# The Observed Mass Function of Young Star Clusters 

Søren S. Larsen

Astronomical Institute, Utrecht University

## What is the ICMF?

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Not very practical:What does "at birth" mean?

## What is the ICMF?

Better:
ICMF = Mean birth rate vs. cluster mass:

$$
\psi(M) \hat{=} \frac{d^{2} N}{d M d \tau}
$$

For large $M\left(>10^{5}-10^{6} M_{\odot}\right)$, birth rate is
typically << $\mathrm{Myr}^{-1}$, even in large galaxies.

## Observational difficulties

- High masses:
- Low birth rates $\rightarrow$ rare, poor statistics
- Low masses:
- Clusters faint, short-lived
- Integrated properties subject to stochastic IMF sampling
- Masses are observationally expensive to measure (virial masses prohibitive for large samples)


## Stochastic IMF sampling

Mean number of supergiants vs age


Stochastic IMF sampling becomes very important below $M \sim 10^{4} M_{\odot}$.
(Barbaro \& Bertelli 1977;
Girardi et al. I995;
Bruzual 2002;
Cerviño \& Luridiana 2004,2006; Maíz-Apellániz 2009;
Piskunov et al. 2009;
Fouesneau \& Lançon 2010; Popescu \& Hanson 2010; Silva-Villa \& Larsen 2011)

## Luminosity vs. mass for stochastic IMF sampling



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## Colours of Galactic open clusters



Dots: observed colours<br>Blue curve: stochastically sampled models<br>Red curve: classical SSP model

Piskunov et al. 2009

## Ages and masses: stochastic effects

Ages



Input

Masses


Bayesian approach

Classical SSP models

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- Use weights based on effect of stochasticity in different bands (Maíz-Apellaniz 2009)
- Reject clusters with poor fits (Fouesneau \& Lançon 2010)
- Generate full model grid of stochastic clusters and search for best fit (Popescu \& Hanson 2010; Fouesneau \& Lançon 2010)


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- Also affect cluster detection via biased size measurements (Silva Villa \& Larsen 201 I)


## NGC 4038/4039, The Antennae



## The CMF of clusters in The Antennae



$$
\begin{aligned}
& \frac{d N}{d M} \propto M^{-2} \\
& \quad ; M>10^{4} M_{\odot}
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Zhang \& Fall 1999

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(note: most massive bins all somewhat below fit)

Zhang \& Fall 1999

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## Shape of the ICMF

- Several studies: $\mathrm{dN} / \mathrm{dM} \sim \mathrm{M}^{-2}$, over some mass range:
- Milky Way open and embedded clusters
(Elmegreen \& Efremov 1997; Lada \& Lada 2003; Selman \& Melnick 2008); $\quad \log M / M_{\odot} \approx 3$
- Large Magellanic Cloud
(Hunter et al. 2003; de Grijs \& Anders 2006; Chandar et al. 2010);
- M5I (Bik et al. 2002; Chandar et al. 201 I);
$3 \leq \log M / M_{\odot} \leqslant 5$
- Antennae (Zhang \& Fall 2005; Fall et al.2009):
$3 \leqslant \log M / M_{\odot} \leqslant 5$
- Several spirals + irr (Dowell et al. 2008)*: dN/dM ~ $M^{-1.8}$ for $4 \leqslant \log M / M_{\odot}$
- Starbursts: NGC 6745*/NGC 3310 (de Grijs et al. 2003): $5 \leqslant \log M / M_{\odot}$
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## ICMF is universal: $\frac{d N}{d M} \propto M^{-2}$

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True or False?


## Luminosity functions: slope vs. Mv



Figure 1. Sample of published indices of power law fit results to LFs of young star clusters as a function of the fit range. The results are taken from: Larsen (2002): six spirals and the LMC; Mora et al. (2007): NGC 45; Gieles et al. (2006b); Haas et al. (2008) and Hwang \& Lee (2008): M51; Whitmore et al. (1999): Antennae; Dolphin \& Kennicutt (2002): NGC 3627.

Gieles (2009)

## Insight from LFs

- LFs invariably steeper than $\mathrm{dN} / \mathrm{dL} \sim \mathrm{L}^{-2}$
- Inconsistent with $\mathrm{dN} / \mathrm{dM} \sim \mathrm{M}^{-2}$ for all M
- Only way to get steep LFs is if ICMF is steeper, too and/or truncated
- MFs possibly truncated at several $10^{5} \mathrm{M}_{\odot}$ (Gieles et al. 2006a,b)


## Two of the cluster-richest, nearby spirals



## Clusters in the Antennae and NGC6946+M83




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## N5236-FI-I: I. $7 \times 10^{5} \mathrm{M}_{\odot}$

NI3I3-F3-I: $2.8 \times 10^{5} \mathrm{M}_{\odot}$


HST/ACS images - note resolution into individual stars!

## CMFs in the Antennae and NGC6946+M83

 $d N / d M \sim M^{-2}$ ?

Larsen (2009)

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Best fits:

$$
\begin{aligned}
& \frac{d N}{d M} \propto M^{-2} \exp \left(-\frac{M}{M^{*}}\right) \\
& M^{*}=2 \times 10^{5} \mathrm{M}_{\odot} \text { (spirals) } \\
& \mathrm{M}^{*} \sim 2 \times 10^{6} \mathrm{M}_{\odot} \text { (Antennae; } \\
& \text { Jordán et al. 2007) }
\end{aligned}
$$

## More MFs

## Spirals:

Generally consistent with $M^{*}=2 \times 10^{5} M_{\odot}$ Schechter fct.

## Antennae:

Cut-off at higher mass (>106 $\mathrm{M}_{\odot}$ )


Portegies Zwart, McMillan, Gieles 2010,ARA\&A

## LF of young clusters in M5I


$d N / d L \sim L^{-2} ?$ Poor fit

LF based on Schechter MF with $M^{*}=2 \times 10^{5} M_{\odot}$ ?

OK fit, if there is some disruption.

## The Most Massive YMCs

Clusters with $\mathrm{M} \sim 10^{7}$ $M_{\odot}$ in starbursts $\rightarrow$ ICMF more top-heavy than in spiral discs


Arp 220 - most massive clusters $\sim 10^{7} \mathrm{M}_{\odot}$, $R_{\text {eff }} \sim 10$ pc (Wilson et al. 2006).

NGC $7252-\mathrm{W} 3: \mathrm{Mvir}_{\text {vir }}=(8 \pm 2) \times 10^{7} \mathrm{M}_{\odot}$,
$R_{\text {eff }} \sim 18 \mathrm{pc}$ (Maraston et al. 2004)


## Small samples: hard to tell the difference

Large Magellanic Cloud:


Consistent with $\alpha=-2$ power-law? YES ( $\mathrm{P}=0.56$ )

Consistent with $M^{*}=2 \times 10^{5}$ $M_{\odot}$ Schechter fct?
YES ( $\mathrm{P}=0.94$ )

## M83 (WFC3 early release)



# ICMF upper cut-off consistent with other constraints? 

## Upper ICMF limit $\rightarrow$ Brighter Clusters Should be Younger



Gieles et al. (2006)

## Brighter clusters are younger



Larsen (2009)

## Size-of-sample effects



## Brightest clusters: size-of-sample effects



Bastian (2008)

## The $L_{\max }$ vs. SFR relation for Schechter MFs



Larsen (2010)

Filled circles: spirals
Triangles: starbursts/ mergers

N assumed to scale with SFR

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- Luminosity functions (too steep)
- Direct MF determinations
- $L_{\text {max }}$ vs. SFR (or $N$ ) relation ("size-of-sample effect")
- Mean $L_{\text {max }}$ vs. age trend (brighter clusters younger)


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- But a Schechter fct with $M^{*} \sim 200,000 M_{\odot}$ fits well
- The ICMF does not appear to be universal. Cut-off at higher masses in starburst/merger environments.
- But: No cluster system has data from the lowest (<102 $M_{\odot}$ ) to the highest ( $>10^{6} M_{\odot}$ ) masses


## Peculiar MF in dwarfs?

(part of) spiral: NGC 6946

Dwarf:
NGC 1705

## Peculiar MF in dwarfs?





