# What is this radio interferometry business anyway?



#### What are you letting yourself in for?



EUROPEAN ARC ALMA Regional Centre || UK

# What is useful to know

- Basics of interferometry
- Calibration
- Imaging principles
- What provides detectable sources?
  - ALMA spatial coverage
  - Spectral details: see OT session
- Simulations for ALMA

# What is useful to know

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  - Spectral details: see OT session
- Simulations for ALMA

#### sim•u•late ('sim yə,leit)

to intend to deceive; make a pretence of; feign: e.g. to simulate illness:

Friquet .... under the pretext of having a swollen face which he had managed to <u>simulate</u> by introducing a handful of cherry kernels into one side of his mouth, and had procured a whole holiday from Bazin. **Twenty years after** (Alexandre Dumas)





- Earth rotation aperture synthesis
- Vectors between pairs of baselines sweep out *uv* tracks
  - Record combined signals per sec
- Maximum resolution (synthesised beam)  $\theta \sim \lambda / B_{max}$ 
  - $\underline{B}$  15 km,  $\lambda$  1 mm =  $\theta$ ~14 mas
- Field of view  $\lambda/D_{antenna} \sim 20''$ 
  - Equivalent to single dish resolution







- Earth rotation aperture synthesis
  - Fourier transform ⇔ Dirty Beam
- Sensitivity helped as noise decorrelates *but*
  - Sparse coverage gives sidelobes
- Max. angular scale imageable
  - $\sim 0.6 \ \lambda/B_{min} \sim 8'' \ (\lambda \ 1 \ mm)$ 
    - no ACA, compact 12-m config







- Combined  $\phi$  depends on  $\delta s$
- Complex visibility amplitude is sinusoidal function of  $\boldsymbol{\phi}$

### Earth rotation aperture synthesis



 Telescopes separated by baseline B<sub>geom</sub>

- Earth rotates
  - Projected separation  $b = B_{geom} \cos \theta_0$
- Samples different scales of source
- Additional geometric delay path  $\Delta$ 
  - Remove in correlator



# Earth rotation aperture synthesis



(3)

(2)

core

lobe

- Complex visibility amplitude is sinusoidal function of  $\boldsymbol{\phi}$ 

1/06

1/04

# Correlation

- Digitise and combine signals in correlator
  - Create spectral channels by adding ~msec time lags
  - Make parallel (and cross) polarizations
    - (another) FT into frequency domain
      - Output averaging determines integration time
- Produces complex visibility data
  - Time series of amplitudes & phases per baseline
    - per polarization, per spectral channel



### From interferometry to images

Source

- Fourier transform of complex visibility amplitude and phase gives sky brightness  $\sum V_v(u_v,v_v) e^{[2\pi i(uvl + vvm)]} dudv = I_v(l,m)$  $- \text{ or } V(u,v) \Leftrightarrow I_v(l,m) \text{ for short}$
- Sensitivity:  $\sigma_{rms} \propto \frac{T_{sys}}{\sqrt{N(N-1)/2} \ \delta v \ \Delta t}$ 
  - Number antennas (ALMA's huge collecting area!)
    - dv freq. width per image,  $\Delta t$  total time on source



# ALMA instrumental calibration

- Pointing corrections before correlation
- Water vapour in the troposphere
  - Refraction: delay to phase of incoming wavefronts
    - Water Vapour Radiometry (WVR)
    - Measure 183-GHz atmospheric line
      - Derive path length corrections at observing v every second
  - Amplitude absorption amd emission
    - System temperature measurements every few min ( $T_{sys}$ )
- Residual delay and bandpass errors
  - Phase & amplitude corrections as a function of  $\boldsymbol{\nu}$
  - Derive from bright astrophysical source
    - Good signal to noise in a single channel
- Planets, large moons, asteroids to set flux scales
- Phase-referencing corrects time-dependent errors

PWV ~0.6, Band 9 raw 0.25 - 2.5 km baselines



Time



# Calibration sources: flux density

- Primary flux calibration uses planets, moons, asteroids
  - Models and ephemerides available
  - Mostly negligible polarization

0.05

- Still often have to select short baselines!
- Beware planet/moon atmspheric lines
  - If no Solar System object, use monitored QSO



# Phase referencing

- Observe phase-ref source close to target
  - Point-like or with a good model
  - Close enough to see same atmosphere
    - Few 10 degrees (isoplanatic patch)
  - Bright enough to get good SNR quicker than atmospheric timescale  $\boldsymbol{\tau}$ 
    - (after WVR applied)
    - $\tau$  10 min/30 s short/long *B* & low/high v
- Nod on suitable timescale e.g. 5:1 min
  - Derive time-dependent corrections to make phase-ref data match model
  - Apply same corrections to target
  - May correct amplitudes similarly
- Self-calibration works on similar principle



### Source structure in uv plane



Baseline length in wavelengths (uv distance)

..5e+06 2e+06 2.5e+06 UVDist\_L

3e+06

3.5e+06

#### Phase errors in 3D



# Calibration strategy

- Need Signal to Noise Ratio  $\sigma_{ant}/S_{calsource} > 3$ 
  - per calibration interval per antenna

$$\sigma_{ant}(\delta t, \delta v) \approx \sigma_{array} \sqrt{\frac{N(N-1)/2}{N-3}}$$

- $\sigma_{\text{array}}$  is noise in all-baseline data per time-averaging interval per frequency interval used for calibration
- Have to average in time and/or frequency
  - Bandpass first or time-dependent cal. first?
    - Do not average over interval where phase change  $d\phi > \pi/4$
  - Keep polarizations separate if possible in early calibration
- Usually start with bandpass calibration
  - Instrumental artefacts, shallow atmospheric lines...
    - May need to perform time-dependent  $\boldsymbol{\phi}$  calibration first

#### This example: $d\phi < \pi/4$ over inner 50% band

- Bandpass calibrator bright as possible
  - Average inner 50% band, perform time-dependent phase & amp calibration (G1) with solint required for SNR
    - If atmospheric lines, chose channel intervals to avoid
  - **2.** Apply calibration (G1), average all times for freq. dependent phase and amplitude calibration, i.e. bandpass calibration (B1).
    - Smooth every e.g. 20 channels if necessary for SNR
      - G1 is not used any more
- Phase-reference fairly bright source
  - **3.** Apply B1 and perform time-dependent phase calibration (G2) averaging all channels, shortest *dt* for enough SNR
    - Apply B1 for all calibration hereafter, to all sources
  - **4.** Apply B1 and G2 and perform time-dependent amp. cal.
    - Amp calibration needs higher SNR than phase-only; for bright sources you can do it all in step 3.









### Effects on imaging



#### No astrophysical calibration: no source seen



#### Amplitude and phase solutions: source seen, snr 22



(r)

Phase-only solutions: source seen, snr 15

#### CASA calibration: Measurement Equation

 $\underline{V}_{ij} = \mathbf{M}_{ij}\mathbf{B}_{ij}\mathbf{G}_{ij}\mathbf{D}_{ij}\mathbf{E}_{ij}\mathbf{P}_{ij}\mathbf{T}_{ij}\mathbf{F}_{ij}\mathbf{S}_{v}(l,m)e^{-i2\pi(uijl+vijm)}dldm + \underline{A}_{ij}$ 

Vectors		Jones Matrices Hazards						
V isibility = $f(u,v)$	Starting point	Multiplicative baseline error						
<u>I</u> mage	Goal	Bandpass response						
A_dditive baseline	error	Generalised electronic gain						
Scalars	Methods	Dterm (pol. leakage)						
S (manning $I$ to o	hserver	<b>E</b> (antenna voltage pattern)						
polarization)		Parallactic angle						
<i>l,m</i> image plane co	pords	Tropospheric effects						
<i>u,v</i> Fourier plane c <i>i,j</i> telescope pair	cords	Faraday rotation						

#### Visibility data: Measurement Set format

(Edits are stored here first; backup tables can be made and used to modify)

- Unix-like directory structure with binary data and ascii metadata files arranged in subdirectories
- Additional tables in MS and free-standing:
  - Admin: Antenna, Source etc.
  - Processing: calibration, flags, etc.
- ~interconvertible with FITS; similar image format

#### Measurement Set MAIN table

•					🗌 Table	Browser							$\Box \times \Box$
<u>F</u> ile <u>E</u> dit <u>V</u> iew <u>T</u> ools E <u>x</u> port <u>H</u> elp													
3C277.1C.ms								8					
data		UVW 😽	FLAG	WEIGHT	ANTENNA1	ANTENNA2	EXPOSURE	FIELD_ID	Т	IME		DATA	
ble o	53	[-131860, -138051, 85180.9]	[4, 1	[52, 5	1	5	7.99	0	1995-04-15	5-17:14:22.00 [4, 1] Complex			
đ	68	[-131776, -138090, 85247.1]	[4, 1	[52, 5	1	5	7.99	0	1995-04-15	-17:14			
ds	83	[-131692, -138129, 85313.3]	[4, 1	[52, 5	1	5	7.99	0	1995-04-15	-1-14-38.00 [4, 1] Complex			
wor	98	[-131609, -138168, 85379.5]	[4, 1	[52, 5	1	5	7.99	0	1995-04-1	3C277.1C.ms[53, 21] =			:
key	113	[-131525, -138207, 85445.6]	[4, 1	[52, 5	1	5	7.99	0	1995-04-1	Complex Array of size [ 4 ]			
able	128	[-131441, -138246, 85511.7]	[4, 1	[52, 5	1	5	7.99	0	1995-04-1	0			
-	143	[-131357, -138285, 85577.7]	[4, 1	[52, 5	1	5	7.99	0	1995-04-1	0 (-0.16		379 -2 6361	3)
rds	158	[.131273 .138323 856/13 7]	[/ 1	[52 5	1	5	7 99	0	1005-07-1		(-0.104	575,-2.0501	
ywo	Restore Columns Resize Headers								1	1 (0.446854,0.111045)		5)	
PAGE NAVIGATION First << [1/211] >> Last 1 Go							2 (-0.0716612,0.223381)		381)				
								3 (-2.49088,-0.869153)		3)			
										-			

- Some of the columns per visibility measurement

   Correlated amp & phase per baseline per integration
- Data: Complex value per spectral channel for each polarization (XX YY XY YX)





# Time jargon

Total integration time = 456357 seconds Observed from <u>15-Apr-1995/17:13:58.0</u> to <u>20-Apr-1995</u> (UTC) Timerange (UTC) Scan FldId FieldName nVis Int(s) 17:13:58.0 - 17:28:38.0 0 3C286 1665 7.99 17:29:38.0 - 18:29:30.0 1 OQ208 6750 7.99 2

17:07:38.0 - 17:09:54.0	8	10 1300+580	270	7.99
17:10:37.0 - 17:17:49.0	9	11 3C277.1	825	7.99
17:18:36.0 - 17:19:56.0	10	10 1300+580	165	7.99
17:20:35.0 - 17:27:55.0	11	11 3C277.1	840	7.99
17:28:42.0 - 17:29:54.0	12	10 1300+580	150	7.99

- Time on all sources
  - Span of observations (might be gaps)
- Flux scale/polarisation calibration scans
- .99 Alternate phaseref/target scans
  - Single integration time

- Estimate hour angle coverage
- An integration is the shortest averaging time in correlated data
- A scan is usually the time between source changes

 The phase-ref/target cycle should be less than the atmospheric coherence time

#### Polarization jargon: Rx feeds CIRCULAR **ALMA** LINEAR feeds feeds Correlations Left/Right/cross XX, YY, XY, YX correlations Stokes Q =LL RR LR RL (XX - YY)/2Stokes V =Stokes U =(RR-LL)/2(XY - YX)/2Stokes V =Stokes Q =(XY - YX)/2i(RL + LR)/2Polarized intensity P Stokes U = $= \sqrt{(Q^2 + U^2 + V^2)}$ (RL - LR)/2iPolarization angle $\chi$ $= \frac{1}{2} \operatorname{atan2}(U/Q)$

Diagrams thanks to Wikipaedia

### Brightness temperature

- Brightness temperature  $T_{\rm b} = S_{\rm source} \ 10^{-26} \ \lambda^2$  /  $2k_{\rm B} \ \Omega$ 
  - S (Jy) in single dish beam area  $\Omega_{SD}$  (sr) at  $\lambda(m)$ 
    - Resoved by SD?  $\Omega = \Omega_{\text{SD}}$
    - Unresolved?  $\Omega$  = estimated true (smaller) source size
- Predict ALMA flux density per synthesized beam  $\theta_{b}$

$$-S_{\text{ALMA}} = T_{\text{b}} 2k_{\text{B}} \Omega_{\text{ALMA}} / 10^{-26} \lambda^2$$

- Now  $\Omega_{ALMA} = \theta_b^2$
- Use Sensitivity Calculator
  - At least  $5\sigma_{rms}$  on peak and  $3\sigma_{rms}$  on any extended details
- Check ALMA maximum spatial scale
  - Use **OST** or **CASA** simdata to check imaging fidelity

### HL Tau on arcmin-arcsec scales



#### • $T_{\rm b} = [(S/Jy)10^{26} (\lambda/m)^2] \div [2 k_{\rm B} \Omega/{\rm Sr}]$

– Area  $\Omega$  is *smaller* of (actual size) or (beam size)

• Smooth 5mJy in whole 120" would be  $\sim 1\mu$ Jy/1."5 beam

#### HL Tau on sub-arcsec scales



- D-array lowest contour 0.3 mJy in 1500-mas beam – Peak~3 mJy in ~200 mas diameter  $\equiv$  0.18 mJy in 50-mas
- A-array lowest contour 0.15 mJy in 50-mas beam
  - Missing *smooth, extended* bright flux: missing spacings
  - Missing *sub-asec* flux: small beam  $\Rightarrow$  higher  $T_{b}$  threshold

#### Solution: include ACA (also TP)



# Cleaning

Fourier transform the visibilities and the uv tracks

(m) /



# Cleaning

- Fourier transform the visibilities and the *uv* tracks
- Set a mask to include obvious emission

36"

48''

00''





- CLEAN algorithm identifies brightest pixels
- Store e.g. 10% of each peak as Clean Component

# Cleaning

 Iteratively subtract scaled dirty beam at positions of bright pixels



### **CLEANed** image

• Improved signal-to-noise in final image



Residual is just noise
 Note different flux scale



# **CLEANed** image

• Note improved signal-to-noise in image



- NB if snapshot, extended array, narrow channels....
  - Sparse *uv* coverage can limit dynamic range

 Final image is combination of residual and Clean Components convolved with restoring beam



# Cleaning and the uv plane

#### NGC 3256 model coloured by baseline over black data



- *uv* model (colour) is FT of Clean Components
  - 'Major Cycles' subtract model from uv data and remake dirty residual image
- Compare model with data to assess quality
  - Use for further rounds of self-calibration

# Weighting

- Each visibility has a weight:
  - Intrinsic, for same  $t_{int}$ ,  $T_{sys}$  etc.:
    - ACA baseline has noise  $12^2/7^2 \times 12$ -m baseline
    - Single 12-m TP dish has noise  $\sqrt{2}~\times$  12-m baseline
  - Different N<sub>samples</sub> per averaged integration/channel
  - Variance of calibration solutions
- Weights can be adjusted further during imaging
  - Grid samples in uv plane
    - Natural: Original samples per cell (empty between)
      - Maximum sensitivity to extended structure
    - Uniform: Extrapolate uniformly
      - Finest resolution, worse noise
    - Intermediate (robust parameter)
  - Change resolution  $\leq 2x$  at cost of higher noise

# Weighting

- Natural:
  - 110-mas resolution,
     3σ 51
     μJy/bm



Uniform: – 80-mas resolution, 3σ 63 μJy/bm

HL Tau Greaves+'07

- Weights can be adjusted further during imaging
  - Grid samples in uv plane
    - Natural: Original samples per cell (empty between)
      - Maximum sensitivity to extended structure
    - Uniform: Extrapolate uniformly
      - Finest resolution, worse noise
    - Intermediate (robust parameter)
  - Change resolution  $\leq 2x$  at cost of higher noise

# Simulating interferometry data

- CASA tasks
  - simobserve, simanalyse
    - Any array if antenna configs provided
    - Detailed parameters
  - simalma
    - Tailored for ALMA
- Observing Support Tool
  - Based on CASA library, results should be same
  - Web interface, limited inputs
    - Less flexible but easier to use
- Why simulate?
  - Effects of interferometer sampling large structures
    - Dynamic range limitations
  - Mosaicing
  - **But** check predicted noise with sensitivity calculator

# Input for simulations

- See http://almaost.jb.man.ac.uk/help/
  - FITS image
    - Required keywords (script available to check):
      - BUNIT, CDELTn, CROTAn, CDn\_n, CTYPEn, NAXIS, NAXISn
  - Declination
    - Very high/low Dec:
      - Elongated synthesised beam
      - Shadowing





# Input for simulations

- Bandwidth, frequency etc.
  - Line: OST handles a single channel only
  - Continuum: OST can adopt optimum place in band
    - NB bands 3,4,6,7,8 full b/w gap between sidebands







- Automatically mosaics if required by input size
   Crep large input if you only need a single pointing
  - Crop large input if you only need a single pointing!
- Resolution: Cycle 2, select array(s) directly
- Peak  $\mu$ /m/Jy/pixel (to rescale input)
- Time needed to reach sensitivity
- Add noise
  - OST does not simulate phase/amp correction!

#### Cycle 2 resolution (scales @100 GHz)



### Cycle 2 examples (scales @100 GHz)

- Data for each array supplied <sup>30</sup> separately by OST <sup>20</sup>
  - Adjust weights when combining arrays
  - Further modify resolution by chosing degree of uniform/natural weighting in imaging
- No unique map
  - Vary combinations to emphasize regions of interest
  - Higher resolution can mean <sup>20</sup> higher noise as well as <sup>30</sup> resolving-out extended <sup>40</sup> structure <sup>30</sup>



#### Structure scales

- JCMT single-dish mosaic of source at 11 kpc
  - 7".5 pixels
  - Field of view 150"
  - Peak 100 Jy/ 7".5 pixel
  - -354 GHz =  $\lambda$  0.85 mm



#### Structure scales

- JCMT source at 11 kpc
   Peak 100 Jy/ 7".5 pixel
  - -354 GHz =  $\lambda$  0.85 mm
- ALMA field of view
  - 1.2 x λ / 12 ≈ 18<sup>1</sup>
    - 12-m dish primary beam
- ALMA synthesized beam
  - $\lambda$  / longest baseline  $~\bullet$ 
    - Compact array: 1"
    - Intermediate: 0".45
- Largest spatial scale
  - $\lambda$  / shortest baseline
    - Compact array λ/14≈7.6"
    - Intermediate  $\lambda/21 \approx 5.2$ "



# ALMA observations at 11 kpc

- Source original size 150"
   ALMA mosaic
- Peak S<sub>JCMT</sub> 100 Jy/pixel
- ALMA compact config
  - Synthesised beam  $\theta_{bc}$  1"
    - Expect peak 100 (1/7.5)<sup>2</sup> = 1.8 Jy/beam?
  - Largest angular scale 7.6"
    - ~Input pixel!
- Flux which is *smooth* on JCMT scales is ~invisible!
  - Standard ALMA simulation fails



# ALMA observations at 11 kpc

- Source original size 150"
   ALMA mosaic
- Source original peak 100 Jy ALMA compact config
  - Synthesised beam  $\theta_{bc}\mathbf{1}^{\prime\prime}$ 
    - Expect peak 100 (1/7.5)<sup>2</sup> = 1.7 Jy/beam?
  - Largest angular scale 7.6"
    - ~Input pixel!
- Flux which is *smooth* on JCMT scales is ~invisible!
- Small-scale details may appear
  - But only if you have added them to the model!



### *d*=55 kpc

- JCMT field 30", distance d = 55 kpc
  - Pixel p = 7".5x 11/d = 1".5
  - $-S_{\text{JCMT}} 100 \times (11/d)^2 = 4 \text{ Jy/pix}$
- ALMA compact  $\theta_{bc} = 1''$ 
  - 7 mosaic pointings
  - $-S_{ALMA} = S_{JCMT} \times (\theta_{bc}/p)^2 \sim 1.8 \text{ Jy/bm}?$ 
    - Actual peak ~ 0.4 Jy/beam
    - Large scale flux still missing





### *d*=55 kpc

- JCMT field 30", distance d = 55 kpc
  - Pixel p = 7".5x 11/d = 1".5
  - $-S_{\text{JCMT}} 100 \times (11/d)^2 = 4 \text{ Jy/pix}$
- ALMA compact  $\theta_{bc} = 1''$ 
  - 7 mosaic pointings

$$- S_{ALMA} = S_{JCMT} \times (\theta_{bc} / p)^2 \sim 1.8 \text{ Jy/bm}?$$







#### d=440 kpc

• JCMT field 30", distance d = 440 kpc

- Pixel 
$$p = 7$$
".5x 11/d = 0".1875

- Stot<sub>JCMT</sub> ~ 2.2 Jy





- ALMA intermediate  $\theta_{bi} = 0.45''$ 
  - Total model ~ largest angular size 5".2
    - Well within field of view
- ALMA recovers all 2.2 Jy
- e.g. use Galactic single dish YSO model, for SFR in nearby galaxy seen with ALMA

# Noise

- Input is noiseless model?
  - Select PWV appropriate for observing band
- Input has smooth noise  $\sigma_{in}$ ?
  - e.g. well-calibrated single-dish/optical etc. image
  - Estimate likely ALMA noise  $\sigma_A$  (sensitivity calculator)
  - Reduce added noise so that  $\sigma_{added}{}^2$  +  $\sigma_{in}{}^2$   $\,\sim\,\sigma_{A}{}^2$
- Input is interferometry image?
  - Beware re-sampling a poorly-sampled image!



# In conclusion...

- Decide what you want to observe science goal!
  - What frequency (and channel width, for lines)?
  - What angular resolution?
  - Largest smooth angular scale within source
    - OT will advise if you need to combine arrays
  - Field of view will you need a mosaic?
  - What flux density per ALMA synthesised beam?
    - Detection experiments  $\geq 5\sigma_{rms}$  noise
      - Sensitivity calculator/OT roughly reasonable time?
- Find an input FITS model
  - Image at another wavelength, theoretical model...
  - Rescale size, brightness as required
    - Details on similar scales as you hope ALMA will see
  - Read the OST Help and simulate!

# What ALMA data do you get?



Image cubes for principal science target channels

Science products + info always delivered to PI

+ Visibility data sufficient to re-do processing in CASA subject to what was available when observations were taken.

All ASDM & FITS images available from Archive



Information and processing summary Data processing scripts



+ any or all of: ASDM (one per EB)





Flag tables

**Calibration tables** 



Calibrated MS

# ALMA data conventions

- Scheduling Block: self-contained observation series
  - Short pointing, flux scale, bandpass, (pol.) cal scans
  - ~20-30 mins alternating between target(s)/ph ref(s)
    - Including multiple mosaic pointings
  - Repeat Execution until desired sensitivity is reached
    - All in same spectral and array configuration
    - Each EB produces one ASDM (ALMA Science Data Model) with binary data and lots of metadata
- Initial data processing (calibration, editing) per-EB
   Convert ASDM to Measurement Set
  - Combine EBc for final target imagine
- Combine EBs for final target imaging
- May also combine different SBs e.g. ACA+main

#### Data organisation for a project



### Individual scheduling block



#### Data reduction summary

- Initial steps common to most data sets
   Standard procedures usually reliable
- Likely to want to self-calibrate

Re-make images at different resolutions etc.

