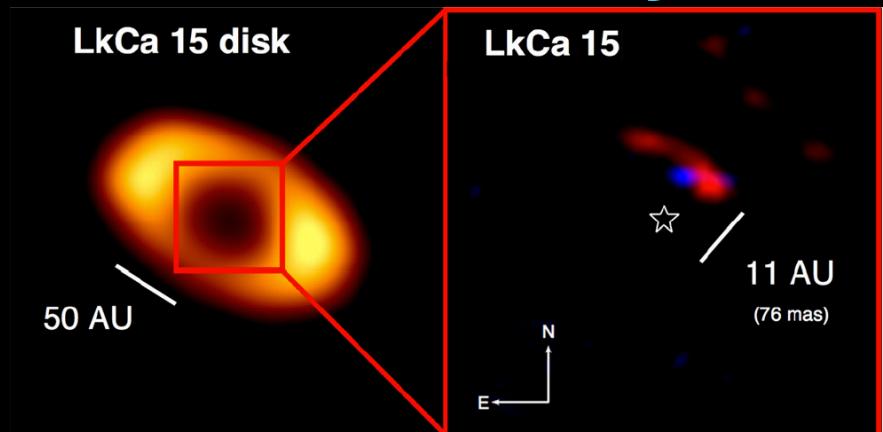


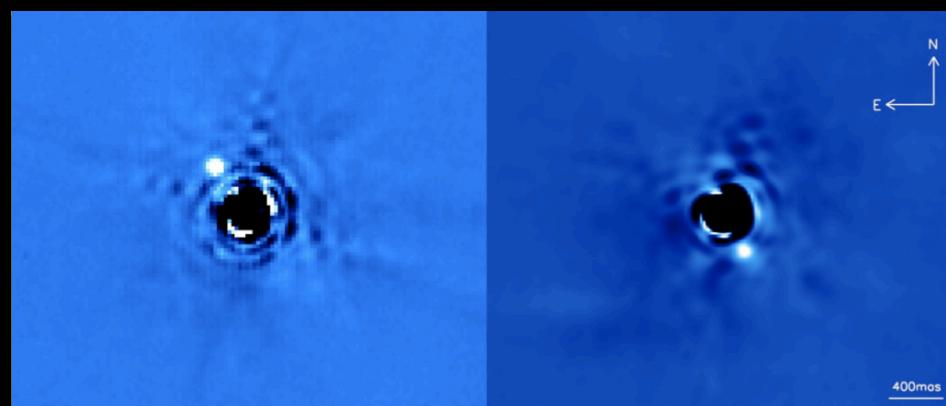
# **STATISTICAL ANALYSIS OF EXOPLANET POPULATIONS FROM LARGE-SCALE DIRECT IMAGING SURVEYS**

Beth Biller, Markus Feldt, Maria  
Lenius, SPHERE WP4  
Mike Liu, Zahed Wahhaj, Eric Nielsen,  
and the NICI Campaign team

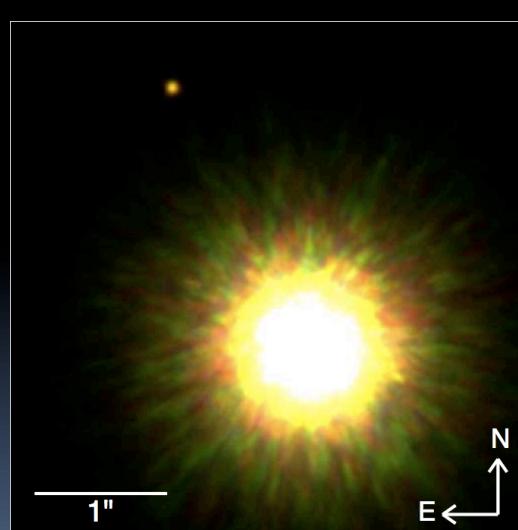
# $\sim$ 10 Directly Imaged Exoplanets...



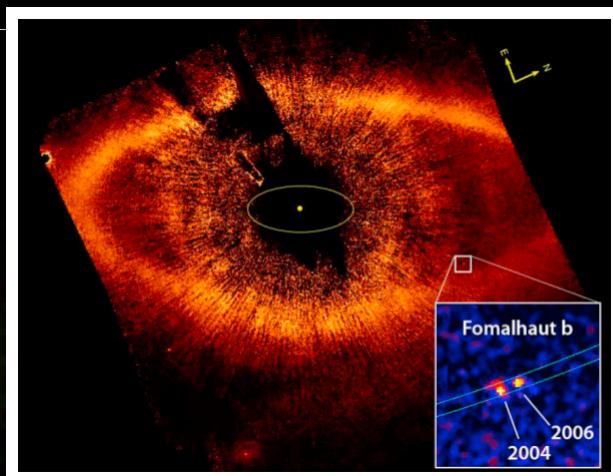
Kraus and Ireland 2012



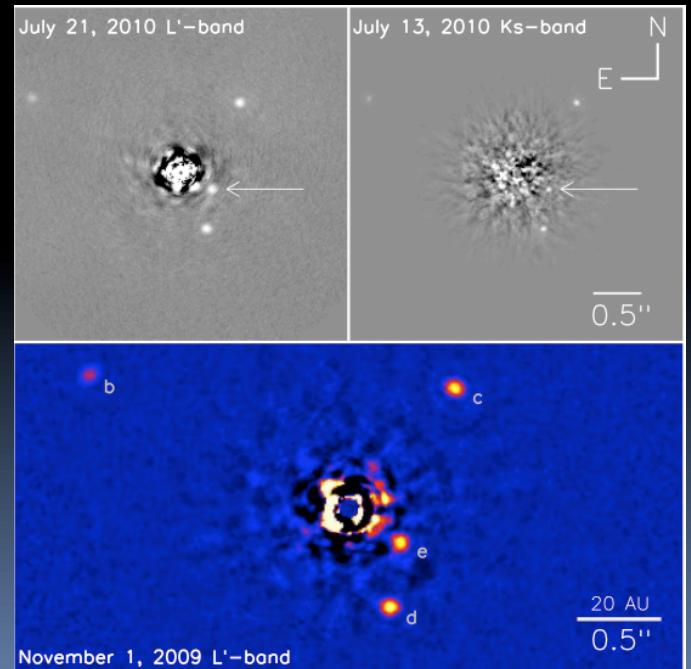
Lagrange et al. 2008, 2010



Lafrenière et al. 2008, 2010



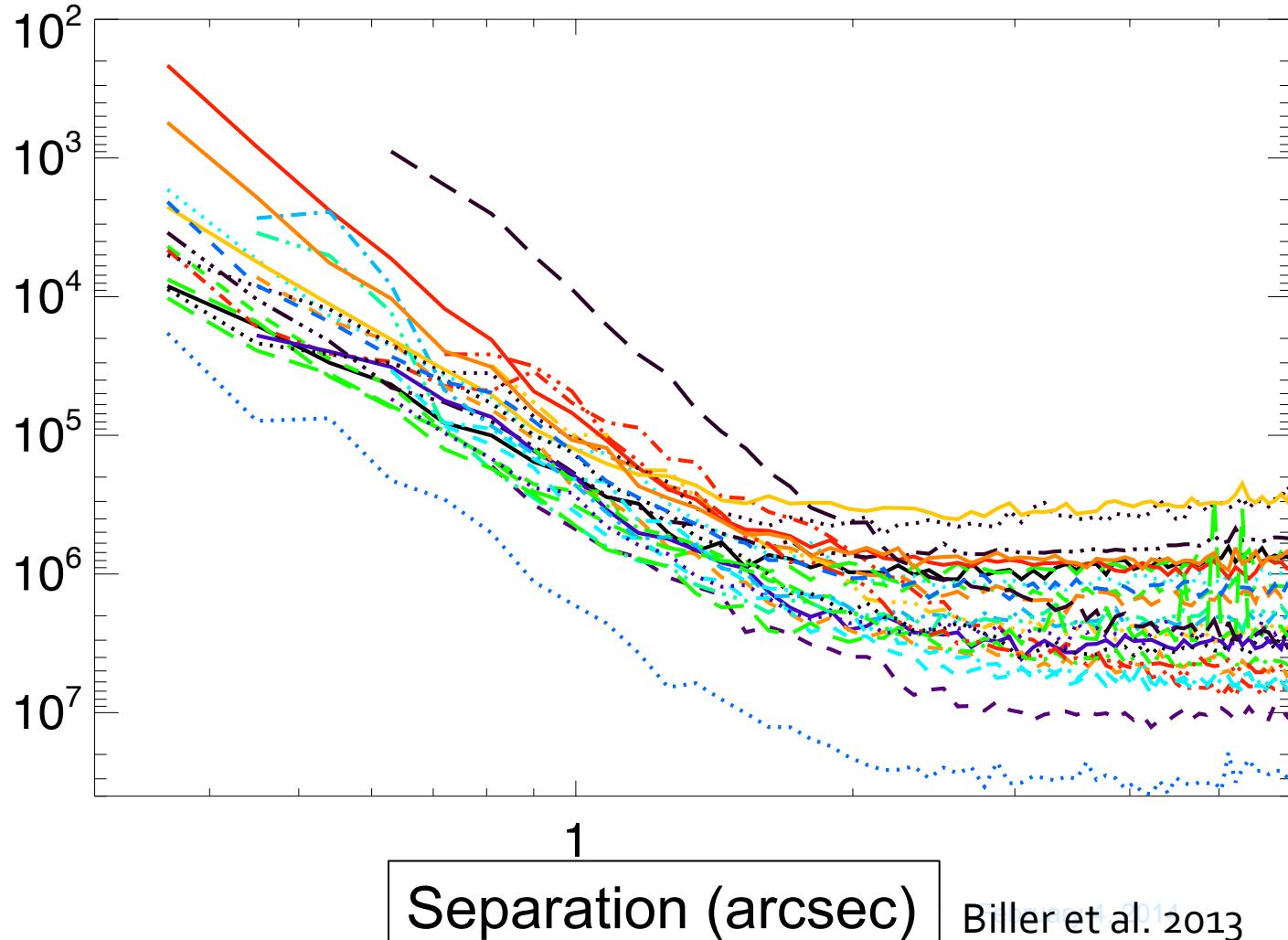
Kalas et al. 2008



Marois et al. 2008, 2010

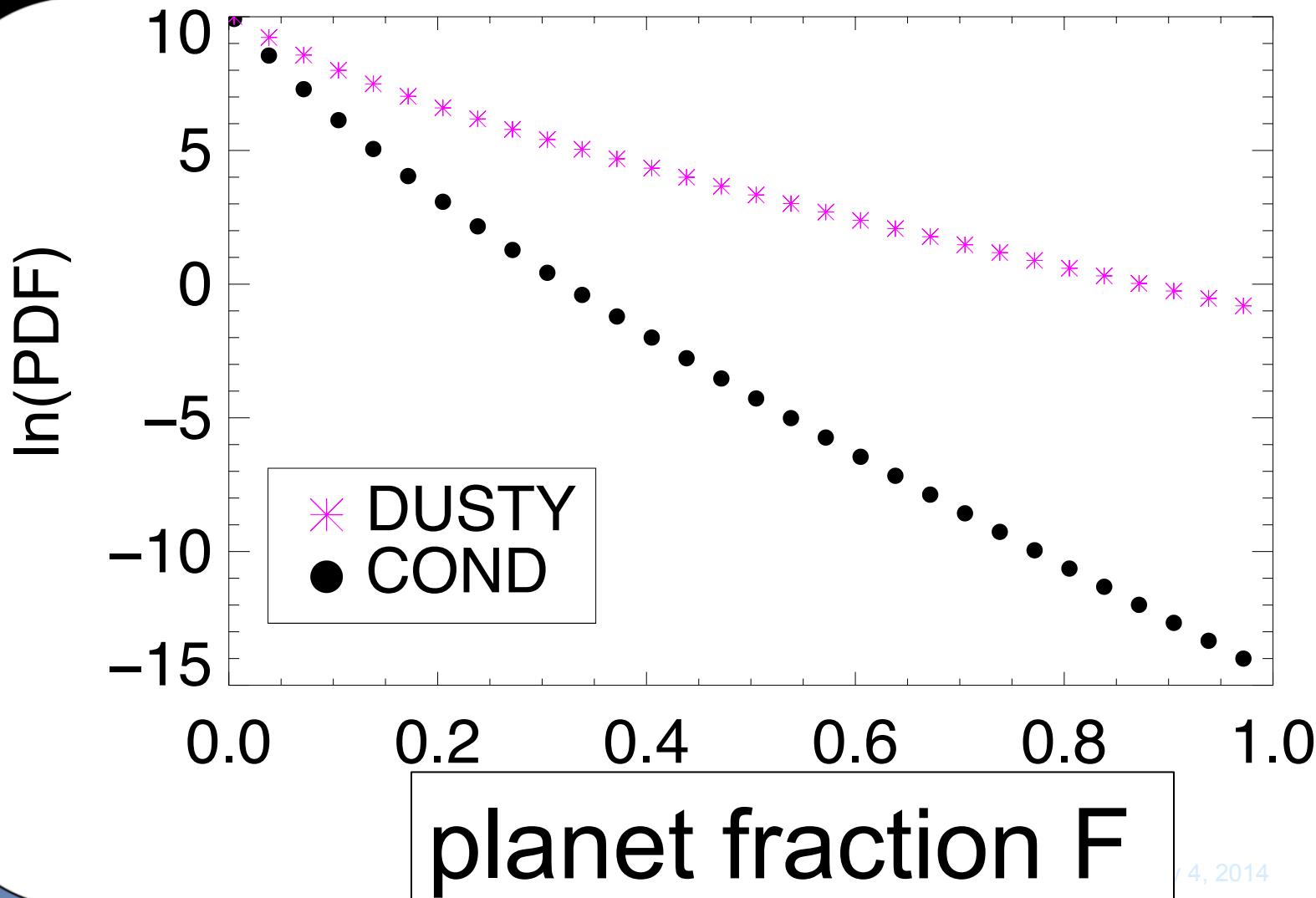
Out of 100s of stars surveyed  
to quite deep contrasts...

Attainable Star-  
Planet Contrast



# Current Survey Statistics already place strong constraints

Biller et al. 2013

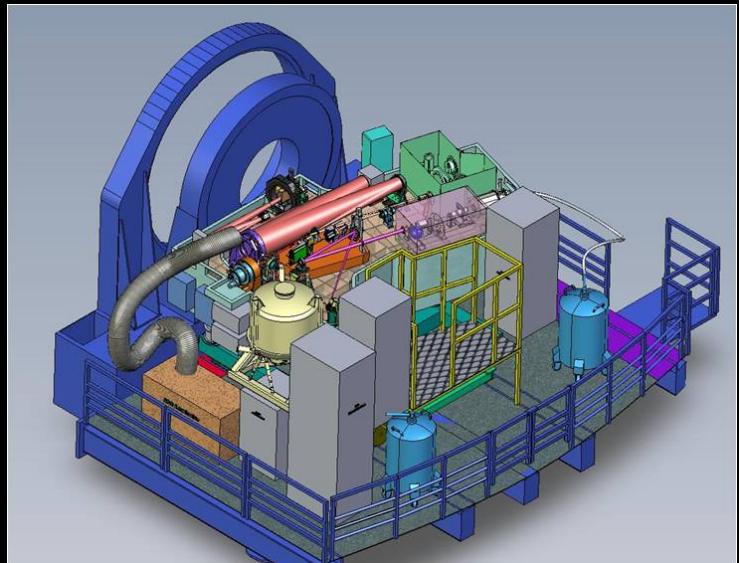


# Strongest Constraint on Planet Fraction to date from 78 NICI Campaign stars:

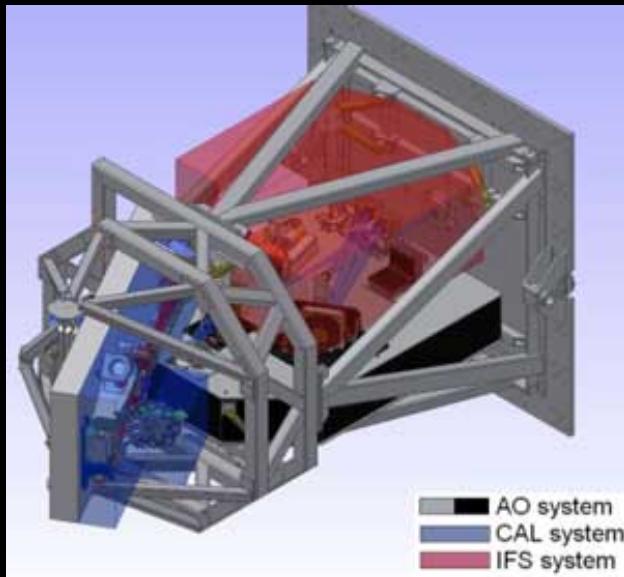
<8% host 1-20 Mjup  
planets at semi-major  
axes of 10-150 AU  
(95% confidence level, COND models)

# Upcoming Instruments

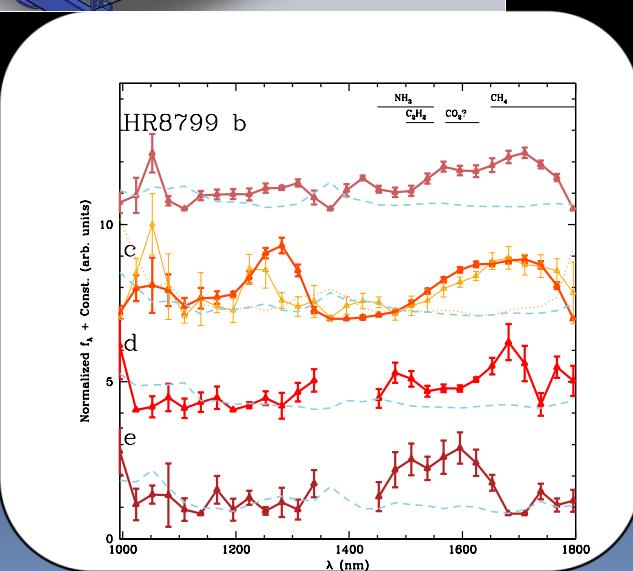
SPHERE @ VLT



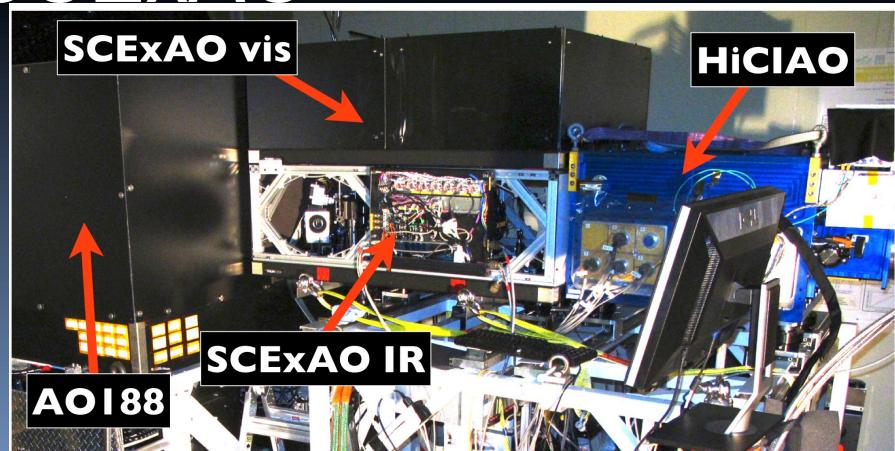
GPI @ Gemini



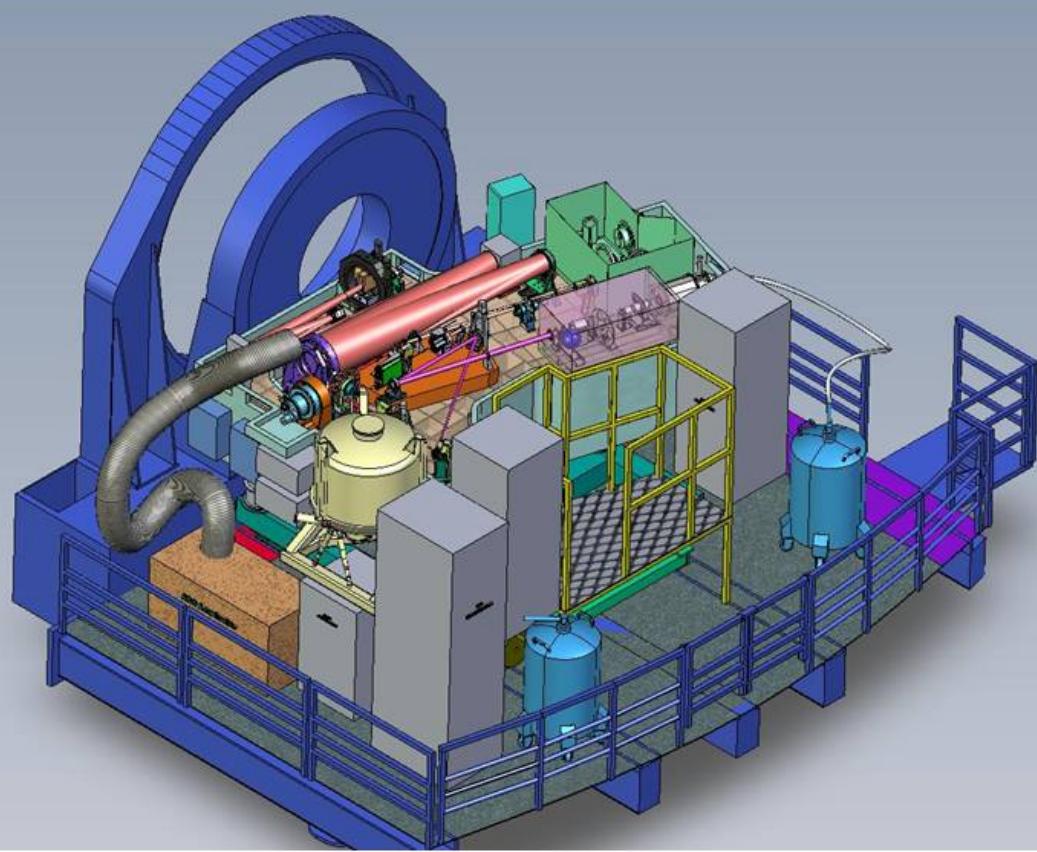
Project  
1640



SCExAO

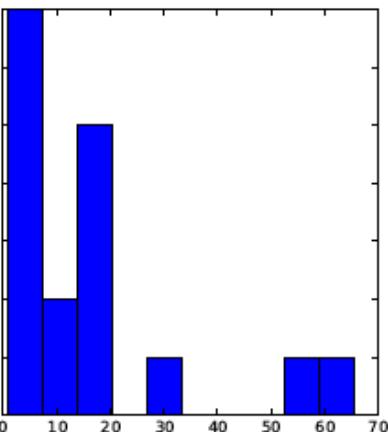


# NIRSUR with SPHERE @ VLT - predicted start in 2015

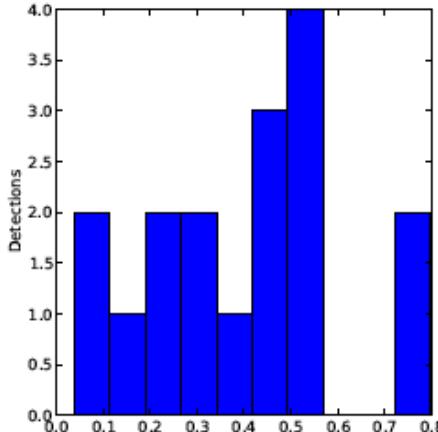


# Simulated Surveys for SPHERE NIRSUR

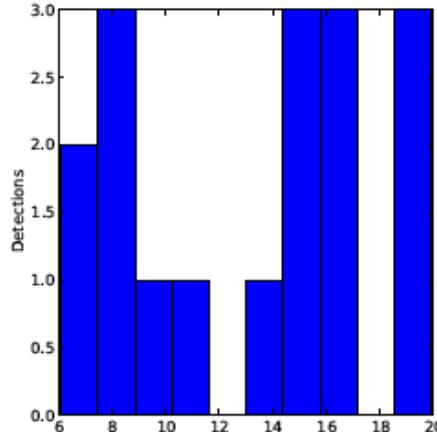
Number Detected



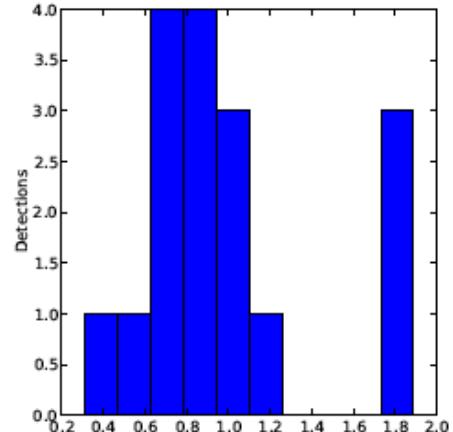
Planet  
Mass ( $M_{Jup}$ )



Planet  
Eccentricity



Semi-Major  
Axis (AU)



Stellar  
Mass ( $M_{Sun}$ )

Monte Carlo simulation following  
the approach of Nielsen & Close, 2010  
and Bonavita et al. 2012.

# Assumed Planet Distribution

$$dN/dm \propto m^\alpha, \alpha = -0.63$$

$$dN/da \propto a^\beta, \beta = -1.16$$

until cutoff radius

Cumming et al. 2008 found  $\alpha \sim -0.63$  and  $\beta \sim -1.16$  for  
RV planets out to  $\sim 8$  AU

$$R(a, M | \alpha, \text{cutoff}, \beta, C) = CM^\beta a^\alpha$$

(until cutoff, where C is a normalization factor related  
to planet frequency F)

# Normalize to known RV planets

Fischer and Valenti 2005 find a  
**planet frequency of 3.94%** for  
planets with:

- Mass 1-13 Mjup
- separations 0.3 – 2.5 AU
- stellar mass: 0.7 – 1.6 Msun
- [Fe/H]: -0.5 – +0.5

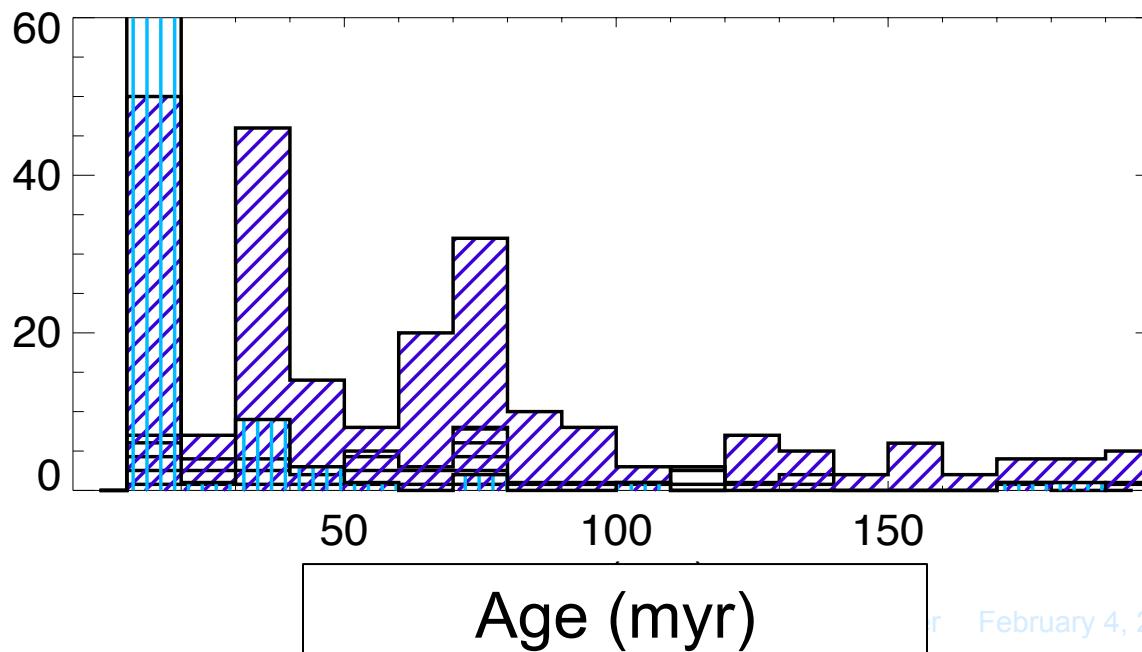
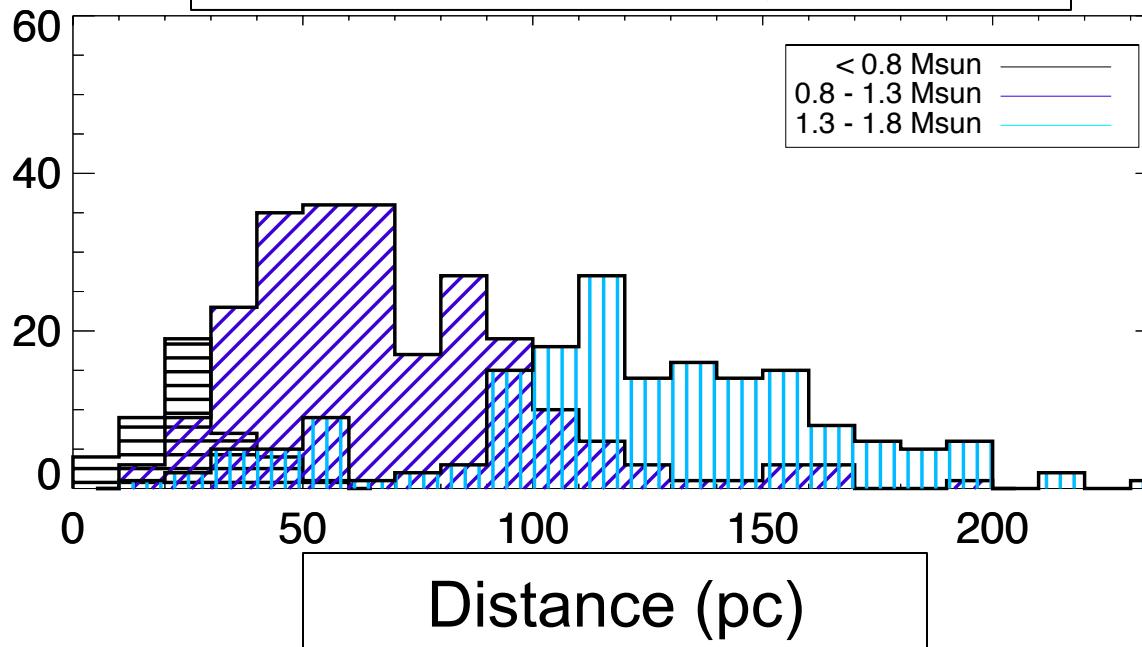
# Mass-Scaled Planet Distribution

$$dN/dm \propto m^\alpha M^{-\alpha}$$

$$dN/da \propto a^\beta \text{ until cutoff radius}$$

Cumming et al. 2008 found  $\alpha \sim -0.63$  and  $\beta \sim -1.16$  for  
RV planets out to  $\sim 8$  AU

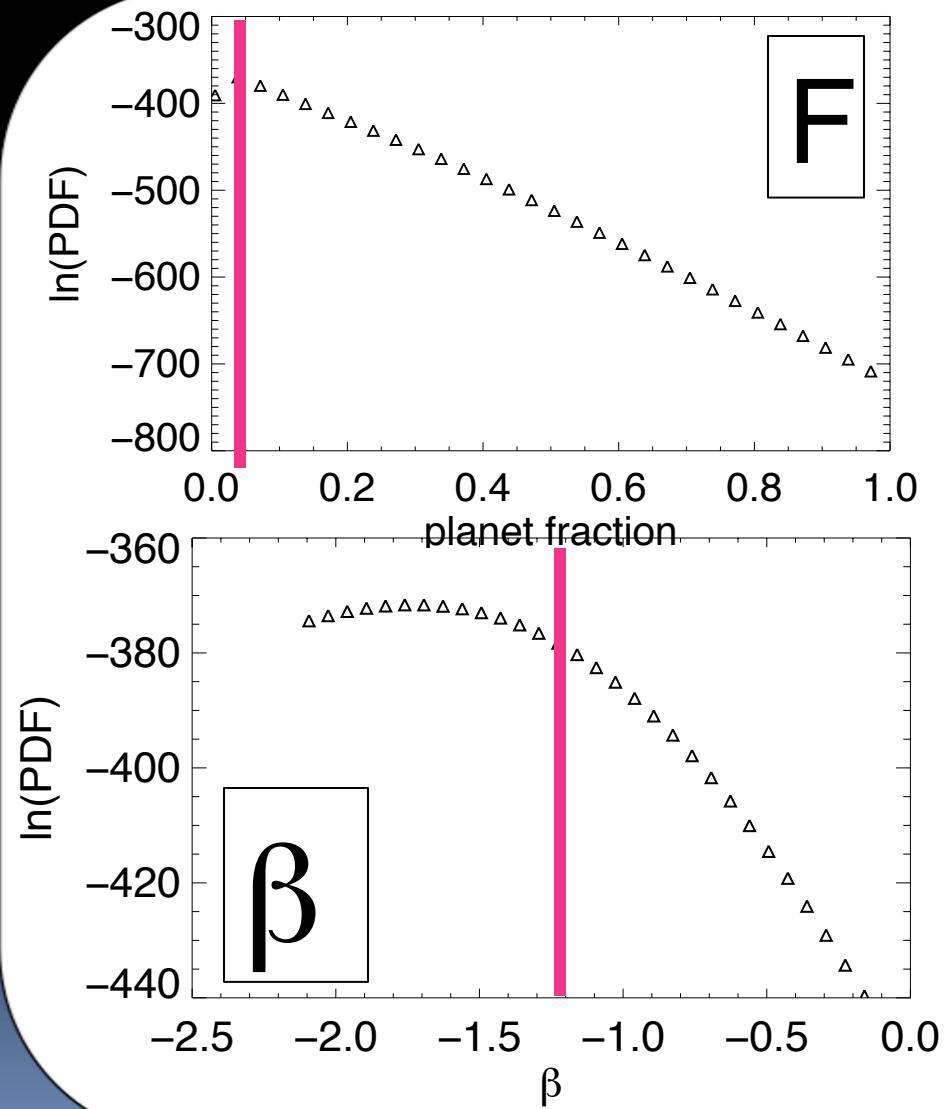
# 400 star 8 – 200 Myr sample



# Predicted # of detections vs. cutoff

SMA Cutoff	Unscaled	Mass-Scaled
20 AU	$17 \pm 4$	$27 \pm 6$
30 AU	$26 \pm 7$	$46 \pm 3$
40 AU	$34 \pm 5$	$57 \pm 5$
50 AU	$43 \pm 4$	$66 \pm 5$

# Bayesian retrieval of simulation parameters



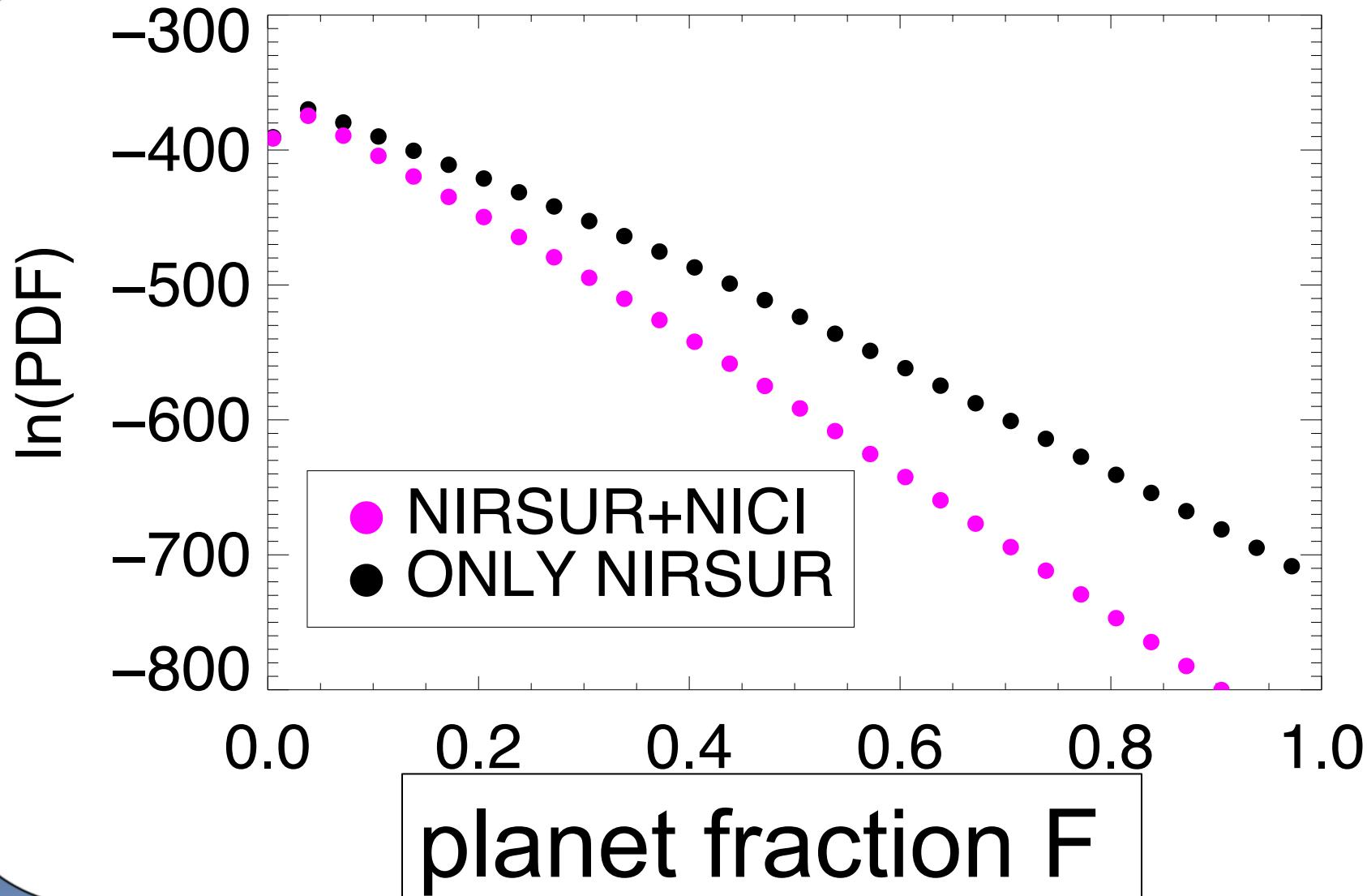
Current surveys are the  
prior for future surveys

# Constraints from Current + Future Surveys

- 400 star simulated NIRSUR
- 78 MG stars from Biller et al. 2013



# Bayesian retrieval of simulation parameters



# Conclusion

Strongest constraints will likely continue to be for:

**planet fraction F**

# Bayes' Theorem

Posterior PDF

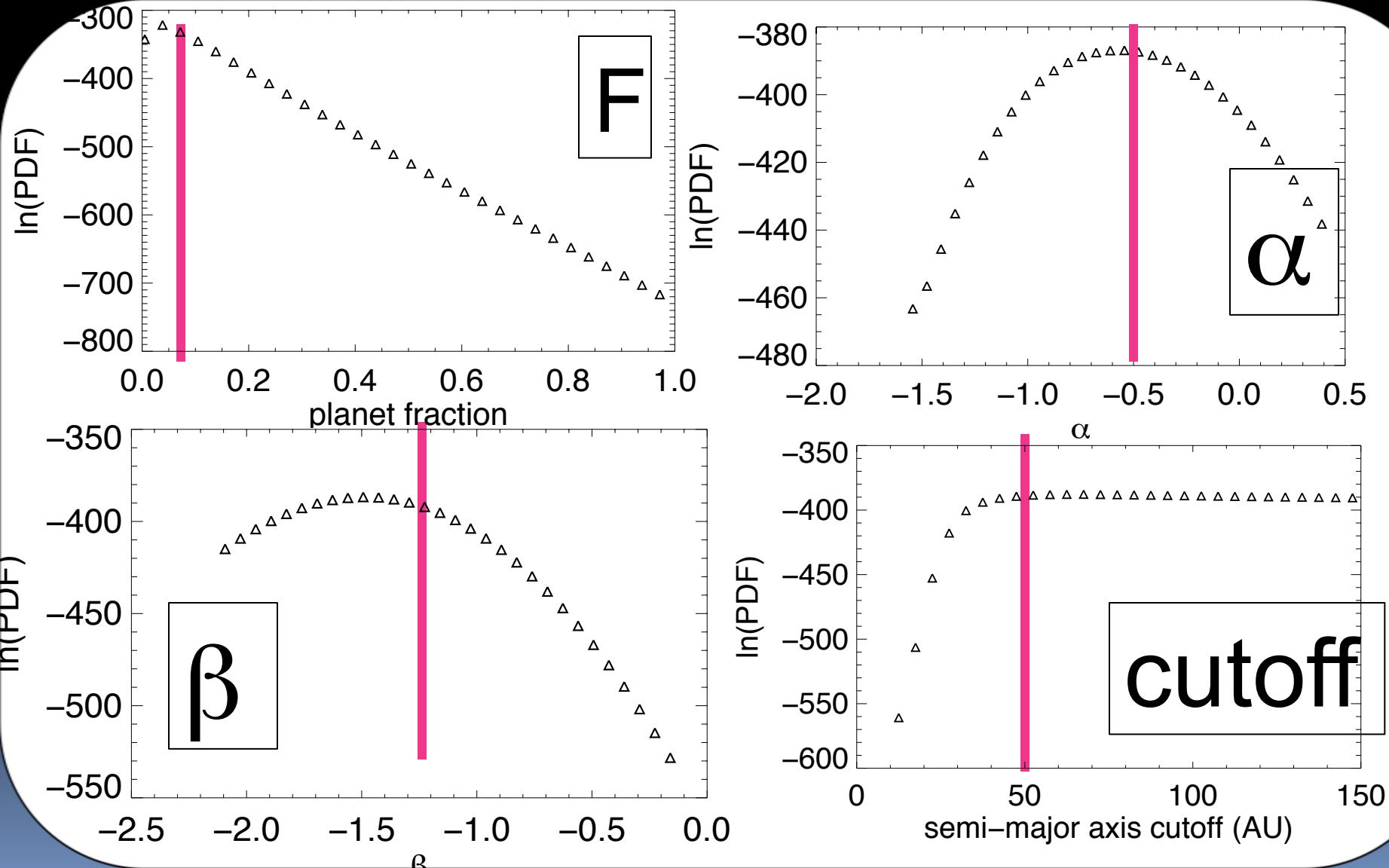
$$\text{prob(model|data,I)} \propto$$
$$\text{prob(data|model,I)} \times \text{prob(model|I)}$$


Likelihood Function

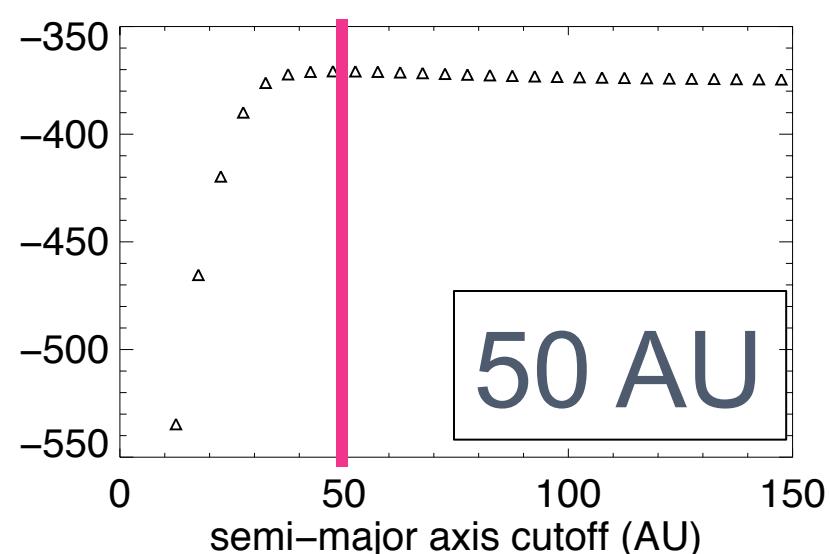
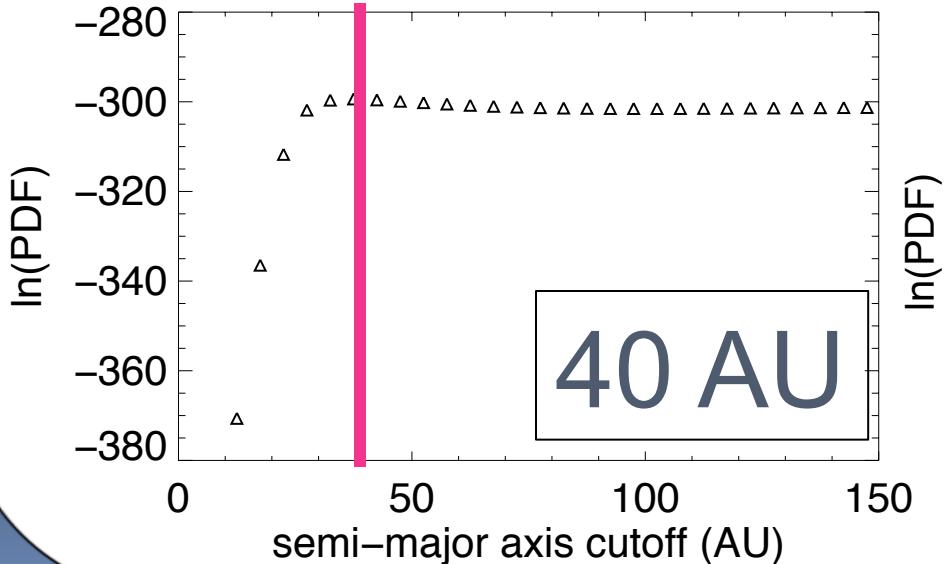
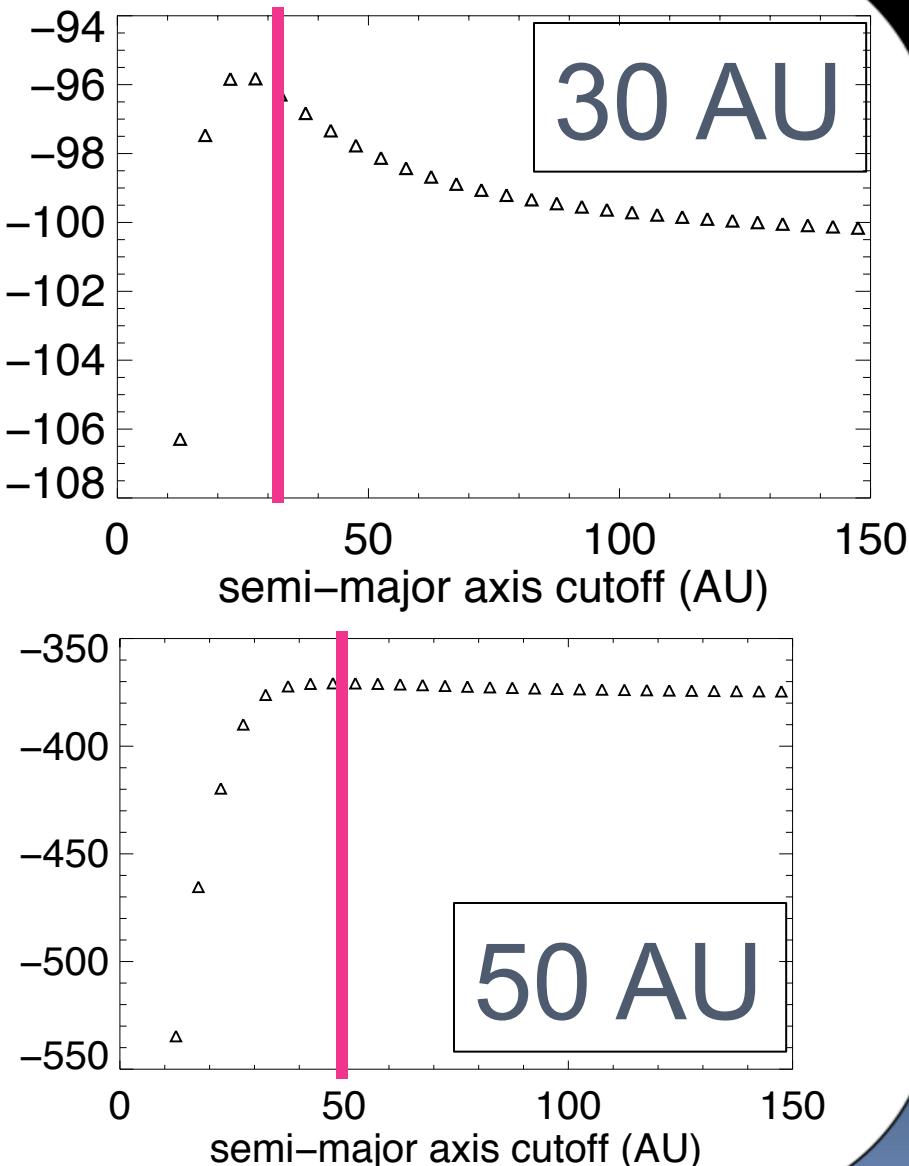
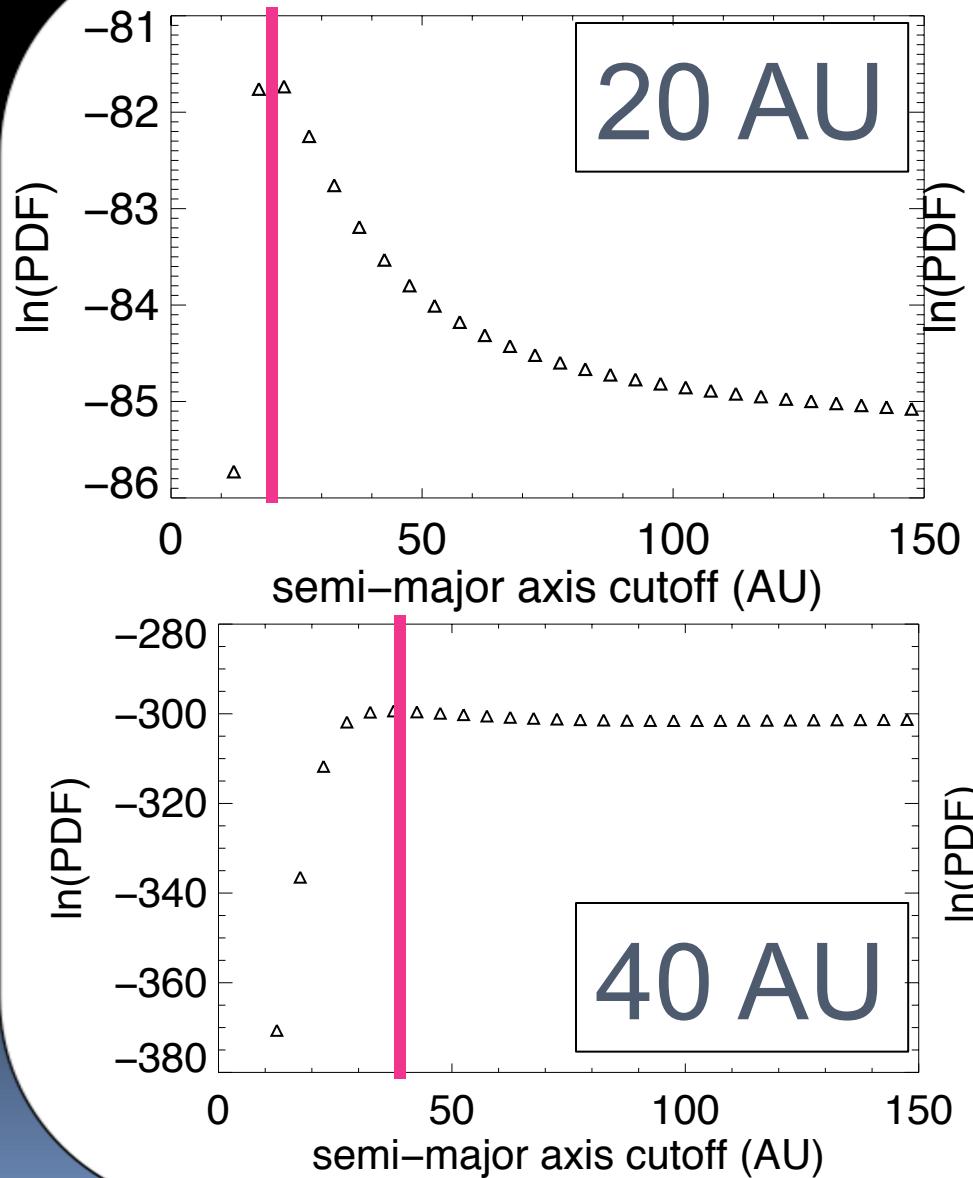


Prior

# Same thing, Gaussian priors on $\alpha$ and $\beta$



# Constraints on Cutoff



# Constraints on Cutoff- Gaussian Priors

