

# ~~Detection of extrasolar planets~~

**Not a good title for ELT (will be done before)!**

**I will “limit” myself to the  
Possibility of studying terrestrial exoplanets**

**Key words are**

**studying**

**(spectrum, time variability, polarization . . .)**

**and**

**terrestrial**



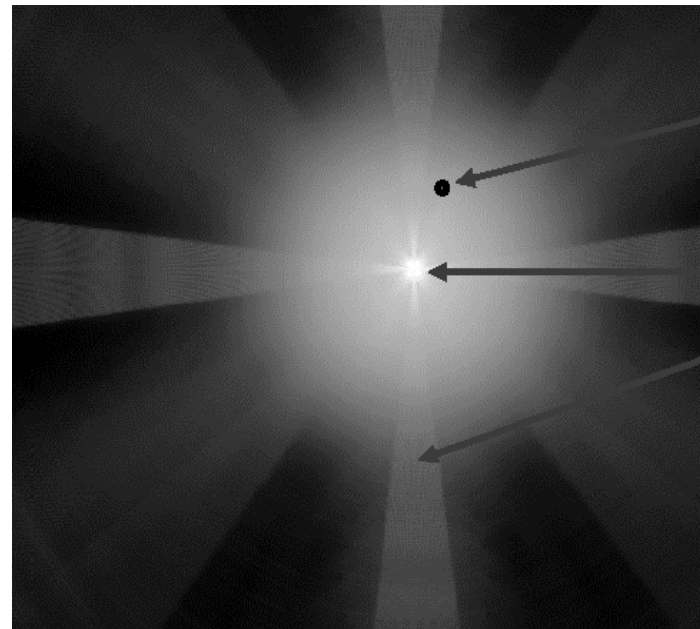
## An OWL reference on the subject:

### *“Critical science with the largest telescopes: science drivers for a 100m ground-based optical-IR telescope”*

T. G. Hawarden, D. Dravins, G.F. Gilmore, R. Gilmozzi, O. Hainaut, K. Kuijken, B. Leibundgut, M.R. Merrifield, D. Queloz & R.F.G. Wyse

Proc. of SPIE Vol. 4840

*“ ...The exo-Jupiter in Fig. 6 is detected [in J] at hundreds of sigma [in 10,000 s] (high resolution spectroscopy of this object could be secured in a night) and the exo-Earth is detected at around 10 sigma (for albedos of 0.7 and 0.4 respectively). While a 30-m will be hard put to detect an earth beyond ~3pc, OWL’s range should be  $\geq 25$  Pc. A year’s observing would allow a census of the 2600-odd stars (including 360 “solar type single F, G, K stars) within this radius, yielding orbital parameters for innumerable planets.”*



#### Model includes:

- AO halo (Strehl = 0.8; Lorentzian, FWHM = 0.4)
- Central diffraction structure
- Pattern from telescope structure rotated during exposure
- (exo-Earth at end of “halo” arrow)

## the logics of this presentation

*First we will see how far Physics allows to go in studying extrasolar earth-like planets.*

**Physics means:** how turbulence induced wavefront *phase* errors, star photon fluxes, wind speed, etc. combine in limiting the **AO PSF contrast**. In practice:

- Assuming reasonably good conditions:  $r_0(V) = 20 \text{ cm}$ ,  $\langle v \rangle = 10 \text{ m/s}$
- We can calculate a PSF with the semi-analytical method of Jolissaint-Veran 2001,
- We can tune up the **actuator density** for good performances in  $< \text{one arcsec}$  field:
- We can calculate a plausible **AO PSF contrast** to see what we could do with it.
- *We will see that the potential for extrasolar research is very good.*

**Initially I will neglect**

- *Scintillation*
- *Speckle-noise*
- *Diffraction effects*
- *Segmentation effects*

**But later** I will briefly discuss  
**some important implications**  
of the initially neglected effects

**At the end** I will  
say what I think  
about *technical*  
*feasibility aspects*

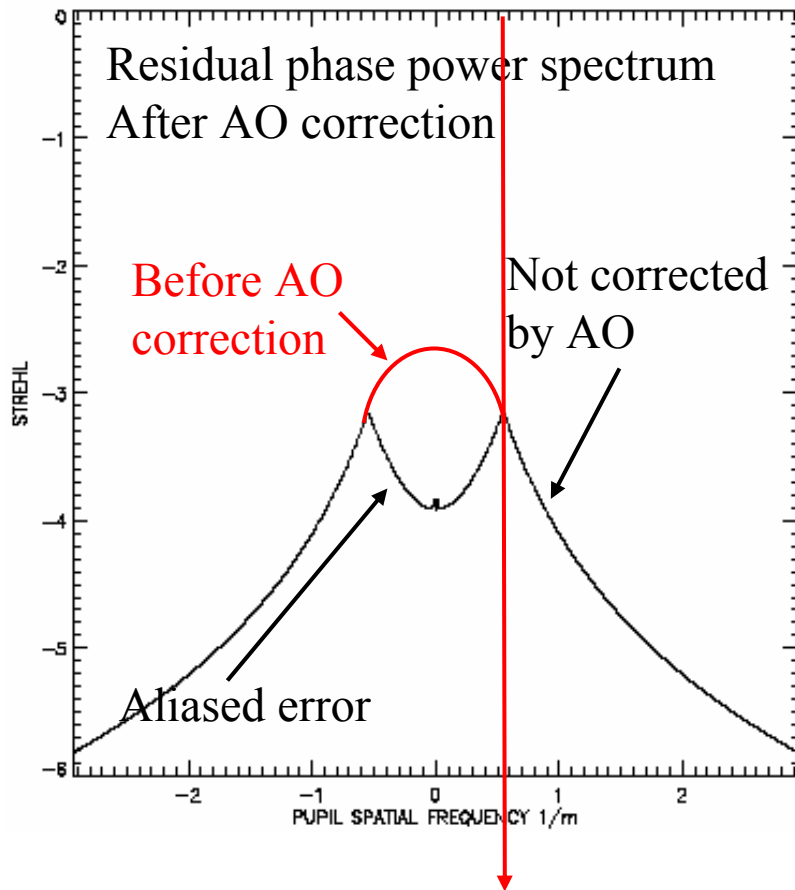
## Scattering of light by Residual Wavefront (phase) Error (RWE)

The RWE, i.e. the “leftovers” of the (phase) AO correction, scatters light around the star *proportionally to the Phase Power Spectral Density of the total RWE* (total includes the effects of “fitting”, “phase lag”, “photon noise”, “aliasing”, etc. errors).

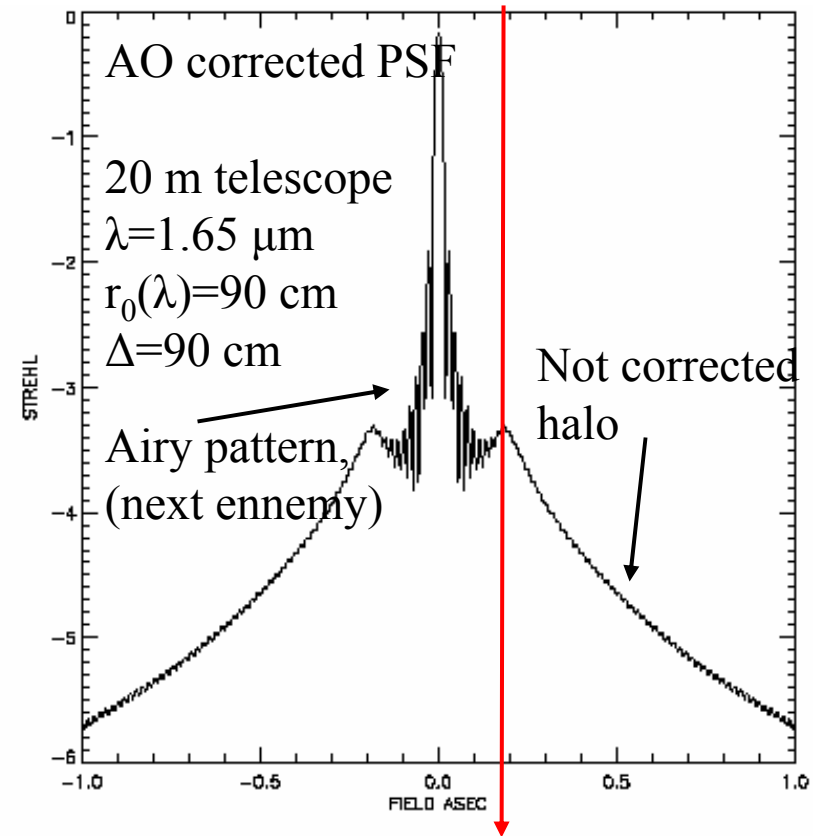
In other words:

- The RWE at spatial wavelength  $W$  scatters light of wavelength  $\lambda$  at an angle  $\alpha = \lambda/W$  at  $\alpha \sim 0.1$  arcsec, in V band  $W \sim 1$  m, in K band  $W \sim 4$  m, **1-4 m scales are critical**
- As with a given actuator separation  $\Delta$  we can correct the wavefront error only at  $W > 2 \Delta$ , there is always a non-corrected part of the RWE spectrum ( $W < 2 \Delta$ ), that produces (by aliasing) further contamination of the corrected part.
- The correction must extend well beyond the spatial frequency of interest ( $W = \lambda/\alpha$ ).  
(In other words:  $\Delta \ll \lambda/2\alpha$ )
- The scattered light intensity  $I$  at angle  $\alpha$  is proportional to the RWE phase variance  $\sigma^2(W)$  at the corresponding  $W$ .  **$I(\alpha) \propto \sigma^2(W) = \sigma^2(\lambda/\alpha)$**

# AO halo shape (adapted from Jolissaint and Veran 2001)



Critical spatial frequency  $f_c = 1/W_c = 1/2 \Delta$

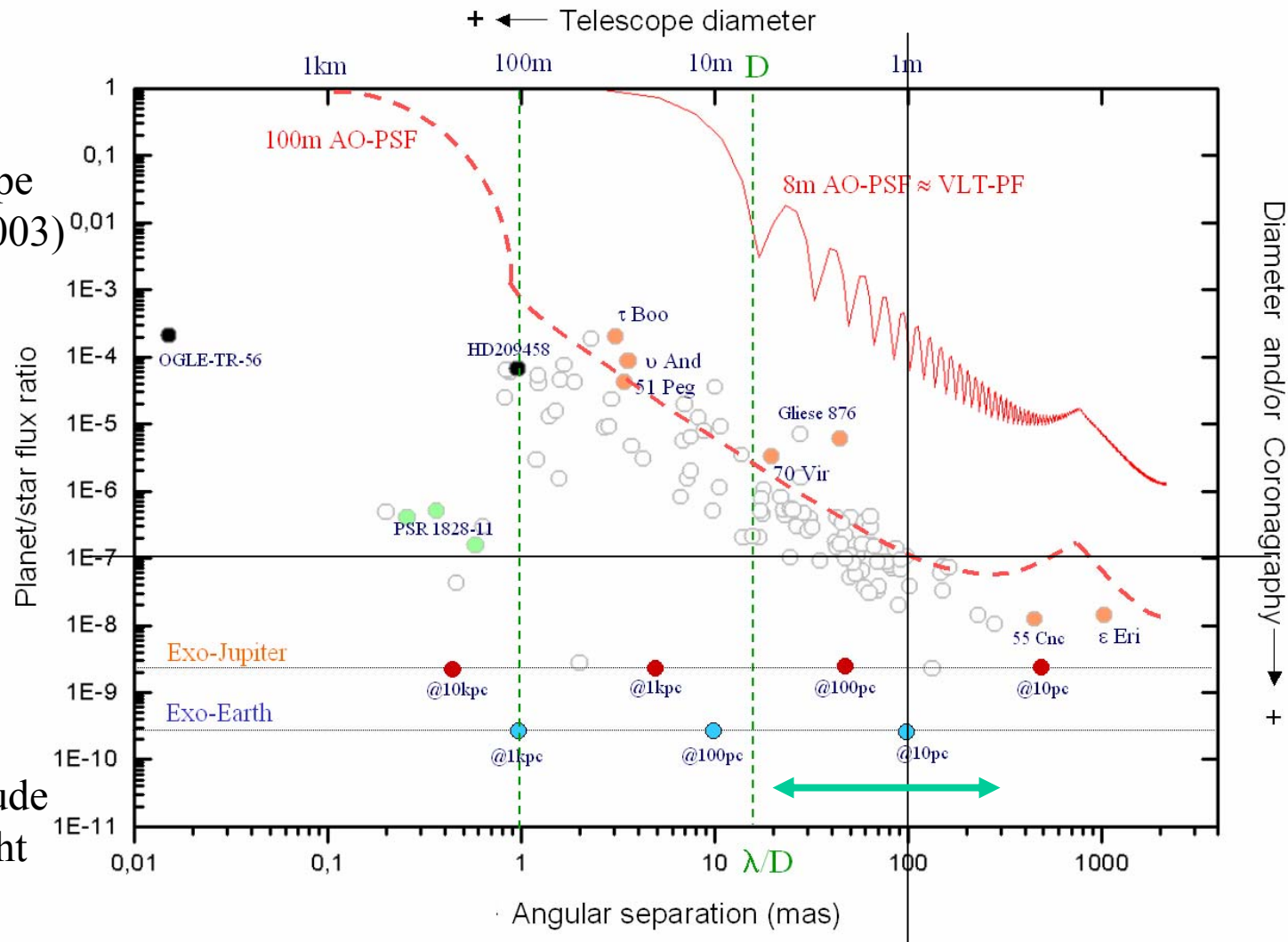


Critical field angle  $\alpha_c = \lambda/W_c = \lambda/2 \Delta$

## Result: V band AO PSF (theoretical contrast)

Planet/star flux ratio and angular separation for known exoplanets compared with telescope PSF (Lardiere et Al. 2003)

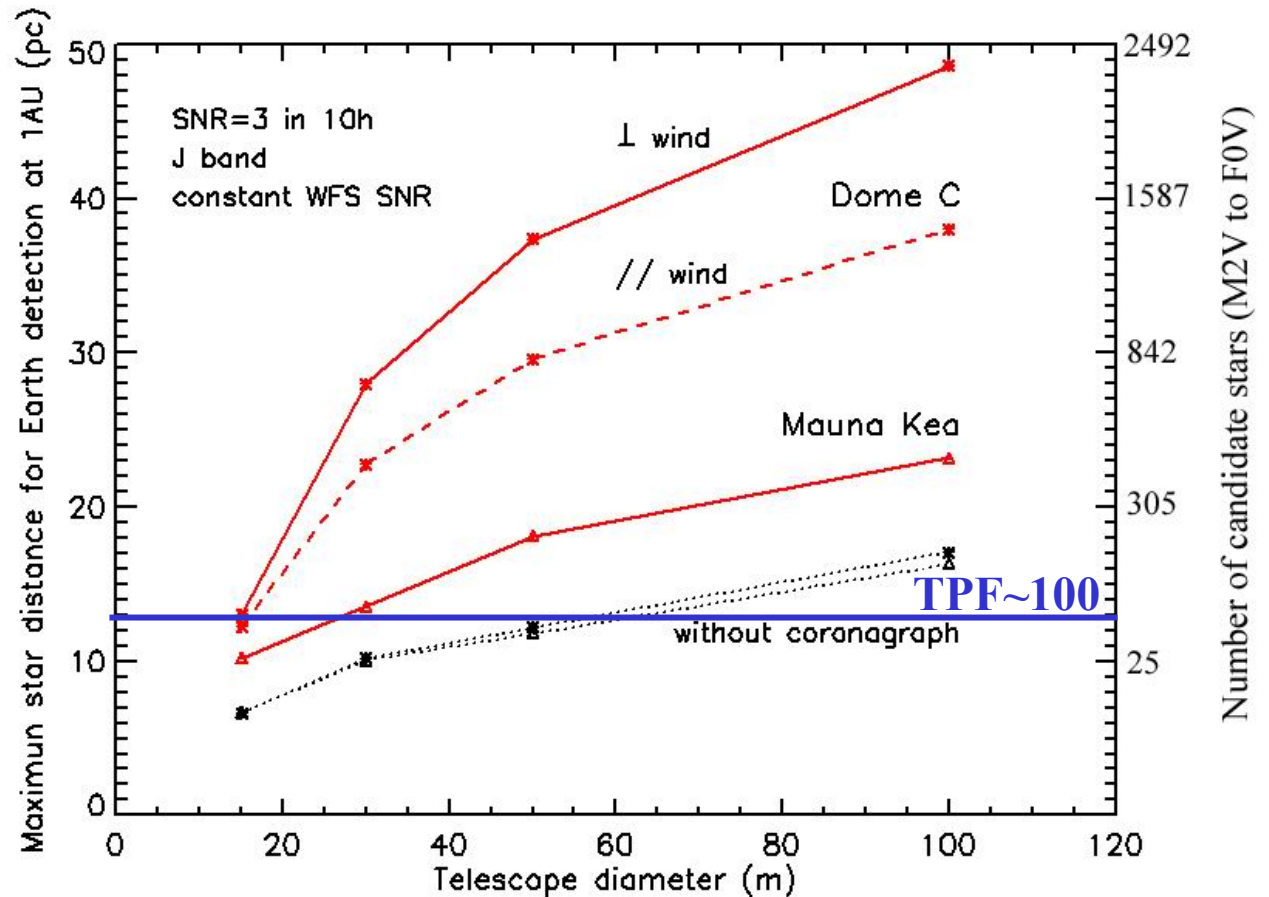
- A)** even a 100 m telescope cannot resolve some of the known planets from their stars.
- B)** A one arcsec field radius includes most known planets
- C)** Exo-earths, at best distance, are about three orders of magnitude below the scattered light background



## Stellar sample size (choose your telescope and location)

With a **~ 30 m** telescope  
(at “Mauna Kea”)  
one **can explore** at short  
wavelength the entire  
**TPF (goal) sample**  
of **~ 100 stars**  
in **1000 hours**

With a **100 m** telescope  
in “Antarctica” one can  
obtain  **$R > 1000$  spectra**  
of the  
**TPF sample**  
at short wavelength  
(R to K)  
in **1000 hours**





# What you can do with different telescope sizes (L) @ “Dome C” (Lardiere et Al. 2003)

Example (see black arrow)

The Sun-Earth system  
At 10 PC

Would be **detected**  
In J filter ( $R_J = 4$ )

**By a 50 m (sq) telescope**  
**with  $2.5 \times 10^5$  actuators**

In ten hours

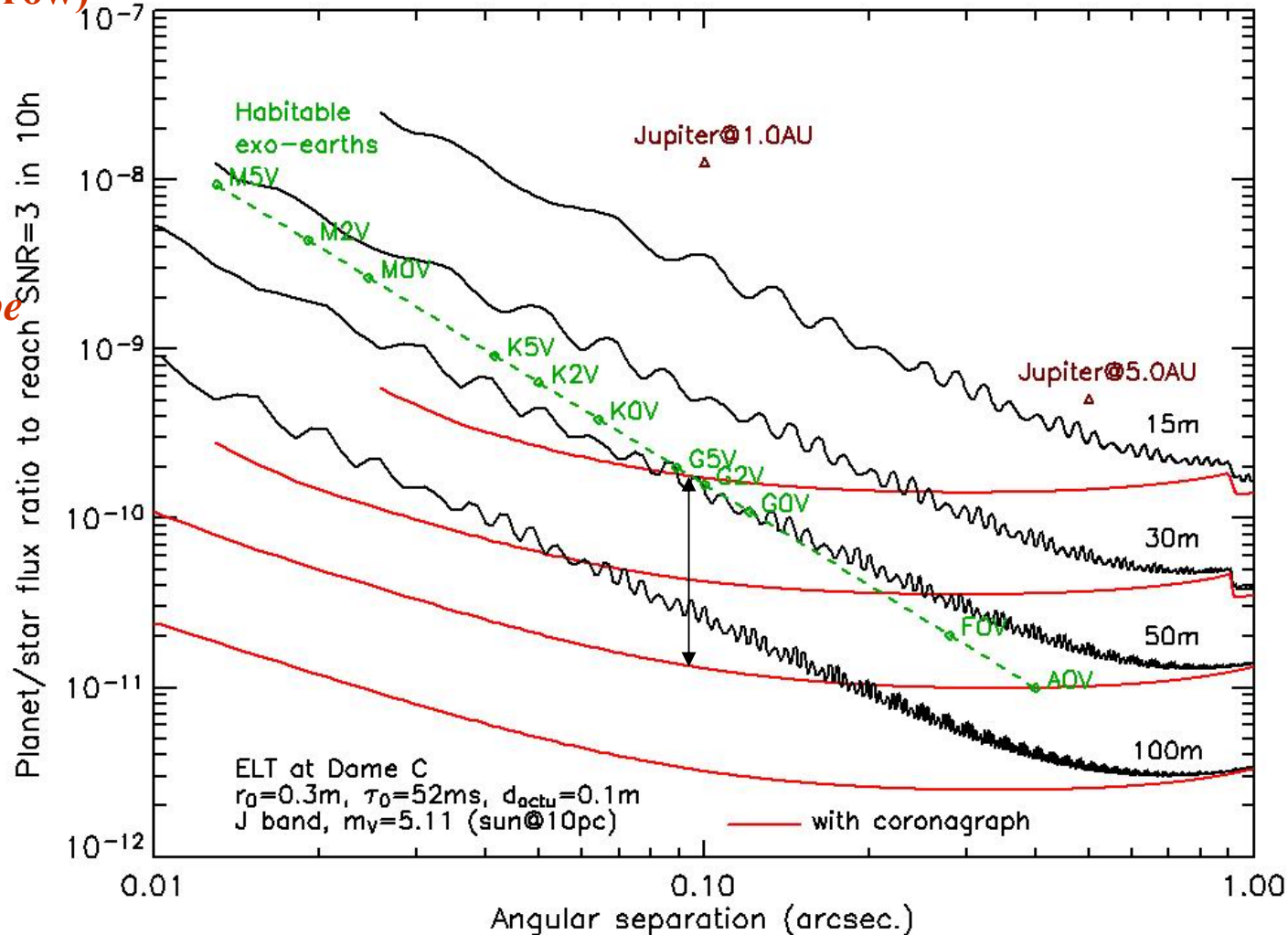
At  $S/N \sim 30$ .

(in 6 min at  $S/N 3$ )

**Spectroscopy** with  
 $S/N \sim 5$  (per sp. el)  
At  $R=144$

$[R = R_J \cdot (30/5)^2]$

Would also require  
About **ten hours**

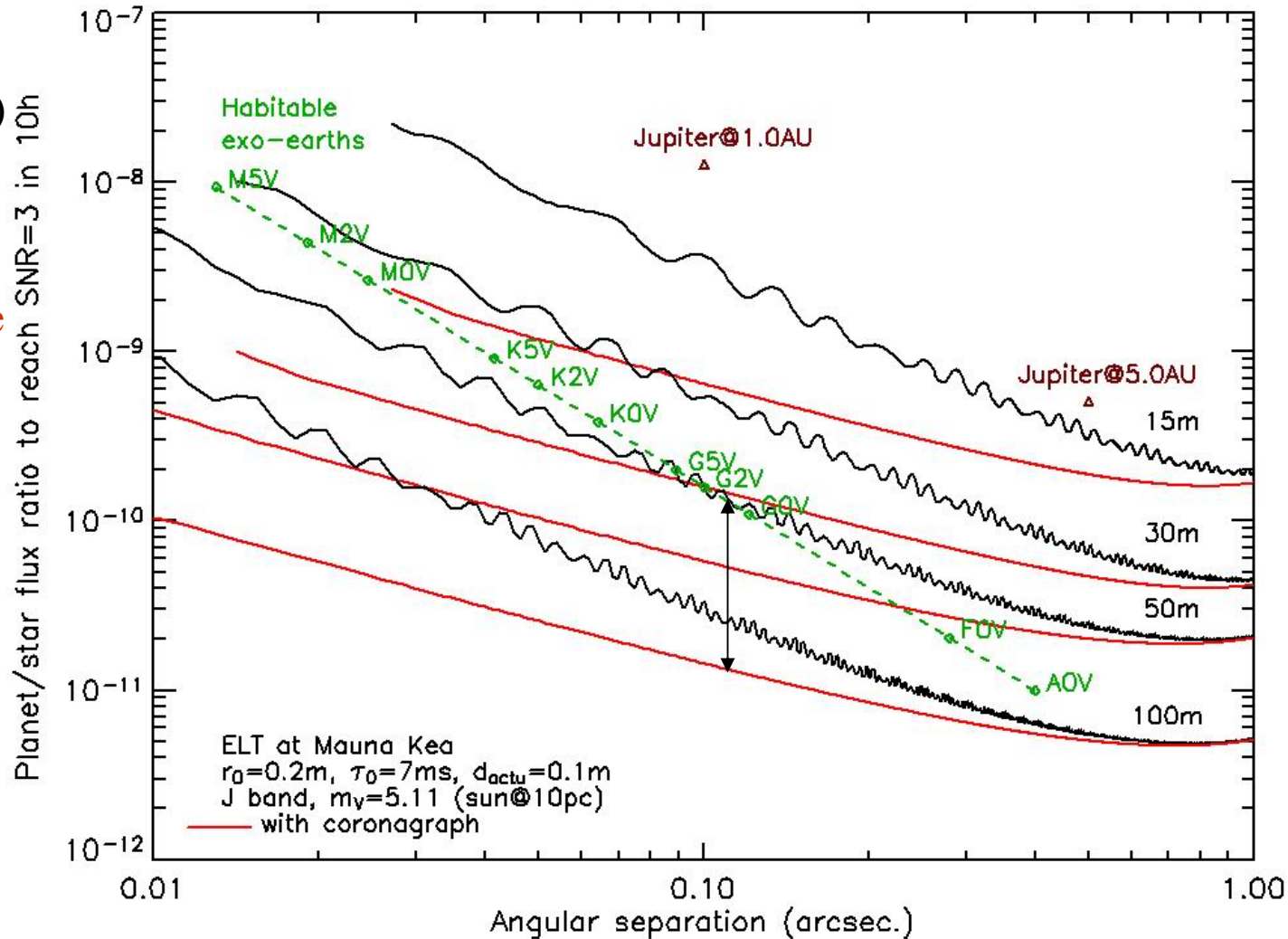




# What you can get with different telescope sizes (L) @ Mauna Kea (Lardiere et Al. 2003)

Same Solar case,  
Same arrow (factor 10)  
Same performances

Now one needs:  
A 100 m (sq) telescope  
with  
 $\sim 10^6$  actuators

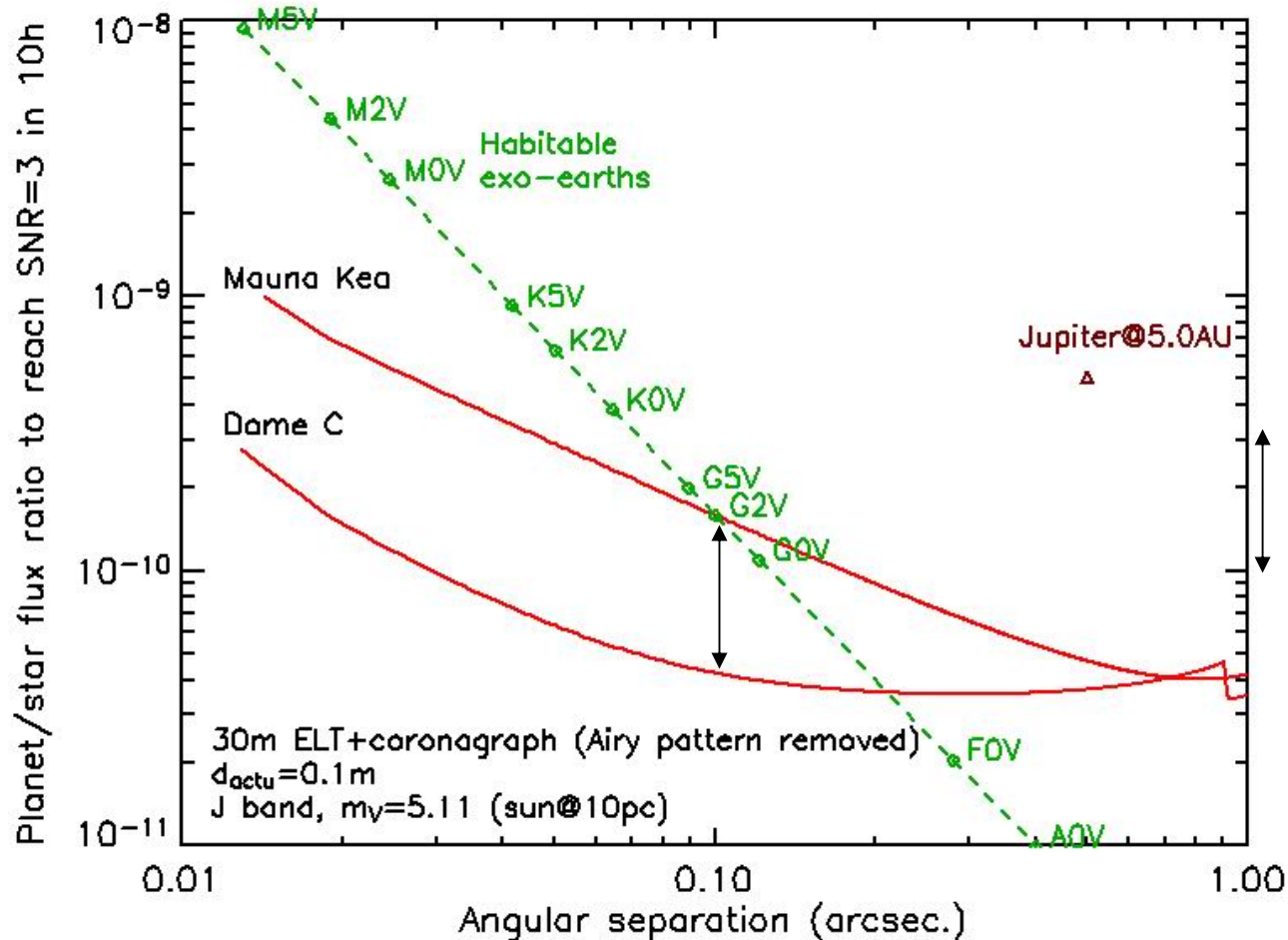


# Which planets the competition could see from the two sites with a 30 m telescope? (Lardiere et Al. 2003)

Not bad!

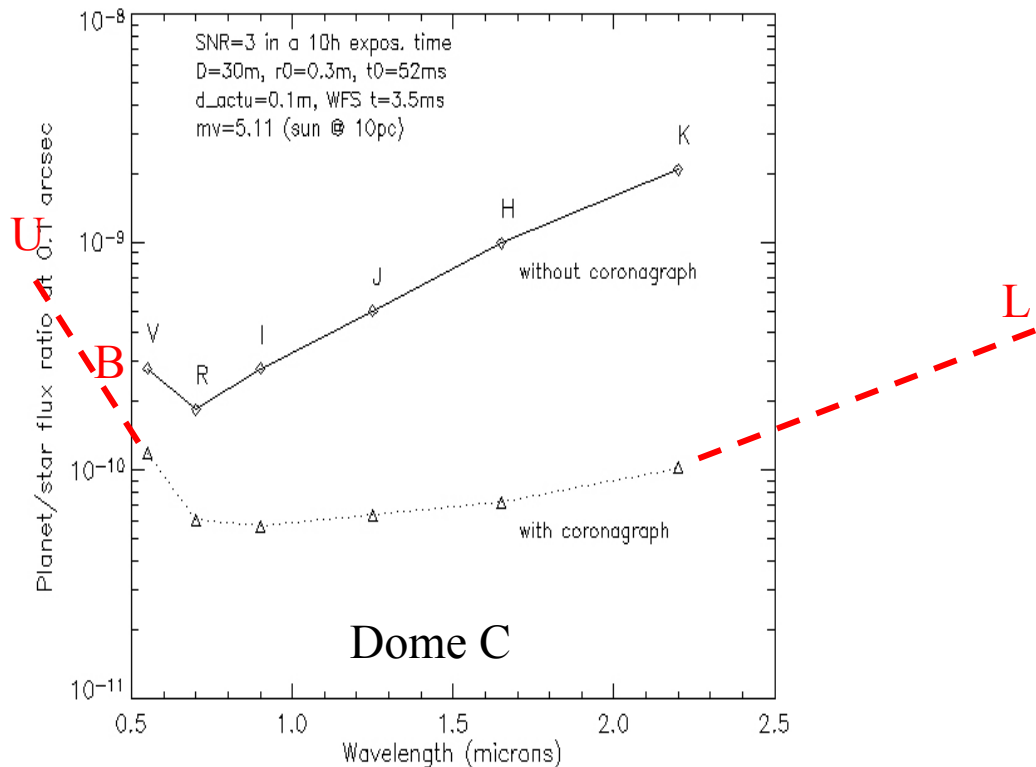
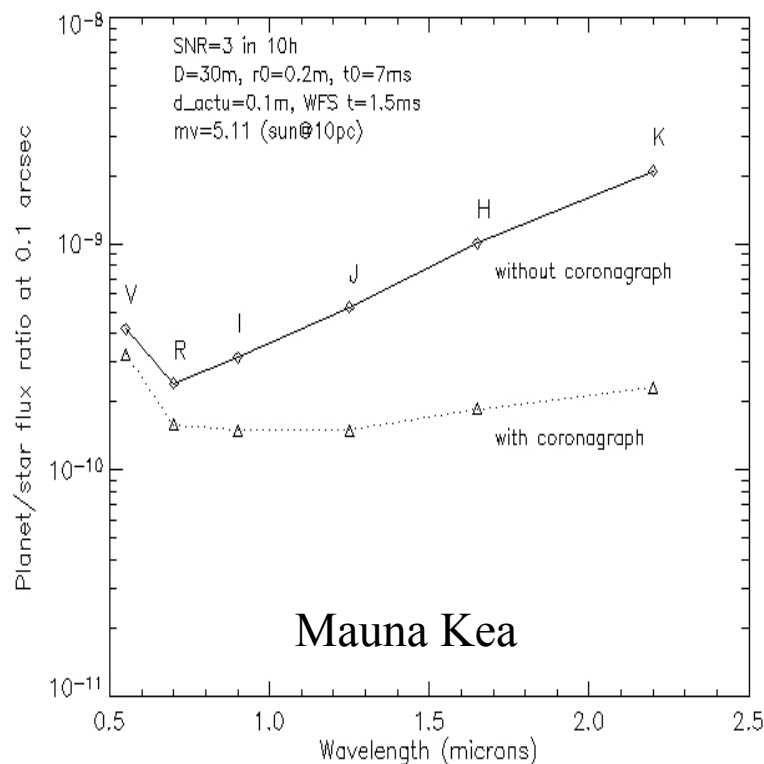
10 hours for an Earth  
at 10 Pc (at  $3\sigma$ )  
from MK,

1 hour from Dome C



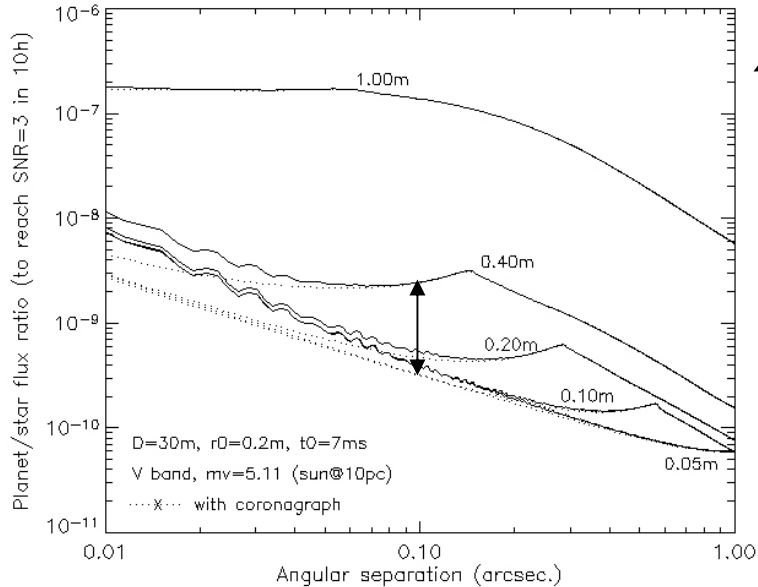
# What happens at other wavelengths? (Lardiere et Al. 2003)

Going to longer wavelengths the increasing  $r_0/\Delta$  compensates the decreasing  $\lambda/D$ .  
**An option for L band at Dome C**, where the thermal background is reduced by  $10^{-3}$ !  
 V is not at all bad, R, I, J are optimum. **B and U should be explored**, could be used for diagnostics of many non-terrestrial planets (or maybe even terrestrial ones. . .)



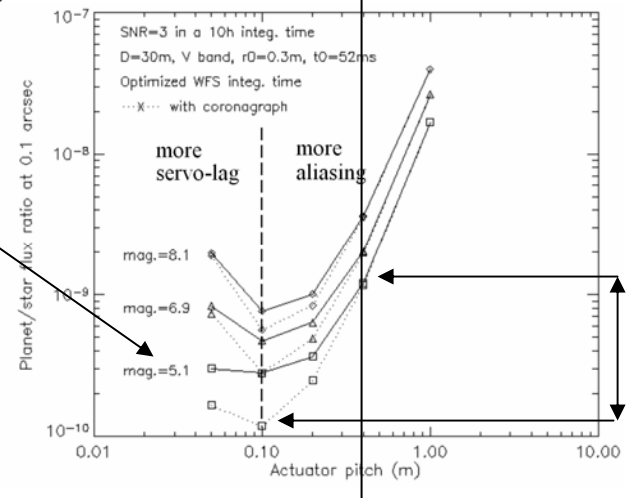
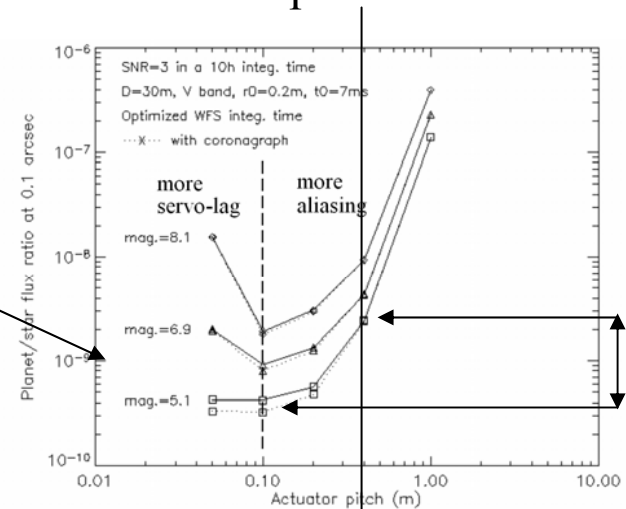
## Some more technicalities (Lardiere et Al. 2003)

Effect of different actuator separation  $\Delta$



Selecting the best  $\Delta$   
For Mauna kea  
(10 cm)

And for Dome C  
(Again, independently  
10 cm)



Going from  $\Delta=10$  cm to  $\Delta=40$ cm  
(adequate for  $S \sim 0.8$  in J) changes the exo-eaths  
detection treshold by one order of magnitude.  
(*detection time by two orders of magnitude*)

## A few words on the neglected AO effects

*The effects on contrast of **intensity fluctuation on the pupil (scintillation)** are similar but much smaller than those of phase “corrugation”.*

Scintillation can be controlled in a Multiconjugate AO System, but at the cost of adding complexity (and some extra residual phase error).

*In the following I assume that scintillation is removed by correcting phase errors in a **MCAO** scheme, **IF NECESSARY** (work is in progress).*

*If there are **slowly varying terms in the residual wf error**, part of the the scattered light will concentrate in **speckles**, making the detection of planets much more difficult.*

*There are ways of avoiding the formation of speckles that allow achieving a Signal to Noise ratio limited by “Poisson” photon noise, although this may require **a COMPLEX “planet finder” instrument.** (see Angel 2002)*

*More work is certainly needed on both above subjects, but **Poisson fluctuations** of the rate of arrival of the photons scattered by residual wavefront phase error **remain the main AO limitation to the study of exoplanets***

# The enemies of Extreme Contrast

Many factors work against the study of terrestrial exoplanets from the ground:

1. **Atmospheric turbulence** (only partially corrected by Adaptive Optics)
2. **Diffraction effects**
  - By pupil outer edge (largely curable by pupil shape choice + coronagraphy)
  - By pupil inner edge (smaller effect, but more difficult to cure.
  - By secondary support structure (spikes only in a few directions)
  - By primary (and other) mirror segmentation (a variety of small, but nasty, effects)
3. **Vibrations of optical components**
4. Non uniform reflectivity (amplitude variations)
5. Scattering by defects, edges, dust . . .

*Only N 1 is specific of groundbased telescopes  
(and is the worst ennemy).*

All the other effects are *in principle* tractable by

- appropriate telescope design choices
- coronagraphic techniques
- severe tolerancing



## diffraction effects

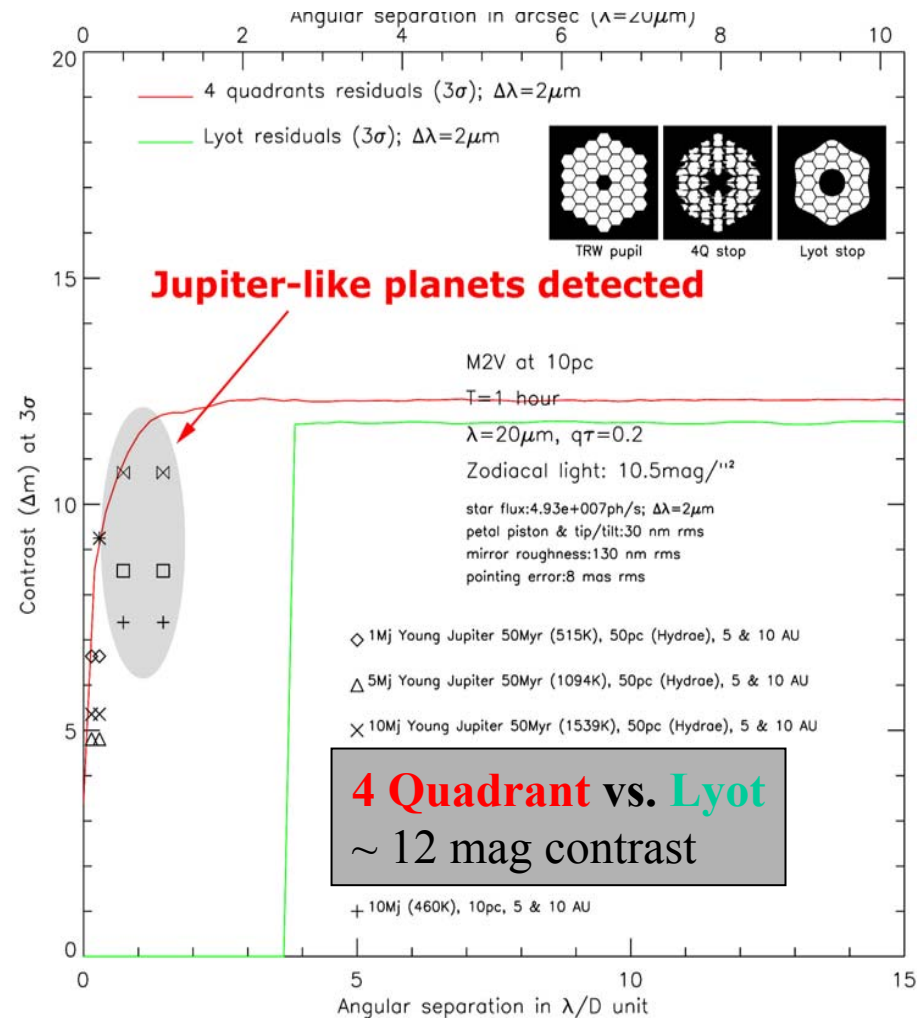
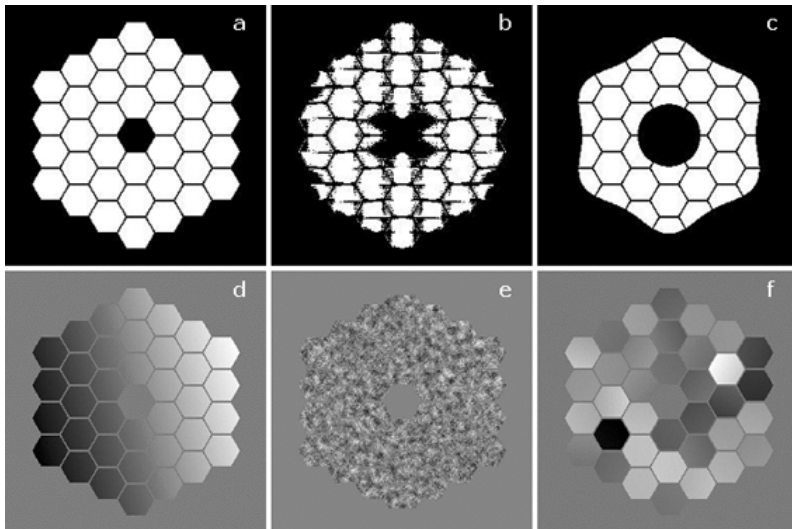
Various coronagraphic techniques can reduce the light diffracted out of the peak,

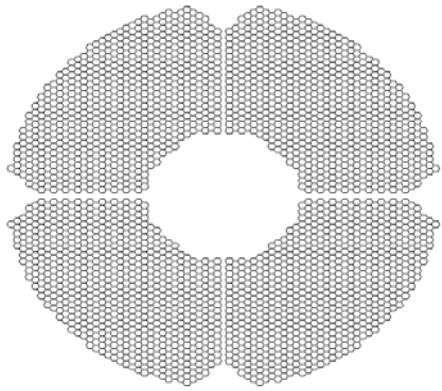
**But**

- Complex pupil shape is a problem
- Chromatism is another problem
- High contrast translates in high light loss

**Therefore**, to make the problem manageable,

- make the pupil as “clean” as possible
- don't ask for extreme contrast increase



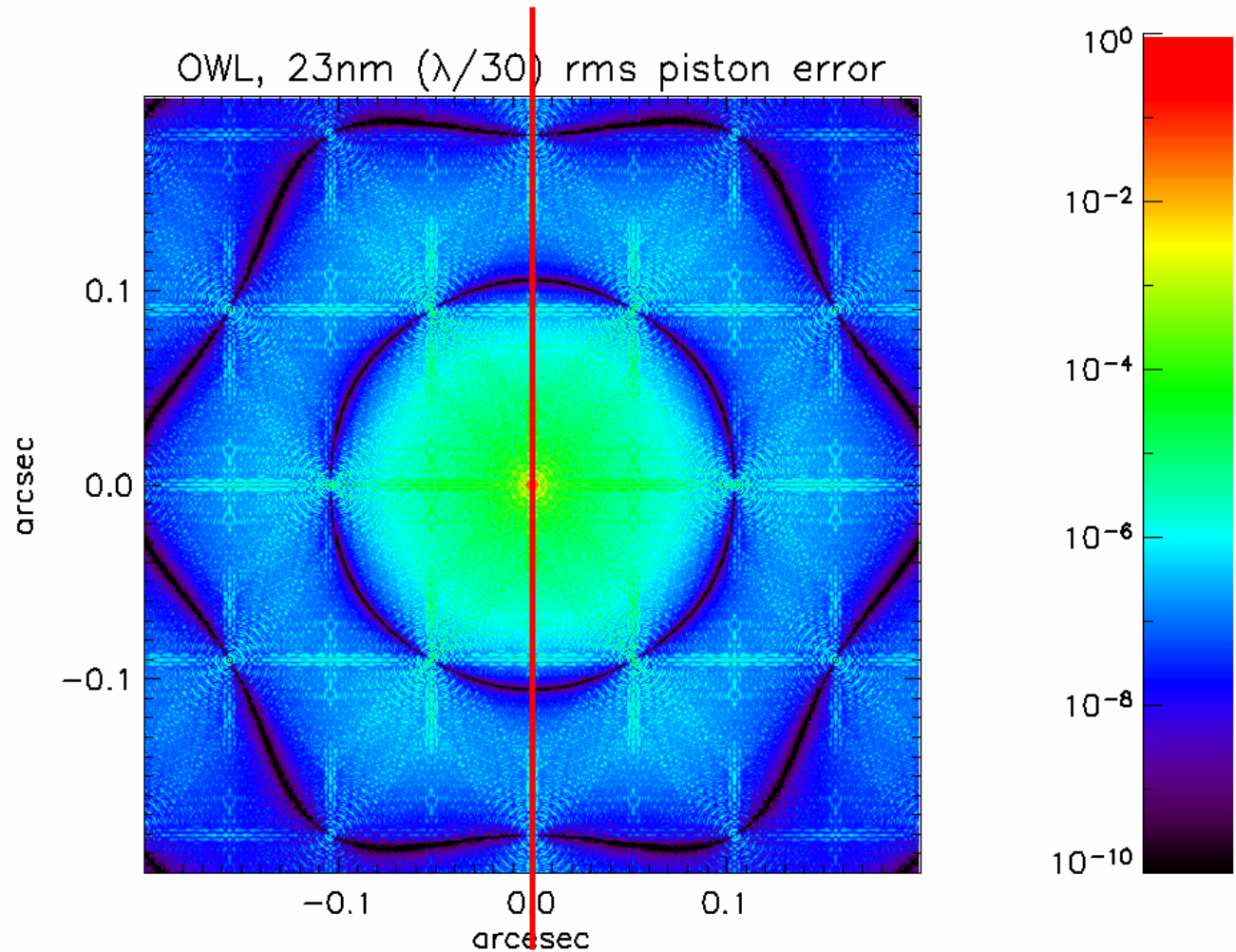


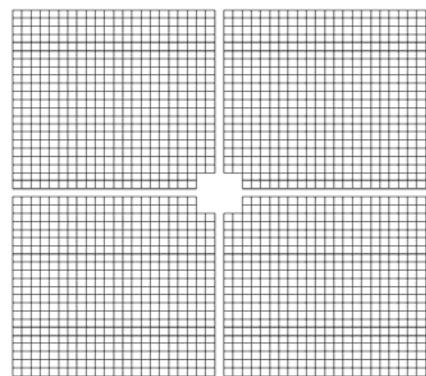
## OWL-like pupil, R band

100m diameter,  
10mm gap,

1.6m side-to-side hexagonal segments  
33% obscuration

PSF at 700 nm  
computed by A Riccardi  
Following the analytical  
approach of  
**Yaitskova\_et\_Al\_2002,**





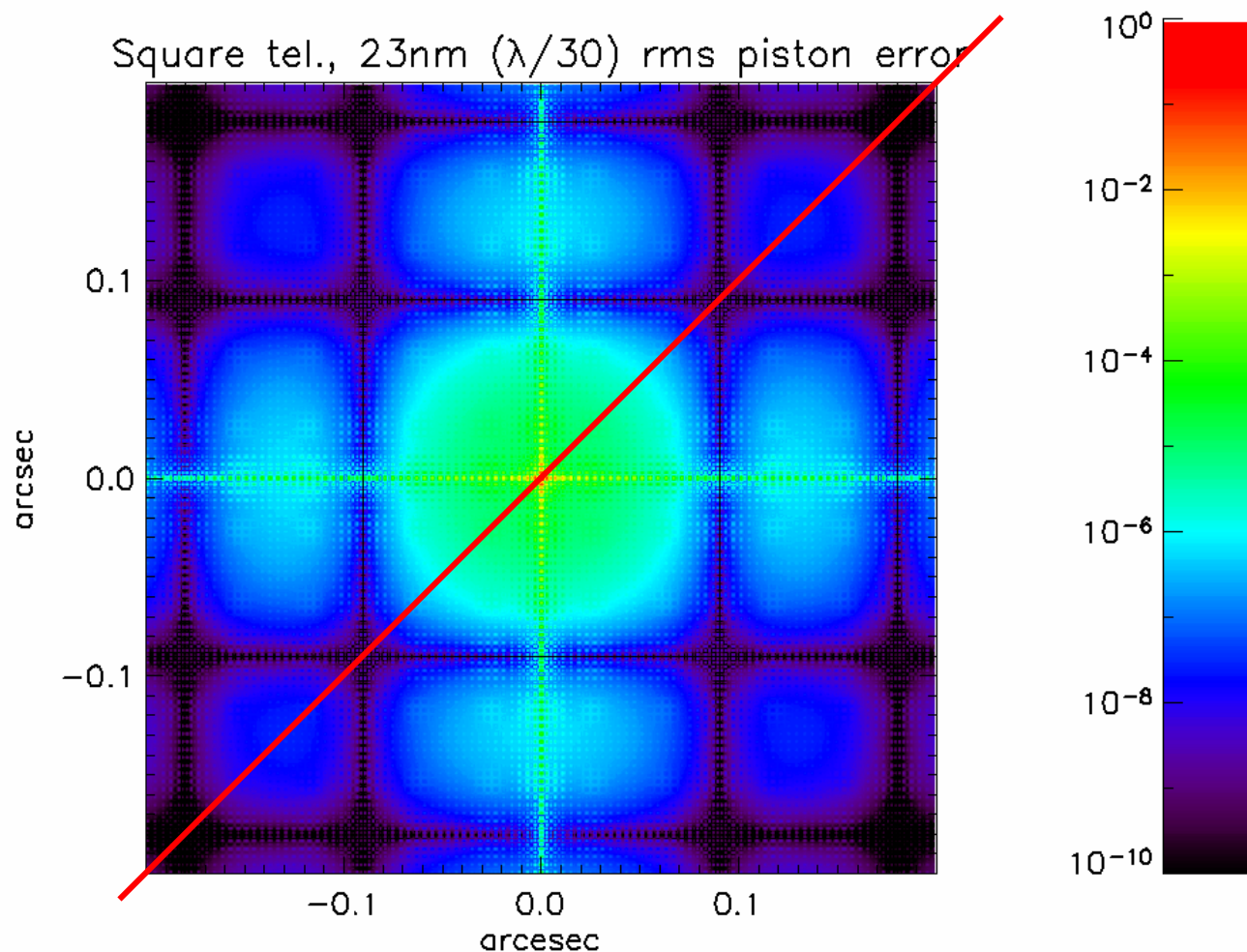
**71 m square pupil, R band**

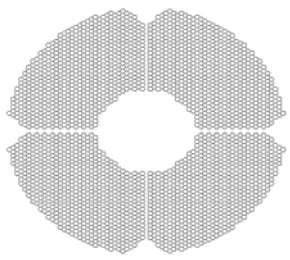
**100m diagonal ~ same area as OWL**

1.6m side square segments

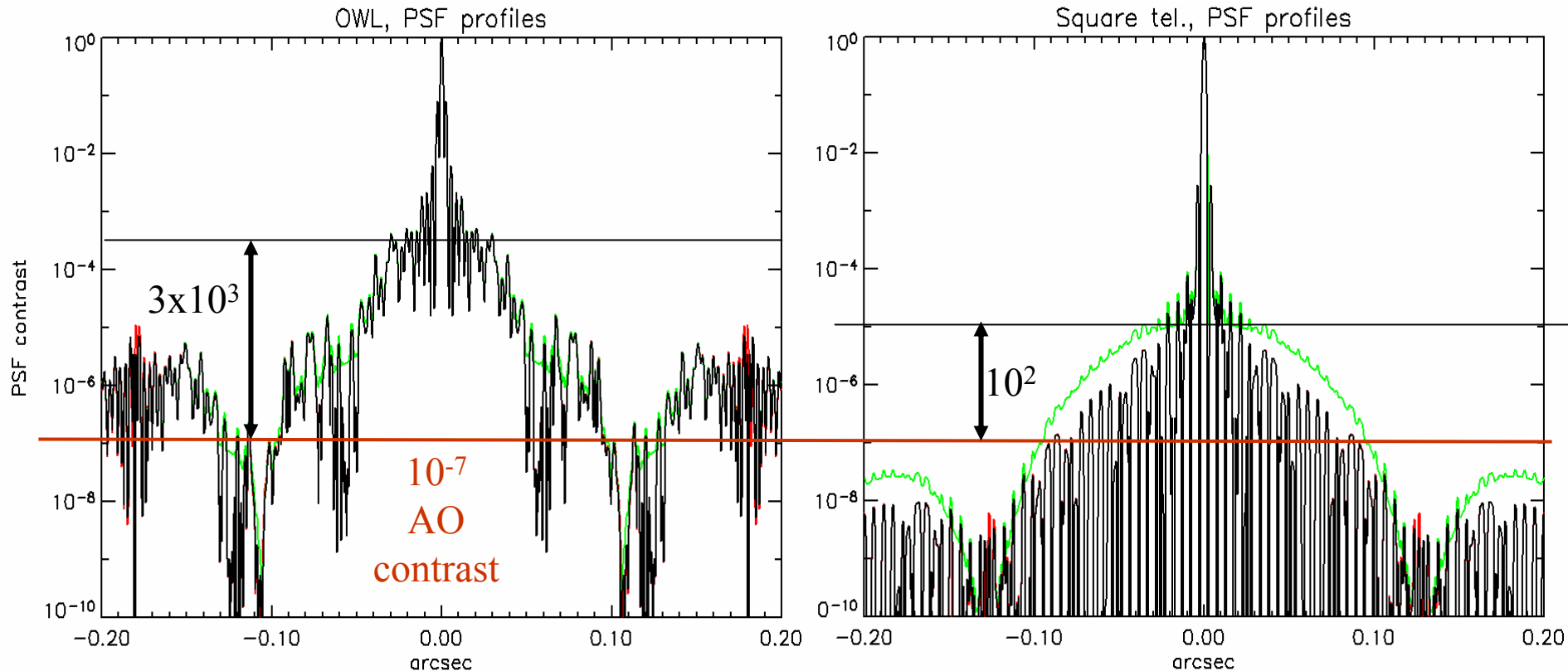
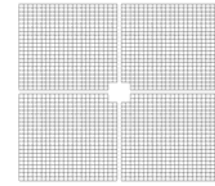
10mm gap, 10% obscuration

PSF at 700 nm  
computed by A Riccardi  
Following the analytical  
approach of  
**Yaitskova\_et\_Al\_2002,**





## Comparison of the 700 nm profiles



Black, no gaps

Red, 10mm gaps

Green, 23nm rms wf piston

**Coronagraphy can remove most of the structure, *BUT NOT PISTON***

## Is Piston Error the *show stopper*?

Piston errors send light mostly within an angle  $\alpha \sim \lambda/d$  ( $d$ =segment size)

To reduce the piston problem we could:

- **use much larger segments**, to obtain  $\alpha \sim 20\text{-}30$  mas ( $d > 5$  m at V)  
(doesn't work at longer wavelength)
- **use much smaller segments**, to obtain  $\alpha > 1000$  mas ( $d < 0.2$  m at V)  
(this works well in principle, but the number of segments diverges and their control becomes a new big problem)
- **reduce piston rms error by ~ an order of magnitude** (from  $\sim 20$  nm to  $\sim 2$  nm wf)  
Scaling from Esposito et Al. 2003 one finds that 2 nm rms WF differential piston error can be measured by a Pyramid WFS on a star of mag  $\sim 8$  with sufficient bandwidth (tens of Hz) to control segment vibrations and atmospheric terms.

**Differential segment piston can (MUST) be controlled adaptively!**



so ... what type of AO is needed *to study exo-earths*?

Appropriate wf corrector(s):

- A very high order corrector ( $\Delta \sim 10$  cm,  $> 2$  kHz bandwidth, any conjugation)  
**The high order corrector MUST be segmented to control segment piston  
this has profound (positive?) implications on many AO parameters**
- Possibly a medium order corrector at a high conjugate to control scintillation

And, in addition:

- A Piston sensitive wavefront sensor (Pyramid WFS, for instance)
- Large, fast WFS detectors
- A lot of computing power (maybe)



## Opinions on segmented correctors

*If a typical segment is  $\sim 2 \text{ m}^2$  we only need  $\sim 200$  DoF per segment. The problem is NOT in the corrector size or complexity, but in accuracy of correction, gap size, edge effects, speed, reliability, cost . . .*

*Let different approaches compete, then choose the winner!*

### Options (in my personal order of preference):

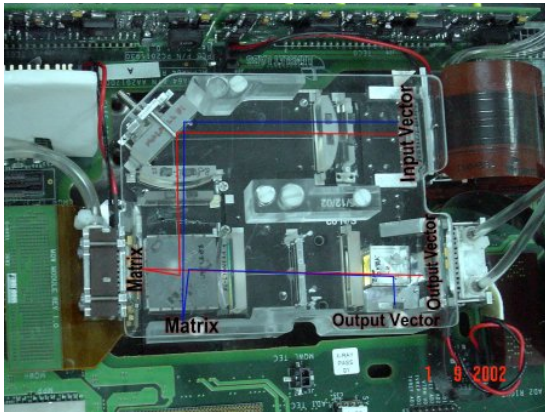
1. use **adaptive primary mirror segments** (Riccardi et Al. 2003)
2. use “**adaptive secondary technology**” with higher actuator density somewhere else in the telescope (**with segmentation scaled from primary segmentation**)
3. use **segmented, buttable, Piezo or MEM correctors on piezo tripods** (piston-tip-tilt) at a re-imaged pupil (**with segmentation scaled from primary segmentation**)

## Opinions on WFS, detectors, computers

### *Piston sensitive WaveFrontSensors:*

- there are many good ideas and approaches for split pupils
- there are quantitative laboratory measurement in one case  
( Esposito et Al. 2003, on Pyramid sensor)
- there are enough photons

*Not anymore a problem*



### *Computing power*

- *segmented correctors can use hierarchical algorithms*
- computational needs ca also be reduced in other ways
- if necessary, optical computing is becoming reality!  
(an optical DSP doing 8 Tera Multiply+Add Operations/s soon on the market by a company from Israel)

### *Fast, large detectors*

A 512x512 LLLCCD (E2V ccd 87, 11 Mpix/s) is on the market only needs multiple (24) readout amplifiers (known technology)

*It will not remain a problem for a long time!*

# Opinions on telescope and site

## A: Telescope

- We better avoid using a large but not optimized telescope for detection because a smaller, well optimized and well located, telescope can outperform the larger one.
- A telescope optimized for extrasolar planets can do everything else optimally (the corrected field can be increased with the addition of extra post-focus conjugates)

## B: Site

- We need to understand whether Antarctica really is what somebody says: something intermediate between ground and space (Storey et Al. 2002)
- If it is, that is the place to go to!  
(even with a small 30 m telescope)

## Conclusion

*Let's start discussing  
what we want to learn  
about extrasolar planets,  
earths in particular  
they seem to be  
well within reach  
of  
ELT*

# Correspondence of file names with references

To make consultation easier I will place the following files (cited in the slides) at the address:

[www.arcetri.astro.it/~salinari/ELT](http://www.arcetri.astro.it/~salinari/ELT)

- Angel\_2002.pdf:** R. Angel, “*Imaging exoplanets from the ground*”, ASP Conference Series, *Scientific Frontiers in Research on Extrasolar Planets*, eds. S. Seager and D. Deming, Washington D.C. 2002.
- Jolissaint\_Veran\_2001.pdf:** L. Jolissaint and J. Veran, “*Fast computation and morfologic interpretation of the Adaptive Optics Point Spread Function*”, Venice 2001 Conf. *Beyond Conventional Adaptive Optics*,
- Esposito\_et\_Al\_2003:** S. Esposito, E. Pinna, A. Tozzi, P. Stefanini, N. Devaney, “Co-phasing of segmented mirrors using pyramid sensors” SPIE Proceedings, S Diego.
- Hawarden\_et\_Al\_2002.pdf:** T. G. Hawarden, D. Dravins, G.F. Gilmore, R. Gilmozzi, O. Hainaut, K. Kuijken, B. Leibundgut, M.R. Merrifield, D. Queloz & R.F.G. Wyse, “*Critical science with the largest telescopes: science drivers for a 100m ground-based optical-IR telescope*”, Proc. of SPIE Vol. 4840
- Lardiere\_et\_Al\_2003.pdf:** O. Lardiere, P. Salinari, L. Jolissaint, M. Carbillet, A. Riccardi, S. Esposito,; “*Adaptive optics and site requirements for search of earth-like planets with ELTs* ” (Proc. of II Backaskog conference on ELTs)
- Riaud\_et\_Al\_2001.ps:** P. Riaud, A. Boccaletti, D. Rouan, F. Lemarquis, A. Labeyrie, “*The four-quadrant phase-mask coronagraph. II, Simulations*”, PASP 113:1145-1154, 2001 September.
- Riccardi\_et\_Al\_2003.pdf:** A. Riccardi, C. Del Vecchio, P. Salinari, G. Brusa, O. Lardiere, D. Gallieni, R. Biasi, P. Mantegazza, “Primary adaptive mirrors for ELTs: a report on preliminary studies” (Proc. of II Backaskog conference on ELTs)
- Storey\_et\_Al\_2002.pdf:** J. Storey, M. Burton, M. Ashley, “*Antartica as stepping stone to space*”,  
<http://www.phys.unsw.edu.au/~mgb/Antbib/stepping-stone.pdf>
- Verinaud\_Esposito\_2002:** C. Verinaud and S. Esposito, “*Adaptive optics correction of a stellar interferometer with single pyramid wavefront sensor*,” Opt. Letters , 2002.
- Yaitskova\_et\_Al\_2002.pdf:** N. Yaitskova, K. Dohlen, P. Dierickx, “*Diffraction in OWL: effects of segmentation and segment edge misfigure*”, Proc. of SPIE Vol. 4840

# Useful scaling rules and relations (Lardiere et Al. 2003)

## *Symbols and definitions*

Fried's coherence length	$r_0$
Coherence time	$\tau_0$
Turbulence weighted wind speed	$v_0$
Telescope diameter	$D$
Actuator separation	$\Delta$
Field angle	$\alpha$
Contrast due to RWE	$C(\alpha)$

$$C(\theta) = \frac{\sum_n \sum_n PSF(\theta)}{\iint_{\infty} PSF}$$

(sums on planet pixels)

Contrast with coronagraph	$Co(\alpha)$
Strehl ratio	$S$
Integration time	$T$
Photon flux usable by wfs	$Q_{ph}$

## *Scaling rules:*

$$\alpha = \lambda/W$$

$$C(\alpha) \propto D^{-2} \text{ (at given } \alpha, S \sim 1)$$

$$C(\alpha) \propto (\Delta/r_0)^2 \text{ (if not limited by } Q_{ph})$$

$$Q_{ph} \propto (r_0)^3/v_0$$