁻¹⁴, but the vast majority of planets remain hidden; their presence in-
18 ferred from visual evidence of gaps and rings seen in the thermal continuum emission of dust^{1,3,15}.
19 Subsequent determination of the properties of the planet is limited by the fact that estimates of
20 the gas density from the dust is fraught with uncertainties¹⁶. Ill-constrained gas-to-dust ratios and
21 complex grain evolution folded into commonly used analytical formulae relating dust gap width
22 and depth to planet mass culminate in errors of the planet mass of up to 200%¹⁷⁻¹⁹. Furthermore,
23 it has been shown that a gap does not directly infer the presence of a planet. Massive planets are
24 able to excite spiral waves which open up secondary and tertiary gaps⁹, while grain growth around
25 ice-lines and the shepherding of dust by (magneto-)hydrodynamical instabilities have also been
26 shown to produce ring-like structures⁵⁻⁸. In all, while hidden planets are the preferred interpreta-
27 tion of structure seen in dust emission maps, current methods do not robustly distinguish between
28 scenarios nor provide reliable constraints for embedded planet masses.

29 We use archival Atacama Large Millimetre Array (ALMA) data of HD 163296 which shows

30 ring structure in the mm continuum which have been used to infer the presence of at least two
31 planets at 100 and 165 au³. We use the CO isotopologue emission to detected deviations from
32 Keplerian rotation across these continuum features. Such deviations are consistent with changes
33 in the local pressure gradient expected from significant perturbations in the surface density of the
34 disk²⁰. Comparison with hydrodynamical simulations show that a 1 M_{Jup} planet at 100 au and
35 a 1.3 M_{Jup} planet at 165 au are driving the two outer perturbations, while the inner perturbation
36 is either a smaller mass 0.6 M_{Jup} planet at ~ 65 au, or the outer edge of the magneto-rotational
37 instability (MRI) deadzone. At such large distances from the star these planets result in a minimal
38 effect on the stellar velocity, however deviations in the local gas velocity structure betray their
39 presence.

40 With the high sensitivity and fine velocity resolution (50 m s^{-1}) afforded by ALMA we are
41 able to constrain the centroid of emission to an precision of 8 m s^{-1} , or 0.3% of the projected
42 Keplerian rotation velocity at 150 au, and thus derive an exceptionally precise rotation curve (see
43 the Methods section for the calibration of this precision). Comparison of this rotation curve with
44 a Keplerian profile assuming a stellar mass of $2.3 M_{\text{sun}}$ and a disk inclination of $i = 47.7^\circ$ shows
45 significant (up to 6σ) residuals as shown in Figure 1.

46 Despite the velocity signatures, no clear substructure is observed in the radial profile of the
47 integrated C^{18}O emission shown in panel (a), suggesting no significant changes in optical depth
48 of the emission. However, the emission surface of C^{18}O dips at the locations of the dark rings
49 observed in the continuum emission, the causes of which are discussed in the Methods section.

50 The rotation curve in panel (c) is well matched by a Keplerian profile, however the residual, shown
 51 in panel (d), clearly exhibits significant deviations. Comparable perturbations are observed in ^{12}CO
 52 and ^{13}CO emission and are discussed in the Methods section. The substantial deviation in the inner
 53 disk ($r < 70$ au) is likely due to the spatial resolution of the data (≈ 31 au), while the locations and
 54 amplitudes of the outer features are consistent with predictions for planet driven perturbations²⁰.

55 Particles which have grown large enough to decouple from the gas will rotate with a Keple-
 56 rian velocity, $v_{\text{Kep}} = \sqrt{GM_{\star}/r}$. On the other hand, gas, as traced with molecular line emission,
 57 is in both radial and vertical hydrostatic equilibrium. As such, the radial pressure gradient supports
 58 the gas against the gravitational pull of the central star, slowing the rotation^{21,22}. For a geometri-
 59 cally thick disk, the rotation velocity v_{rot} at a given point within the disk is given by,

$$\frac{v_{\text{rot}}^2}{r} = \frac{GM_{\star}}{(r^2 + z^2)^{3/2}} + \frac{1}{\rho_{\text{gas}}} \frac{\partial P}{\partial r} \quad (1)$$

60 where M_{\star} is the mass of the star and $\partial P / \partial r$ is the radial pressure gradient. In this we have
 61 not included the gravitational component of the disk as this will only introduce a linear trend and
 62 modelling it would require a well constrained gas mass for the disk²¹. Over small scales changes
 63 in v_{rot} will therefore be due to changes in the emission height, z , or changes in the local pressure
 64 gradient.

65 Local changes in the emission height as the sole reason can be ruled out as comparable
 66 perturbations are seen in all three isotopologes, despite a change in height only observed for C^{18}O .

67 Rather the deviations are likely due to changes in the local pressure gradient, such as from a gap
68 carved by an embedded protoplanet¹⁹. This scenario gives rise to a distinct perturbation from a
69 smooth rotation curve: rotation is slowed on the inner side of the perturbation, and hastened on the
70 outer side as shown in Figure 2c. Residuals in the rotation profile agree with this scenario: gaps
71 in the continuum at 60, 100 and 160 au are bounded by a local minimum inwards of the gap and a
72 local maximum outside the gap (although the local minima inwards of 60 au is not observed due
73 to the spatial resolution of the data).

74 To test this hypothesis, we ran hydrodynamical models of embedded protoplanets guided by
75 the best-fit values inferred from the continuum rings³. We limit ourselves to comparisons with
76 the C¹⁸O emission as this is originating from the densest region of the disk and least likely to be
77 affected by the poorly constrained physical structure of the upper disk. We find excellent agreement
78 with the two outer gaps with planets at 100 au and 165 au with masses of 1 M_{Jup} and 1.3 M_{Jup} ,
79 respectively, as shown in Figure 2. Altering the mass and radial position of these two planets we
80 are able to constrain the planet masses to 50% and their radial location to 10% given the current
81 uncertainties on δv_{rot} .

82 Determining the source of the inner-most perturbation is more complex. As noted in previous
83 studies³, the continuum ring is too wide to be well described by a single embedded planet. From
84 our hydrodynamic simulations we are unable to find as a convincing fit as the outer planets, but the
85 inner feature is qualitatively well described by a 0.6 M_{Jup} planet at 65 au. An alternative scenario
86 proposed for the inner gap in continuum emission is the pressure confinement of grains at 80 au

87 due to the edge of the deadzone of the magneto-rotational instability (MRI)^{6,23}. Such pressure
88 confinement would require a pressure maximum at the centre of the bright ring leading to a local
89 maximum in δv_{rot} inwards of that location, consistent with the observations.

90 The observed rotation curve, and thus the inferred pressure gradient, requires the disk to pos-
91 sess a surface density structure comparable to that in Figure 3a. Other hydrodynamical instabilities
92 have been shown to result in surface density perturbations, such as the MRI, zonal flows, the ver-
93 tical shear instability^{24–27}. Tight constraints on the turbulence in the disk^{28,29} limit the strength of
94 these instabilities, resulting in long viscous time scales, considerably older than the age of the disk.
95 Furthermore, many of these instabilities are transient, however to be applicable for HD 163296
96 must be sufficiently long lived enough to drive the continuum substructure we observe. Until there
97 are firm predictions for the rotational profiles expected from these instabilities, embedded planets
98 remain the favoured scenario, naturally recovering all observations.

99 With these observations we have presented the first kinematical evidence of embedded pro-
100 toplanets in a protoplanetary disk. In Figure 4 we compare these planets to the current state of
101 existing planet detections. Our planets are younger (estimated age of $\lesssim 5$ Myr³⁰) and open a new
102 area of parameter space, hinting at the presence of a population of distant Jupiter mass planets.
103 This method provides the first opportunity to inventory the systems which harbour on-going planet
104 formation. In the future the presence of these planets, which retain heat at formation, may be
105 confirmed by sensitive mid-infrared facilities such as the James Webb Space Telescope. Just as
106 important, we have only begun to grasp the potential of ALMA for planet detection and the use of

107 Doppler planet detection into a new realm.

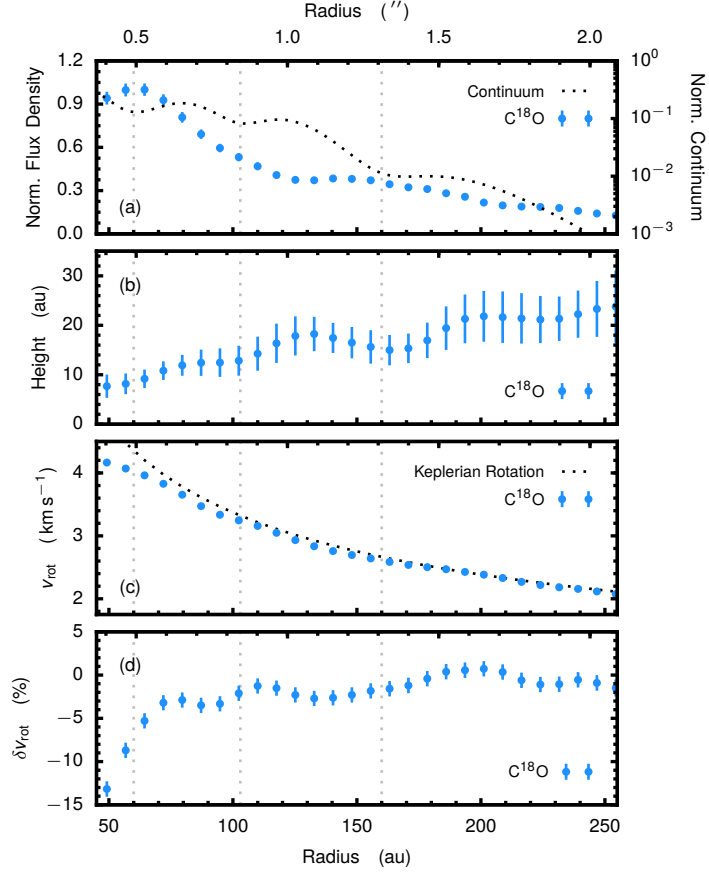


Figure 1: **C¹⁸O observations of HD 163296.** Panel (a) shows the normalised radial profile of the C¹⁸O flux density and the logarithm of the continuum density model³ as the dotted curve. The derived emission surface and rotation velocity, v_{rot} , are shown in panels (b) and (c), respectively. The relative deviation, δv_{rot} , from the reference Keplerian rotation curve shown by the dotted line, is displayed in the bottom panel. All panels show Gaussian Process models of the data with associated 3σ error-bars. The dotted vertical lines show the location of the dark rings in the continuum emission³.

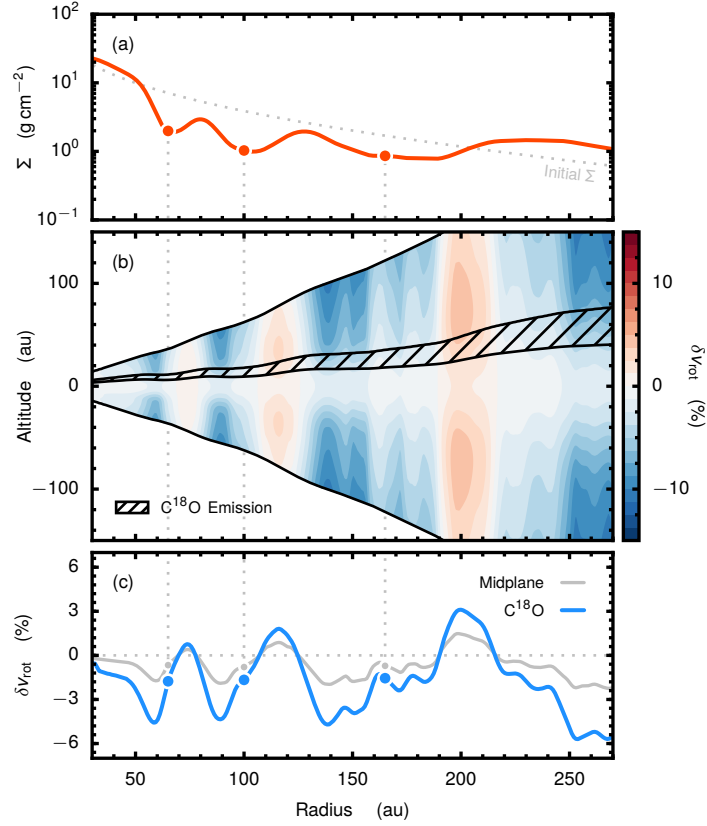


Figure 2: **Best-fit disk physical structure.** The azimuthally averaged surface density from the best-fit hydrodynamical model is shown in panel (a). The velocity structure was calculated from Equation 1 shown in panel (b). The region where C¹⁸O arises is shown by hatching. Radial profiles of δv_{rot} from the midplane and the C¹⁸O emission region are shown in panel (c) by the gray and blue lines respectively.

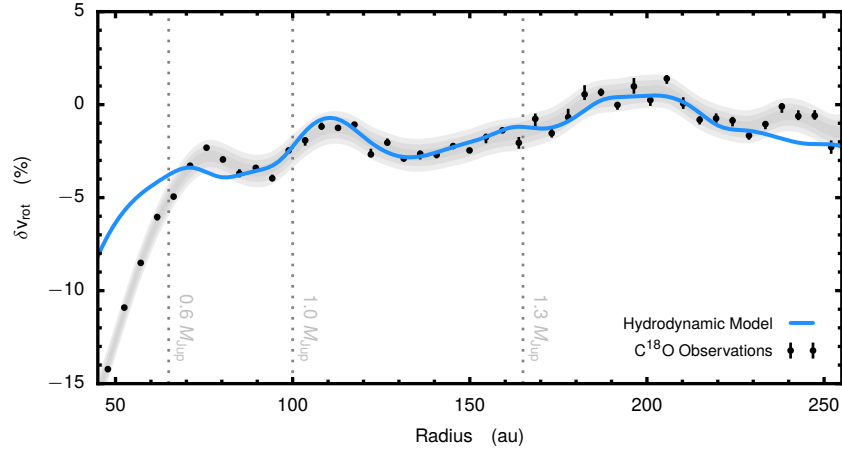


Figure 3: **Comparison of the best-fit model with observations.** Results from individual annuli are shown by black points with the Gaussian Process model with 3σ uncertainties shown by the gray band. The best fit model with 0.6, 1.0 and 1.3 M_{Jup} planets at 65, 100 and 165 au is shown by the blue line.

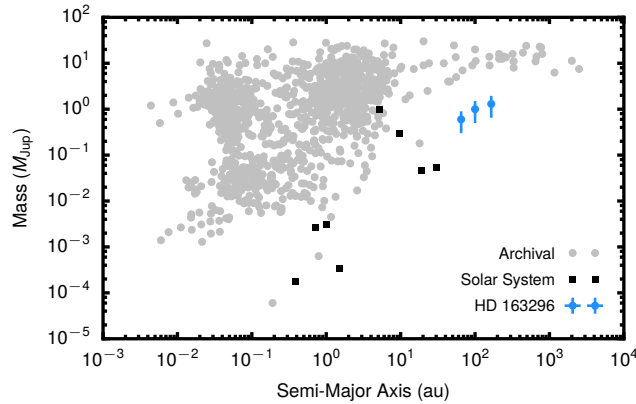


Figure 4: **Comparison with known planets.** Planets detected in HD 163296 shown in blue are probing a new regime in the planetary mass-orbit relation as shown by the confirmed planets in gray points taken from the NASA Exoplanet Archive¹⁰. Black squares mark the planets in the Solar System.

108 **Methods**

109 **ALMA Observations** This project used the archival data 2013.1.00601.S (PI: A. Isella³) which
110 targeted ^{12}CO , ^{13}CO and C^{18}O emission at $\approx 0.25''$ spatial resolution and 15 kHz spectral resolu-
111 tion, equivalent to 20 m s^{-1} . The data were calibrated using the scripts provided with the data and
112 using the `CASA v4.0.0` pipeline. Using `CASA v5.1.1` and following the original work, the
113 data were self-calibrated using the 232 GHz continuum window, before the continuum subtrac-
114 tion using the `uvcontsub` task. Images were produced with a channel spacing of 50 m s^{-1} and
115 a Briggs robust parameter of 0.5 resulting in beam sizes $\approx 0.28'' \times 0.23''$. The images were then
116 rotated assuming a position angle of 132° to align the major axes with the x -axis.

117 **Emission Surfaces** As molecular line emission arises from an elevated region above the midplane^{31,32},
118 the observed emission is asymmetric^{21,33}. This asymmetry was used to derive the emission surface
119 profiles which was used to properly deproject the data into azimuthal bins of constant radius.

120 We follow the method presented in Pinte et al.²², producing multiple samples of the emission
121 surface z as a function of r . Instead of binning the data, we model the emission surface as a
122 Gaussian Process. This implicitly assumes that the underlying function is smooth and takes into
123 account both correlations in the data and in the noise. This model is implemented with `celerite`
124 ³⁴. Figure 5 displays the derived surfaces for the three lines and the associated 3σ uncertainties of
125 the GP model. We used both a simple harmonic oscillator kernel and a Matern 3/2 kernel, both
126 times including a Jitter term to account for the scatter, and found comparable results.

127 The resulting emission surfaces agree qualitatively well with previous modelling predictions.

128 The ^{12}CO surface is comparable to the upper CO molecular layer in Rosenfeld et al.²¹, while the
 129 C^{18}O emission is comparable to that in the model of Flaherty et al.²⁹. We note however that the
 130 observed ^{12}CO emission is somewhat higher than in the model which may suggest a limitation
 131 of the parametric structure used. C^{18}O data clearly shows dips at the locations of the two outer
 132 continuum gaps at 100 au and 170 au, in addition to a third further out at 230 au, coincident with
 133 the outer gap in DCO^+ reported in Flaherty et al.²⁹. The more optically thick lines of ^{12}CO and
 134 ^{13}CO show smoother, less perturbed surfaces.

135 For a vertical Gaussian profile for the density structure, a reasonable assumption for regions
 136 close to the midplane, the emission surface z_τ is given by,

$$z_\tau = \sqrt{2}H_{\text{gas}} \cdot \text{erfc}^{-1} \left(\frac{2(x_{\text{mol}} \cdot N_\tau + 1.3 \times 10^{21})}{\Sigma_{\text{gas}}} \right) \quad (2)$$

137 where N_τ is the observable column density of the emitting molecule required to reach an optical
 138 depth of τ , x_{mol} is the relative abundance of the emitting molecule with respect to H_2 , H_{gas} is the
 139 pressure scale height of the gas and erfc^{-1} is the inverse complimentary error function. Assuming
 140 $x_{\text{mol}} \cdot N_\tau$ remains constant across the gap locations, as suggested by the lack of features in Figure 1a,
 141 changes in the emission height must therefore require a drop in either, or a combination of, H_{gas} ,
 142 and thus the midplane temperature, or Σ_{gas} .

143 As the disk is believed to have negligible non-thermal line broadening^{28,29,35}, the line width
 144 will directly trace the gas temperature. No deviations from a smooth profile are observed for C^{18}O
 145 suggesting that the temperature traced across these gaps is relatively constant, as shown in Figure 7,

146 thus a smooth profile for H_{gas} would be expect. Therefore pressure gradients changes would have
147 to be predominantly driven by changes in Σ_{gas} .

148 **Rotation Profiles** Calculation of v_{rot} takes advantage of the azimuthal symmetry of the disk. No
149 significant azimuthal structure is observed for the HD 163296 disk in thermal continuum emisison,
150 molecular line emission or scattered light emission^{3,28,29,36,37}. For a given radius from the central
151 star, the line profile will share the same properties; only the line centre should be Doppler shifted
152 by the line-of-sight component of rotation. For an assumed v_{rot} , each pixel can be shifted back to
153 a common line centre and then the lines azimuthally stacked to improve the signal to noise³⁸⁻⁴⁰.

154 Rather than assuming a rotation profile *a priori* to make this deprojection, one can be in-
155 ferred. We assert that the correct rotation velocity is the one which results in the narrowest line
156 profile for the stacked profile. Any error in the assumed rotation velocity will result in a slight
157 offset in the line centres before stacking and thus lead to a broadening of the line. By deprojecting
158 the lines to a common centre, we also effectively sample the true line profile at a much higher
159 sampling rate than the correlator, allowing for a highly accurate calculation of the line width.

160 To derive v_{rot} , each image cube was split into annuli with a width of 9 au (roughly two
161 pixels), accounting for the derived emission surface. Although this is below the spatial resolution
162 of the data, wider bins result in sampling a range of v_{Kep} values which can hide any signal from
163 pressure gradients. As each annulus samples points from spatially uncorrelated pixels, the resulting
164 correlation is less severe. Testing this procedure with a forward model with known rotation profiles
165 demonstrated that no significant bias is introduced.

166 For each annulus, v_{rot} was calculated as the velocity profile which minimized the width of the
167 line profile from the stacked, deprojected lines. This minimization used the L-BFGS-B method
168 implemented in the `scipy.optimize` package. During this minimization, we also allowed the
169 relative position angle to vary to account for possible uncertainties in the position angle. A similar
170 approach has been used to model the Doppler shift due to binary stars.⁴¹ This approach was tested
171 on mock data and was shown to robustly recover the rotation profile.

172 Figure 6 demonstrates the procedure with mock data. Here lines are assumed to have
173 $\Delta V = 150 \text{ m s}^{-1}$ sampled at a 40 m s^{-1} resolution, comparable to the observations. Each line
174 is corrupted with white noise with a standard deviation of 10%, comparable to the data. An an-
175 nulus of constant radius is shown in the left panel containing 40 lines, evenly spaced in azimuth.
176 Shifting each spectrum by an amount $v_{\text{rot}} \cdot \cos(\theta)$ results in a single line profile as shown in the
177 centre panel resulting in sampling rate of roughly 2 m s^{-1} . A Gaussian profile is fit to the depro-
178 jected data, varying v_{rot} to minimize the line width. The line width as a function of v_{rot} is a convex
179 function centred at the intrinsic line width, as shown in the right panel. The dashed lines show the
180 recovered values for the mock data; both v_{rot} and ΔV were recovered to an accuracy of 2 m s^{-1} .

181 To calculate uncertainties for the derived v_{rot} profile, we used the deprojected spectra as
182 the model, then used the Monte-Carlo Markov Chain (MCMC) sampler implemented in `emcee`⁴²
183 to sample the posterior distributions of v_{rot} and the position angle. The posterior distributions
184 were uncorrelated and no significant deviation from zero for the position angle was found. 1σ
185 uncertainties, calculated as the 16th to 84th percentiles of the posterior distribution, were found to
186 agree with the simple minimization approach.

187 For the reference velocity profile we take a Keplerian profile assuming $i = 47.7^\circ$ around
188 a $2.3 M_{\text{sun}}$ star. Residuals are calculated as $\delta v_{\text{rot}} = 100 \times (v_{\text{rot}} - v_{\text{Kep}}) / v_{\text{Kep}}$. Changes in the
189 inclination or mass of the central star will result in a vertical offset for δv_{rot} so we are unable to
190 determine if any gas rotation is truly super-Keplerian. Relative values, which trace local changes
191 in the gas rotation, will remain unchanged.

192 The relative residual from v_{Kep} for the three lines is shown in Figure 8. The measurements are
193 shown by the points while the solid line shows a Gaussian Process model. All uncertainties are 3σ .
194 Each annulus is able to constrain v_{rot} to $\approx 2 \text{ m s}^{-1}$, however the Gaussian Process model, which
195 takes into account the entire radial profile and tries to find a smooth model to the observations,
196 has uncertainties of $\approx 8 \text{ m s}^{-1}$. All three lines show broadly comparable features, however C^{18}O
197 exhibits the most clear perturbations. Differences between lines suggest a change in the pressure
198 profile as a function of height as well as radius.

199 The significant difference between the ^{12}CO and the more comparable ^{13}CO and C^{18}O lines
200 is likely due to the ^{12}CO emission tracing a much higher region in the disk as shown in Fig. 5. This
201 demonstrates that we are able to trace perturbations in the disk physical structure in both radial and
202 vertical directions. As full 3D models with fully-consistent temperature and density structures are
203 beyond the scope of this paper, we limit ourselves to the comparison with the C^{18}O emission which
204 traces the region closest to the midplane and thus the region where simple parametric models are
205 most applicable.

206 As deviations are observed in all three isotopologues, yet only significant changes in emis-

207 sion height observed in C¹⁸O, we can rule out solely changes in the emission height as the cause
 208 for the observed deviations. We therefore consider the scenario where the pressure gradient is
 209 significantly perturbed by the presence of a planet opened gap.

210 **Hydrodynamic Models** We carry out hydrodynamic simulations to estimate the masses and radial
 211 locations of planets responsible for the observed gas pressure gradient changes in the HD 163296
 212 disk. We solve the hydrodynamic equations for mass and momentum conservation in the two-
 213 dimensional polar coordinates (r, θ) using FARGO 3D⁴³. The orbital advection algorithm FARGO
 214 ⁴⁴ is used in the calculations. We use 1024 logarithmic radial grid cells between 16 and 480 au,
 215 and 1920 uniform azimuthal grid cells covering full 2π radians.

216 The disk model is based on a parametric model^{28,29} which has found a good fit to CO iso-
 217 tope emission. The initial density profile is described by,

$$\Sigma(r) = \Sigma_0 \left(\frac{r}{r_c}\right)^{-\gamma} \exp\left[-\left(\frac{r}{r_c}\right)^{2-\gamma}\right], \quad (3)$$

218 with $\gamma = 0.8$ and $r_c = 200$ au. The mass normalization constant is given by,

$$\Sigma_0 = (2 - \gamma) \cdot \frac{M_{\text{gas}}}{2\pi r_c^2} \cdot \exp\left[\left(\frac{r_{\text{in}}}{r_c}\right)^{2-\gamma}\right]. \quad (4)$$

219 where $M_{\text{gas}} = 0.09 M_{\text{sun}}$ and $r_{\text{in}} = 20$ au. Since we use two-dimensional simulations to efficiently
 220 explore the parameter space, the temperature profile at the disk midplane is adopted, $T_{\text{mid}}(r) =$
 221 $21 \times (r/r_c)^{-0.3}$ K, along with an isothermal equation of state. We assume a uniform disk viscosity

222 of $\alpha = 10^{-3}$, where α is a dimensionless parameter characterizing the efficiency of mass transport
223 defined as in the canonical α prescription⁴⁵. This choice is consistent with the constraints on the
224 turbulence level in the HD 163296 disk^{28,29}.

225 An initial parameter study was performed using one planet at a time. We place a planet at
226 either 105 or 160 au, which are the locations suggested by the continuum ring locations³, and test
227 four different planetary masses at each location: 0.1, 0.3, 1, and 3 M_{Jup} . We insert planets at
228 the beginning of simulations with their full masses. We have tests in which we begin simulations
229 with 20 Earth-mass cores and grow them over time by accreting available disk material from their
230 vicinity^{46,47}. However, the final gap shapes are almost identical to the case we start with full planet
231 masses. This is because the available masses around the planetary orbits in the HD 163296 disk
232 are much larger than the planets' final masses, so that most of the disk material is pushed away by
233 the planets and only small fraction is accreted.

234 We compare the difference between the minimum and maximum δv_{rot} values measured in
235 numerical simulations with that obtained from the C¹⁸O observation. Using this approach, we find
236 that both at 105 and 160 au a 1 M_{Jup} planet yields a reasonable match. Because of the lack of a
237 δv_{rot} minimum at < 70 au in the C¹⁸O observation, we were not able to use the same approach for
238 the innermost planet. We thus adopt 0.1 M_{Jup} as our initial attempt, as suggested by Isella et al.³.

239 We then include all three planets and vary their masses by 0.1 M_{Jup} and their locations by
240 5 au to find our best-fit model: 0.6 M_{Jup} planet at 65 au, 1 M_{Jup} planet at 100 au, and 1.3 M_{Jup}
241 planet at 165 au. The surface density and the gas rotation velocity are shown in Fig 9.

242 For this second part of the parameter study, we generate simulated C^{18}O velocity profiles
243 to compare these models with the observations. To do so, the surface densities obtained from
244 hydrodynamic simulations were inflated to a full 3D structure using a commonly used parametric
245 hydrostatic structure using the temperature structure from Flaherty et al.²⁹. The C^{18}O abundance
246 was assumed to be 8.67×10^{-8} with a vertical distribution bounded by the freezeout temperature
247 of 27 K to the bottom and a shielding column of $1.2 \times 10^{21} \text{ H}_2 \text{ cm}^{-2}$ above⁴⁸. The velocity
248 structure was calculated using Eqn. 1. Radiative transfer was performed with the non-LTE code
249 LIME⁴⁹ with image values matching the observation. As we do not expect significant spatial
250 filtering from the data³, the images were convolved with a 2D Gaussian beam consistent with the
251 C^{18}O observations to provide a fair comparison. We limit ourselves to comparison with only C^{18}O
252 because in the upper layers, where ^{12}CO is observed to arise, the assumed parametric structure
253 deviates significantly from self-consistently calculated physical structures⁵⁰.

254 Using this iterative process between hydrodynamic simulations and radiative transfer calcu-
255 lations, we were able to constrain the planetary masses and the radial locations within $\pm 50\%$ and
256 $\pm 10\%$, respectively. Figure 10 demonstrates how the δv_{rot} profile changes with these uncertain-
257 ties. We note that these masses are considerably larger than those estimated from the continuum
258 gaps³ as the method presented here does not require poorly known relative abundances and is
259 directly tracing the gas pressure.

260 The value of δv_{rot} at the planet locations is not zero due to the global pressure gradient
261 from the radially decreasing temperature and density, and the non-negligible height of the C^{18}O
262 emission. This can be clearly seen in panel (c) of Figure 2 where $\delta v_{\text{rot}} \approx -2\%$ at the planet

263 locations, consistent with the observations.

264 As when fitting the continuum gaps³, no perfect fit with a planet could be found for the
265 perturbation at < 80 au. Using a $0.6 M_{\text{Jup}}$ planet at 65 au provided a reasonable fit but was
266 unable to fully account for the sharp deviation in δv_{rot} . It appears from Figure 10 that pushing
267 the innermost planet outward could produce a δv_{rot} peak at 75 au; however, locating a planet at
268 ≥ 70 au resulted in the formation of a single, wide gap together with the planet at 100 au, rather
269 than the formation of two separate gaps. Even with α ranging between 0 and 10^{-3} , no reasonable
270 fit was found.

271 We have also examined a possibility that the secondary spiral arm excited by the planet at
272 100 au opens a secondary gap at ~ 70 au. The location of secondary gap is determined mainly by
273 the disk temperature and the planetary mass⁹, and for the disk temperature assumed in the present
274 work we found that a secondary gap forms with $\alpha \lesssim 10^{-4}$, but at < 65 au regardless of the
275 planetary mass.

276 The rapid drop in δv_{rot} at < 75 au might indicate a rapid increase in gas density there, which
277 could potentially be associated with radially varying accretion efficiency in the disk. Recent radia-
278 tive transfer modelling of scattered light images of the HD 163296 disk indeed supports this idea
279 of rapid gas density increase inside of the innermost gap³⁷. Future higher resolution observations
280 will help better understand the origin of the innermost gap.

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394 **Data availability** This paper makes use of the following ALMA data: JAO.ALMA#2013.1.00601.S,
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412 **Author Informations** Reprints and permissions information is available on request. The authors declare
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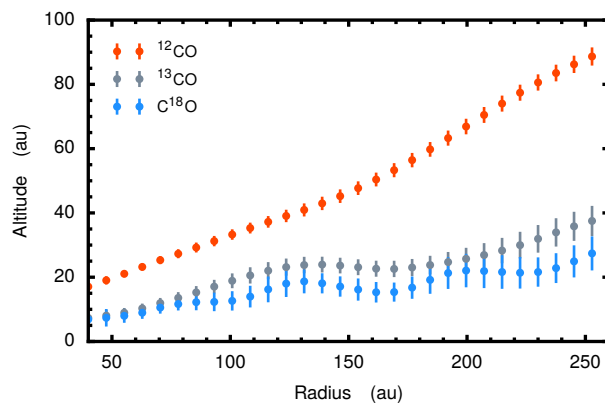


Figure 5: **Emission surfaces for the three CO isotopologues.** Derived following the method presented in ²². Error bars show the 3σ uncertainties.

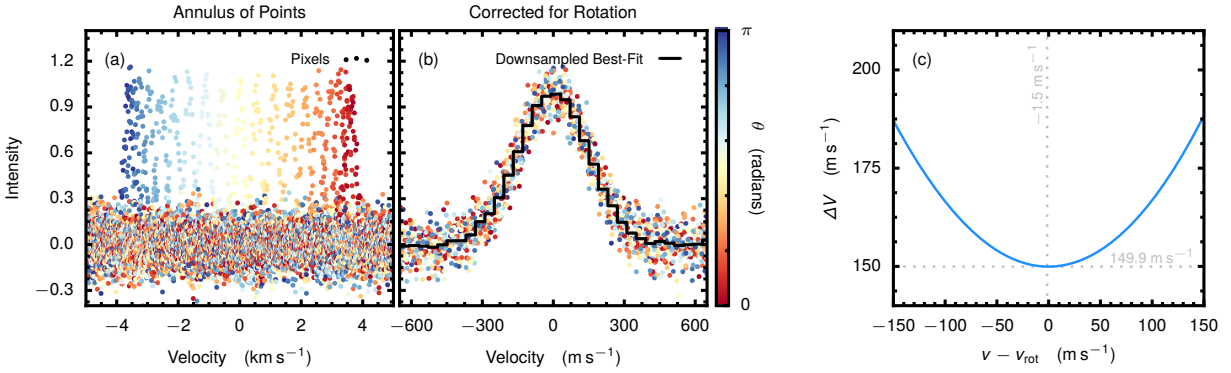


Figure 6: **Demonstration of the method used to calculate v_{rot} .** Panel (a) shows the pixel values taken from an annulus of constant radius. Intrinsic line widths are 150 m s^{-1} sampled at 40 m s^{-1} . Correcting for the rotation, the points align to a single Gaussian as shown in panel (b), sampling the profile at a rate of $\approx 2 \text{ m s}^{-1}$. Colours of the points show their relative position angle in the disk. The black line shows the best-fit Gaussian profile, binned back down to the native velocity resolution. The line width is a convex function of rotation velocity as shown in panel (c). The dotted lines show the values where line width is minimized demonstrating that both v_{rot} and line width are recovered to $< 2 \text{ m s}^{-1}$.

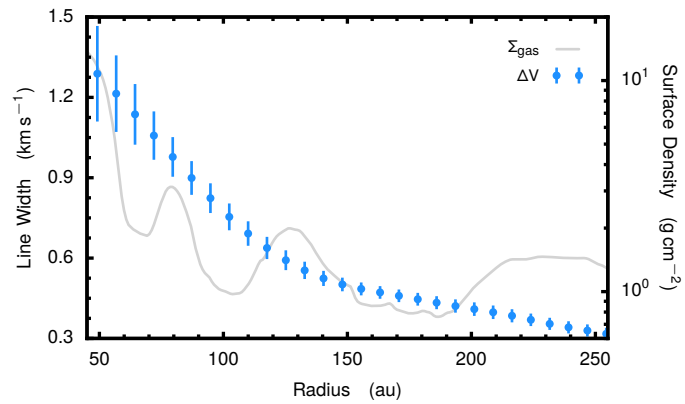


Figure 7: **Line width of the C¹⁸O emission.** No significant deviations from the rotational profile of the line width (shown by blue points with 3σ uncertainties) are observed across the surface density perturbations, shown by the gray solid line, suggesting a smooth temperature profile across the gaps.

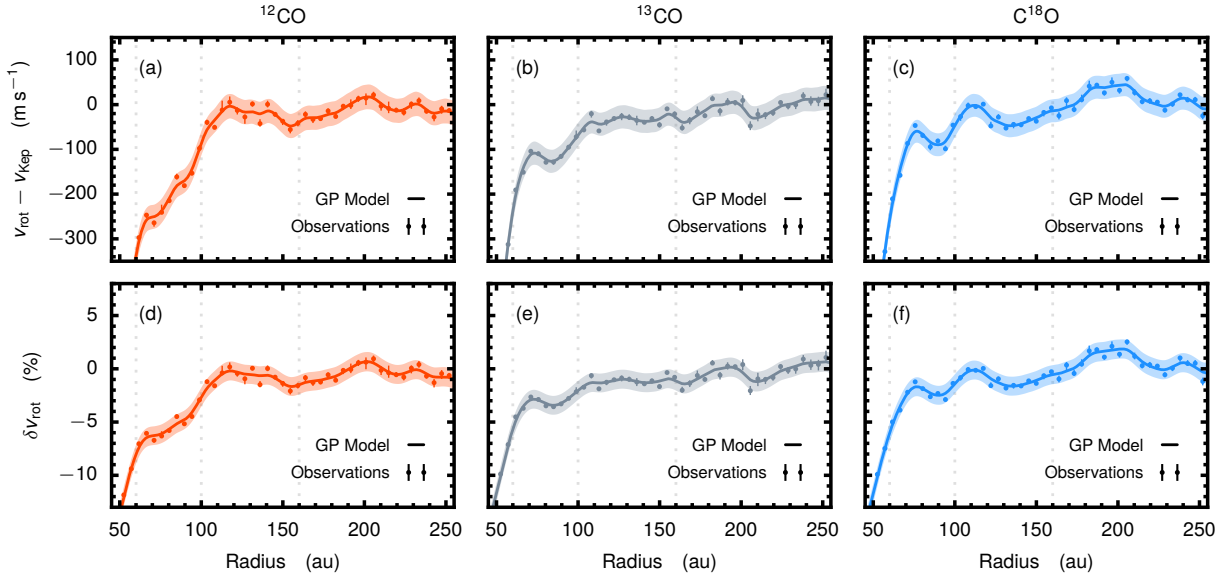


Figure 8: **Rotation velocities for the three CO isotopologues.** ^{12}CO , left; ^{13}CO , middle and C^{18}O , right. The top row shows the difference from v_{Kep} and the bottom row shows the relative difference. Observations are shown by the points with 3σ uncertainties. The solid line and shaded region are the Gaussian Process model and associated 3σ uncertainty. The dark rings in continuum emission are shown by the dashed lines.

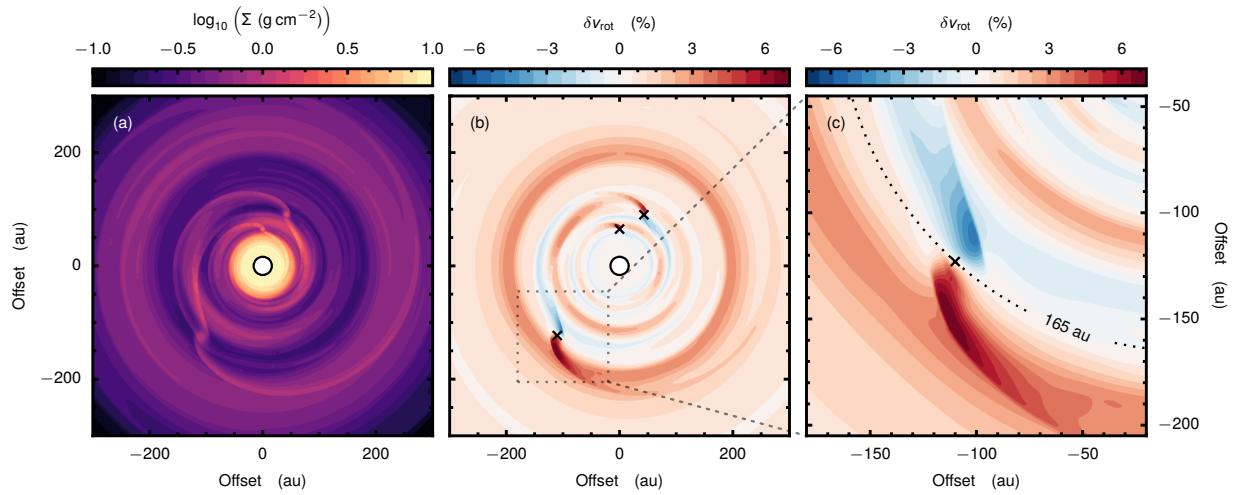


Figure 9: **Surface density and velocity structure of the hydrodynamical model.** The surface density is shown in the left panel while the centre shows δv_{rot} at the midplane. Planet locations are shown with a cross. The right panel shows a zoom in of the outer planet, showing the details of the sub- and super-Keplerian rotation inwards and outwards of the gap.

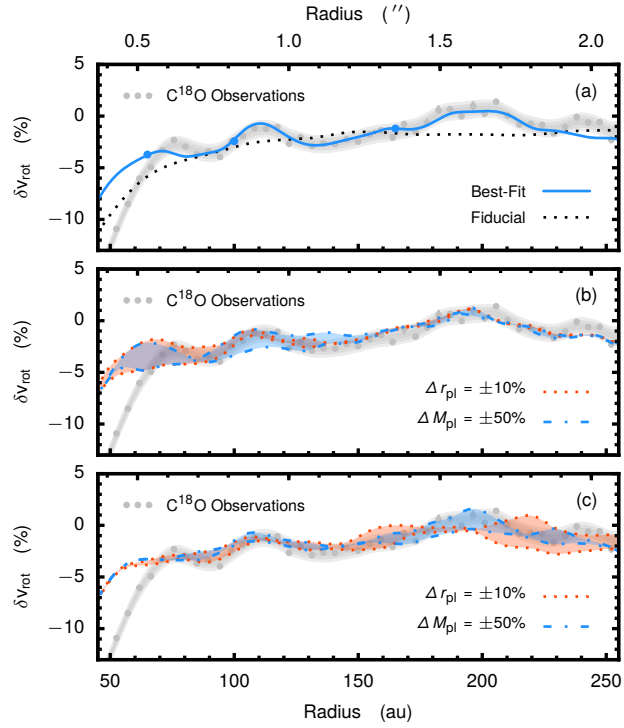


Figure 10: **Sensitivity of δv_{rot} to planetary parameters.** The best-fit hydrodynamical model is shown with the blue line overlaid to the observations in panel (a). The gray region shows the 3σ range of the Gaussian Processes model of the observations. The black dotted lines shows v_{rot} for the fiducial model, showing the fall off at small radii is due to the imaging. Panels (b) and (c) demonstrate the sensitivity of δv_{rot} to changes in planet mass and position for the planet at 100 au and 160 au, respectively. The red shaded region shows the changes in δv_{rot} with a 10% change in the radial location of the planet while the blue shaded regions show the change from a 50% change in planet mass. For panels (b) and (c), only one planet is moved at a time.